



**Universidad**  
Zaragoza

# Directional axion detection

**Ciaran O'Hare**

**Universidad de Zaragoza, España**

Based on [arxiv:\[1806.05927\]](https://arxiv.org/abs/1806.05927)

with S. Knirck, A. Millar, J. Redondo, F. Steffen

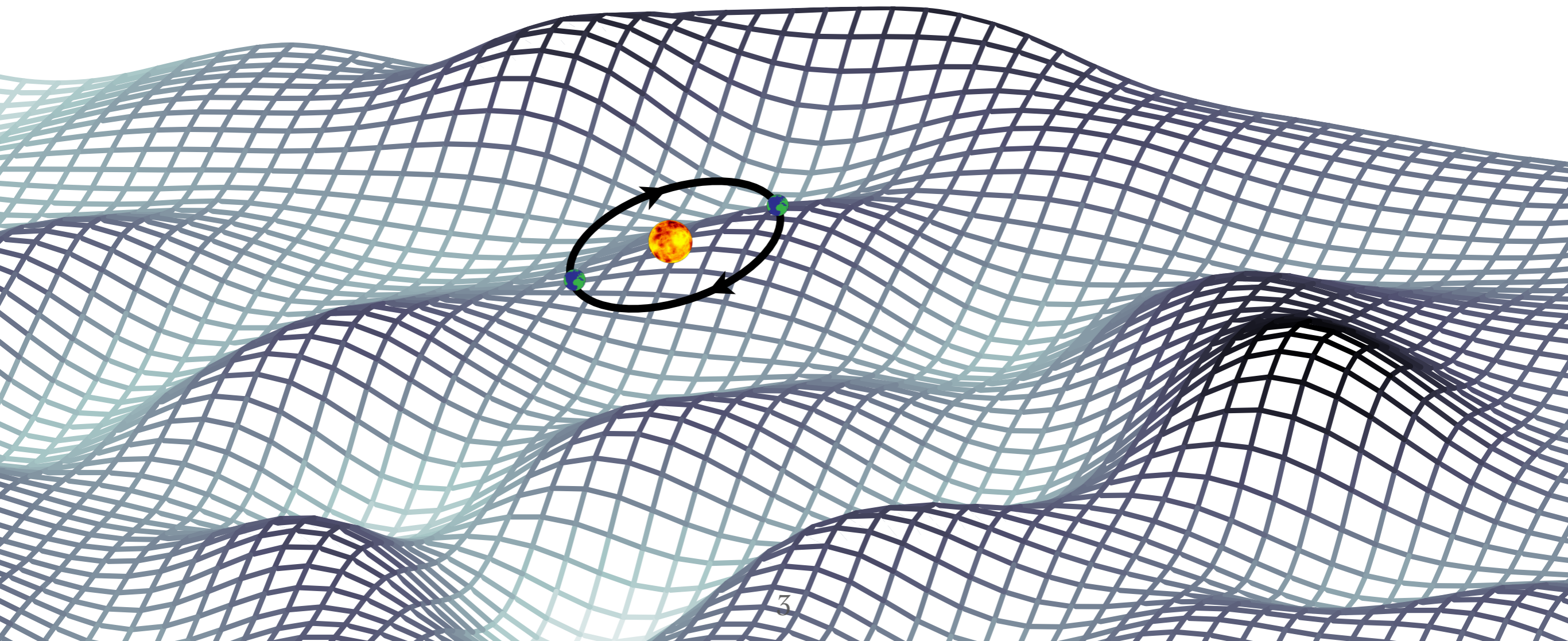
# A directional axion experiment?

- What?
- Is it possible?
- Is it worth it?

**DM axion field:**  $a(\mathbf{x}, t) \approx \frac{\sqrt{2\rho_a}}{m_a} \cos(\omega t - \mathbf{p} \cdot \mathbf{x} + \alpha)$

Oscillations in time:  $\omega = m_a \left( 1 + \frac{v^2}{2} \right)$

Oscillations in space:  $\mathbf{p} = m_a \mathbf{v}$



# The axion field will actually be made of some distribution of modes

$$a(\mathbf{x}, t) = \frac{\sqrt{2\rho_a}}{m_a} \int \frac{d^3\mathbf{p}}{(2\pi)^3} |\mathcal{A}(\mathbf{p})| \cos(\omega t - \mathbf{p} \cdot \mathbf{x} + \alpha_{\mathbf{p}})$$

Related to  $f(\mathbf{v})$ , width  $\sim \sigma_v$

~Time scale for oscillation to dephase

$$\tau_a = \frac{2\pi}{m_a \sigma_v^2} \simeq 40 \mu\text{s} \left( \frac{100 \mu\text{eV}}{m_a} \right)$$

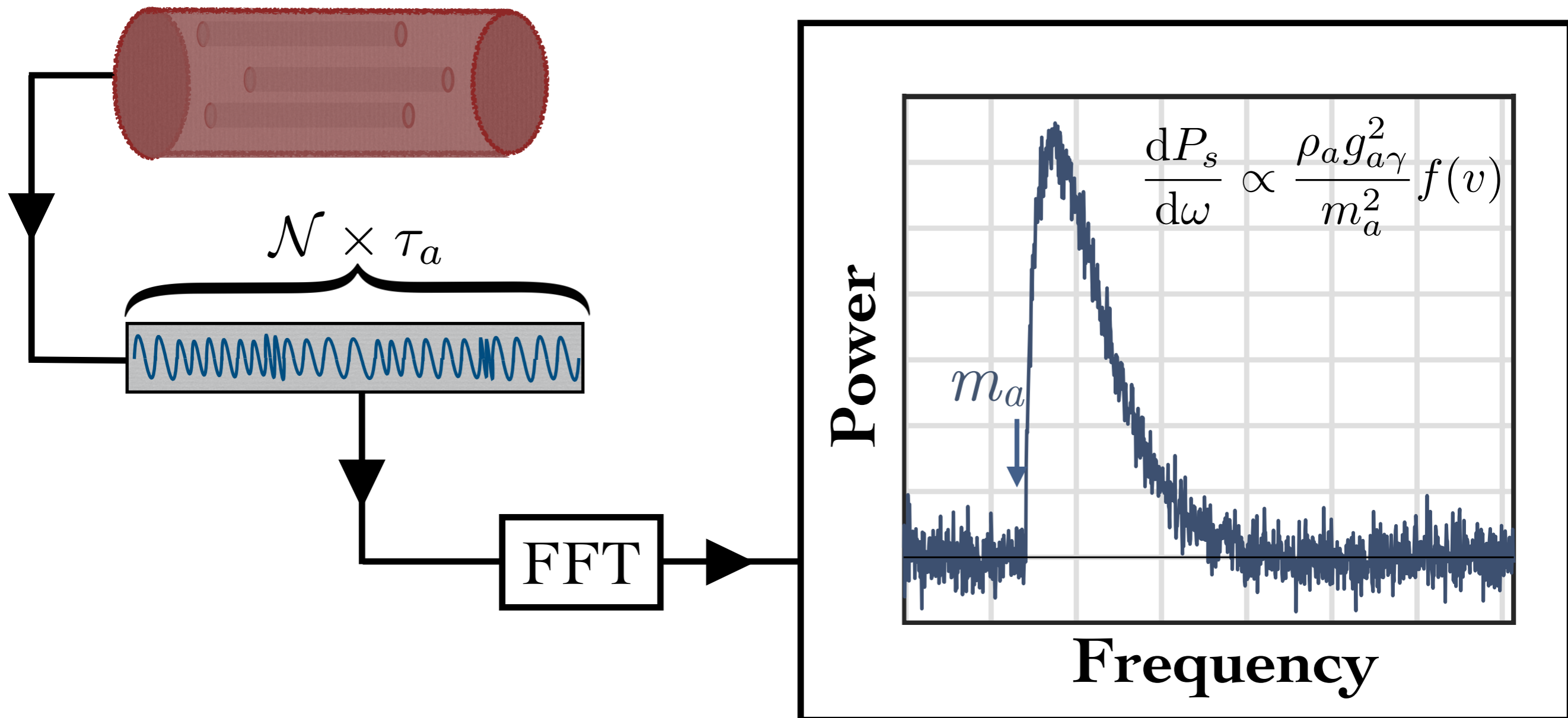
~Length scale for oscillation to dephase

$$\lambda_a = \frac{2\pi}{m_a \sigma_v} \simeq 12.4 \text{ m} \left( \frac{100 \mu\text{eV}}{m_a} \right)$$

# Measuring the axion distribution

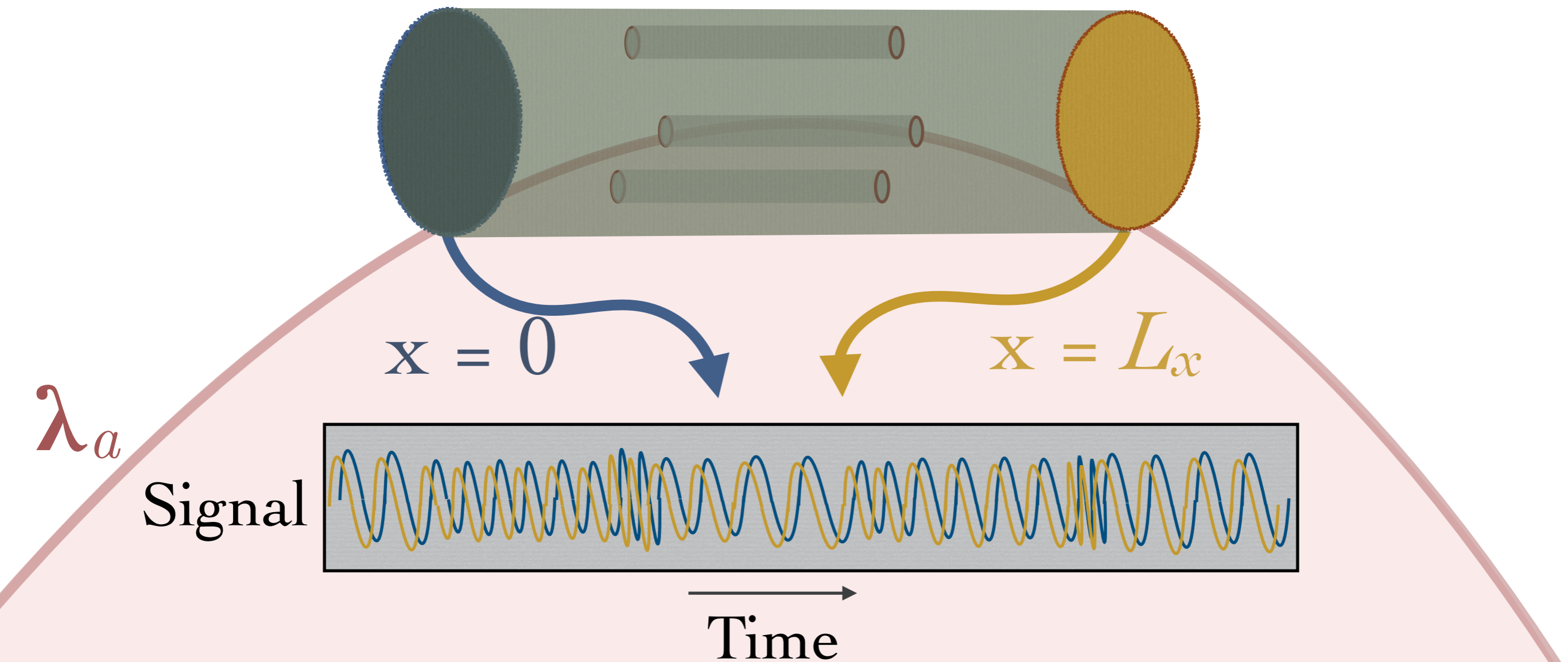
Sampling axion field over many coherence times:

→ Power spectrum  $\sim f(\nu)$



If axion wavelength  $\sim$  experiment size  
→ Phase difference across experiment

$$a = a_0 e^{i(\omega t - m_a \mathbf{v} \cdot \mathbf{x})}$$



# A general formalism

- Parameterise with velocity dependent form factor:

$$P \propto C(\mathbf{v}) = C_0 \left( 1 - \mathcal{G}(\mathbf{v}) \right)$$

- At lowest order in  $v$ , an experiment will be linearly or quadratically directional

**Linear directionality** (l-type)  $C(\mathbf{v}) = C_0 \left( 1 - \sum_{i=x,y,z} g_\ell^i v_i \right)$  Directional correction positive or negative

**Quadratic directionality** (q-type)  $C(\mathbf{v}) = C_0 \left( 1 - \sum_{i=x,y,z} g_q^i v_i^2 \right)$  Directional correction always negative

# Signal from distribution of velocities

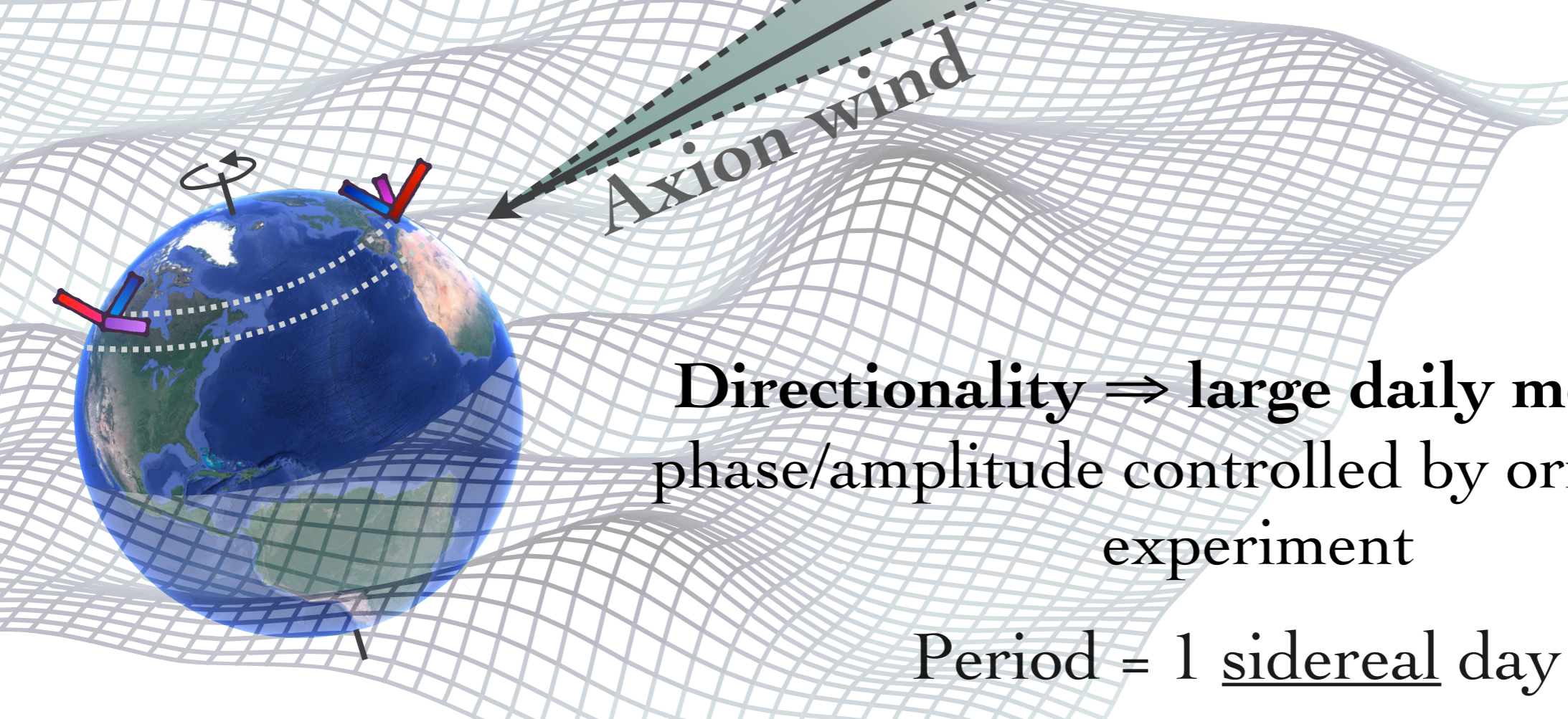
→ Power spectrum now includes integral over **directions**.

$$\frac{dP}{d\omega}(t) = P_0 \mathcal{T}(\omega) \frac{dv}{d\omega} \left( \underbrace{f(v; t)}_{\text{Non-directional speed effect}} + \underbrace{\int d\Omega_v v^2 \mathcal{G}(\mathbf{v}) f(\mathbf{v}; t)}_{\text{Directional velocity effect} \rightarrow \text{Orientation dependent}} \right)$$

Total power →  $P_0 \mathcal{T}(\omega)$   
 Mode/Boost factor →  $\mathcal{T}(\omega)$   
 Non-directional *speed* effect →  $f(v; t)$   
 Directional *velocity* effect → Orientation dependent →  $\int d\Omega_v v^2 \mathcal{G}(\mathbf{v}) f(\mathbf{v}; t)$

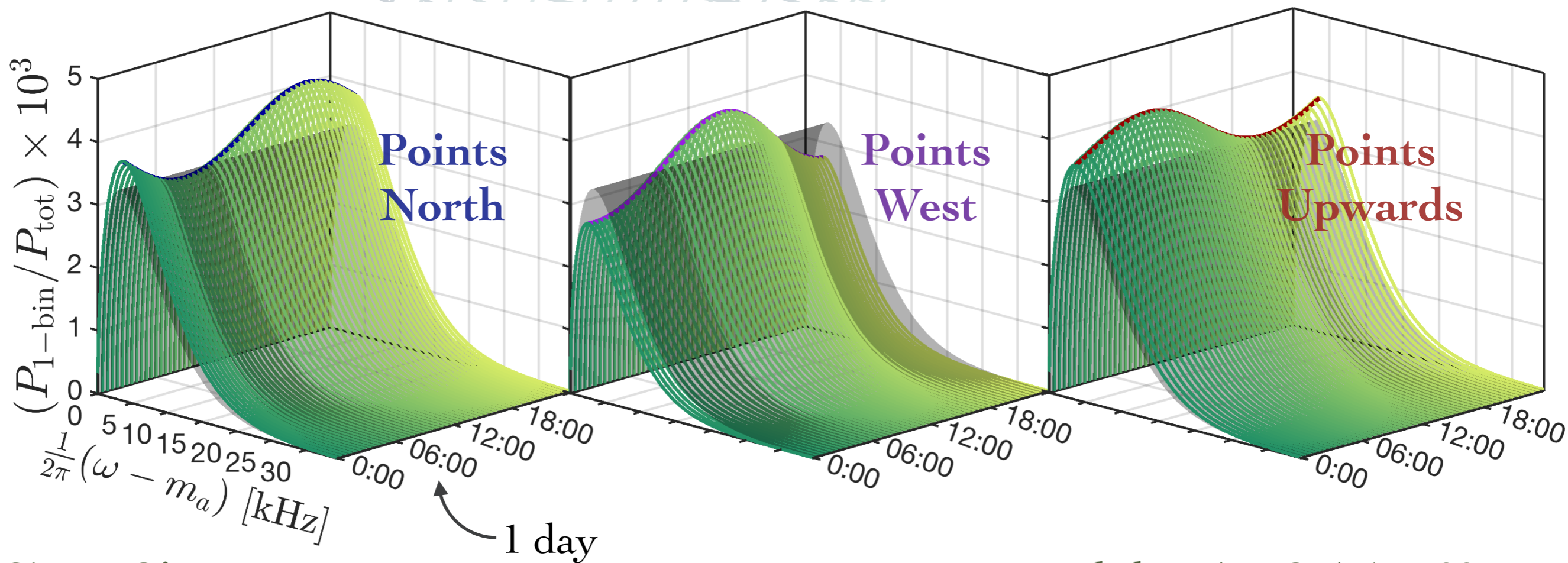
$$\omega = m_a \left( 1 + \frac{v^2}{2} + \dots \right)$$





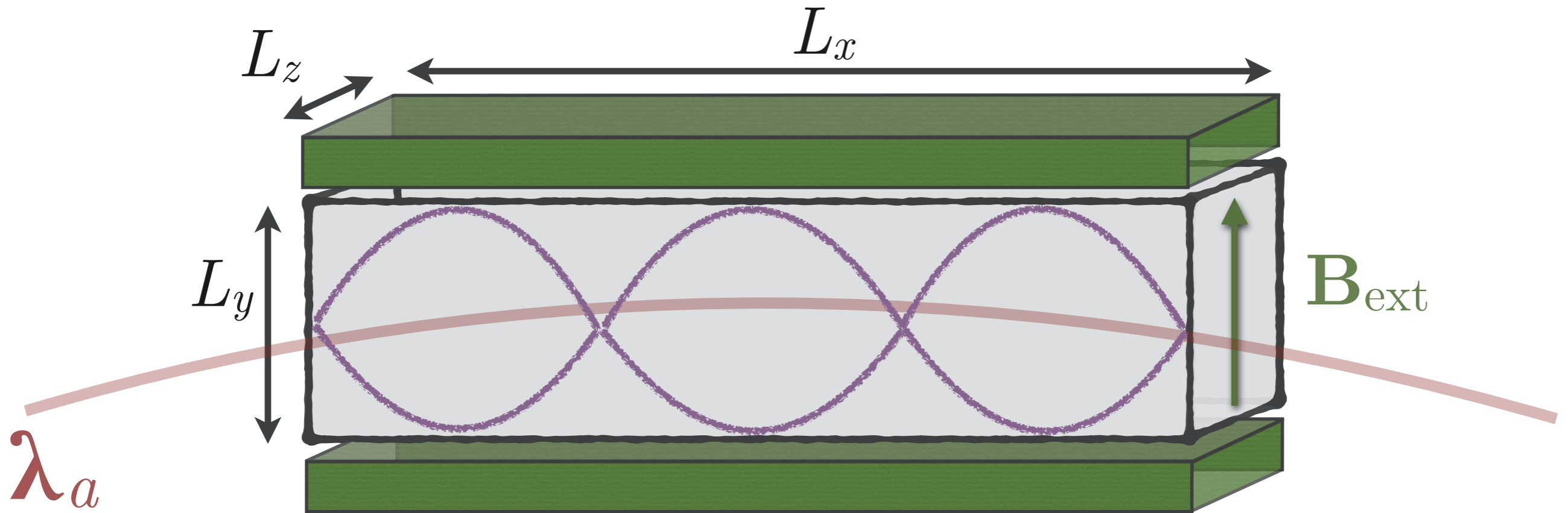
**Directionality**  $\Rightarrow$  large daily modulation  
 phase/amplitude controlled by orientation of  
 experiment

Period = 1 sidereal day



**Is it possible in practice?**

# Simple example: rectangular cavity

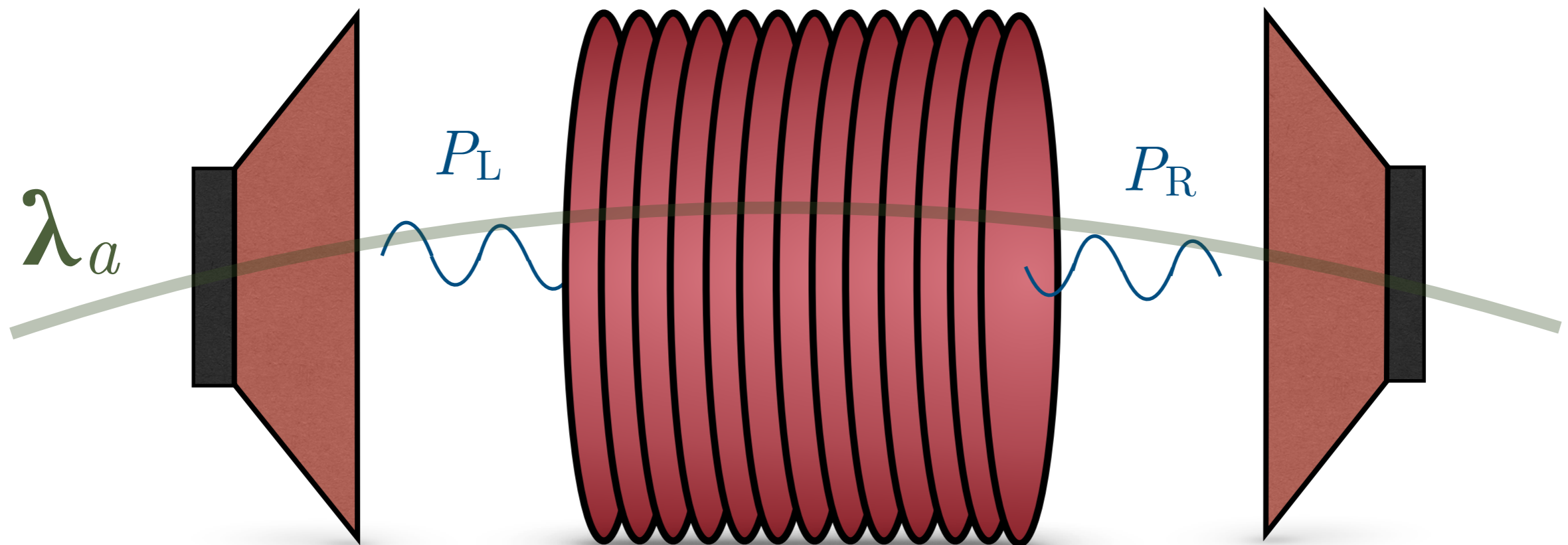


TE<sub>10n</sub> form factor modified for axion with non-zero  $\mathbf{v}$   
 $\rightarrow$  quadratically dependent on  $v_x$

$$C(\mathbf{v}) = \frac{1}{V B_{\text{ext}}} \int dV \mathbf{e}_{10n} \cdot \mathbf{B}_{\text{ext}} e^{im_a \mathbf{v} \cdot \mathbf{x}} \simeq \frac{64}{l^2 n^2 \pi^4} \left[ 1 - \left( \frac{m_a v_x L_x}{2} \right)^2 \right]$$

# More complex example: MADMAX-XL

- Scaled-up MADMAX with many disks spaced just out of phase from perfect constructive interference in the  $v=0$  limit



Combining signals from L/R

→ can be made **linearly or quadratically** sensitive to  $v$

# More complex example: MADMAX-XL

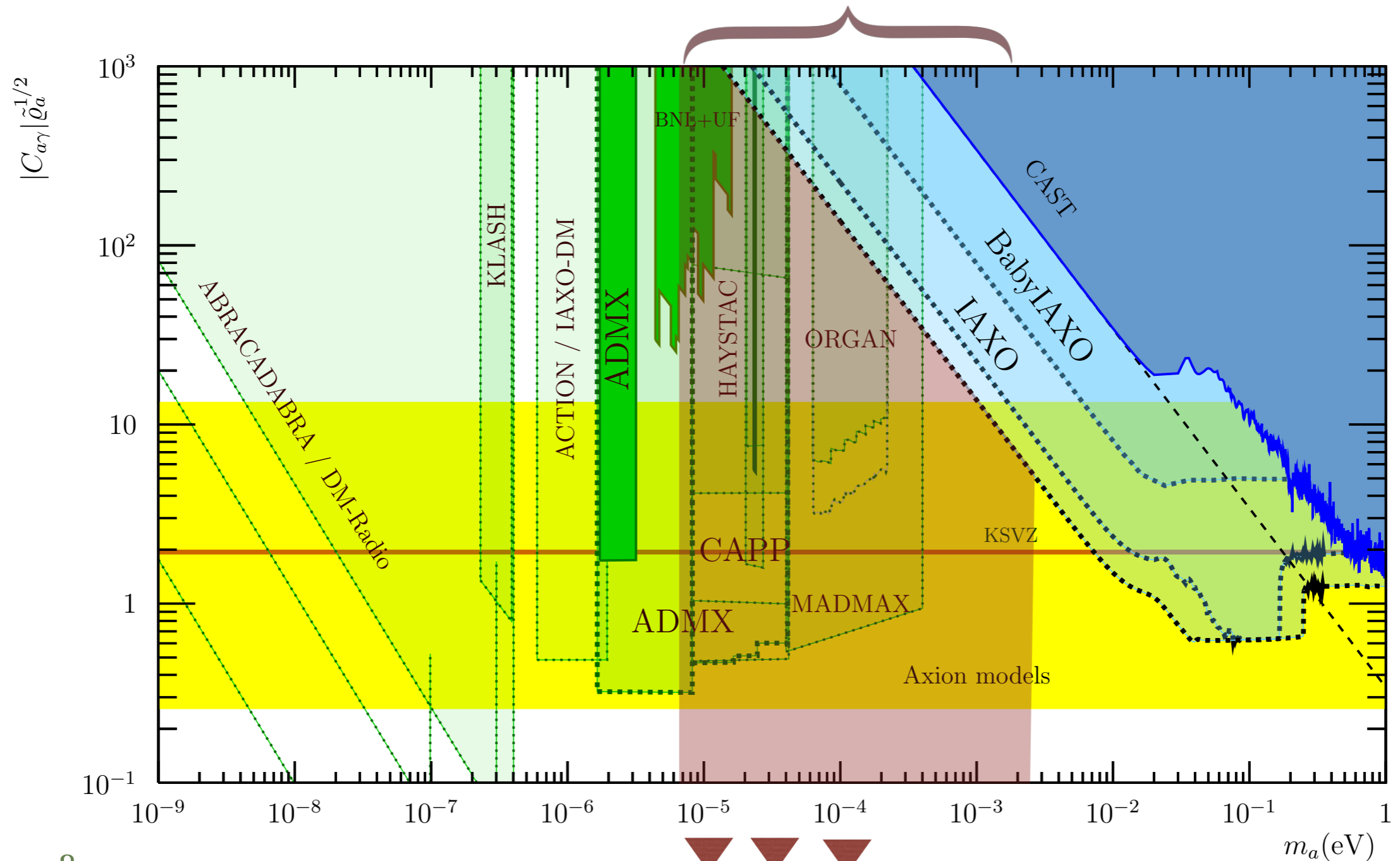
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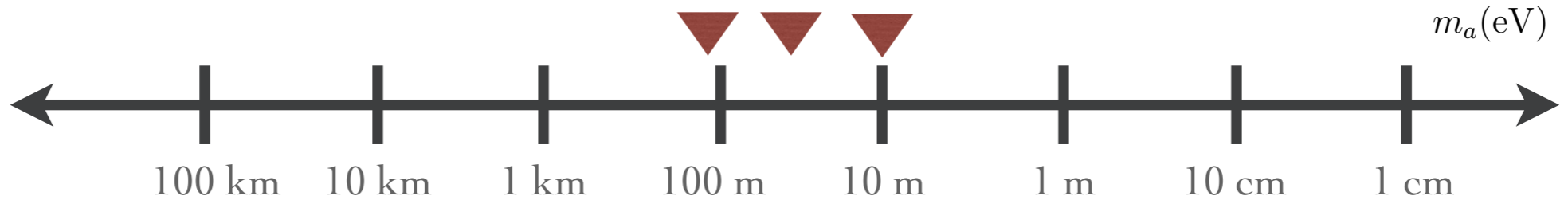
Combining signals from L/R

→ can be made **linearly or quadratically** sensitive to  $v$

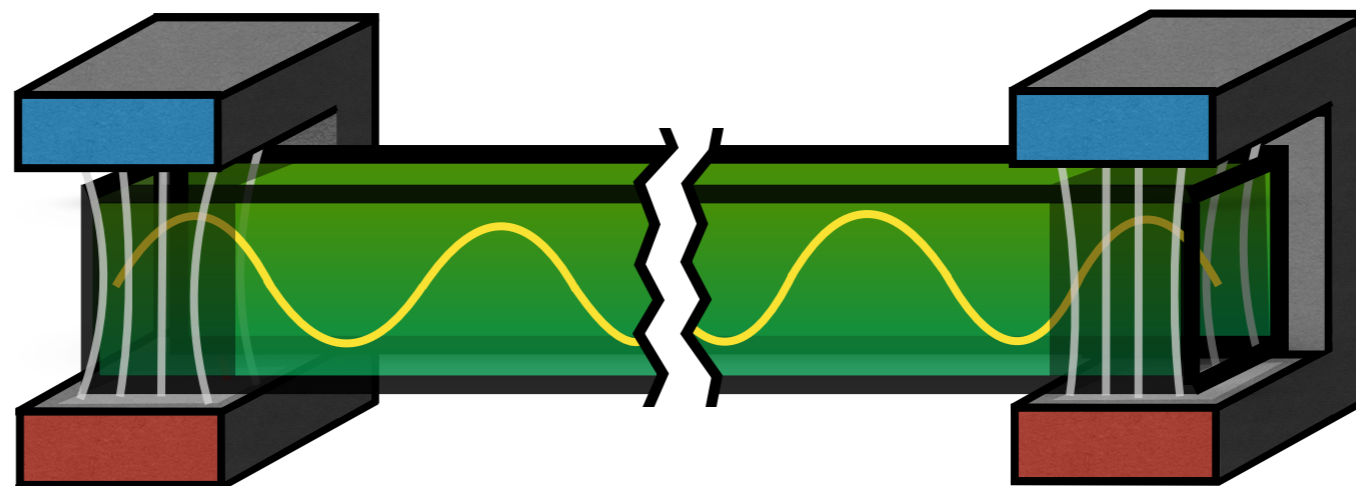
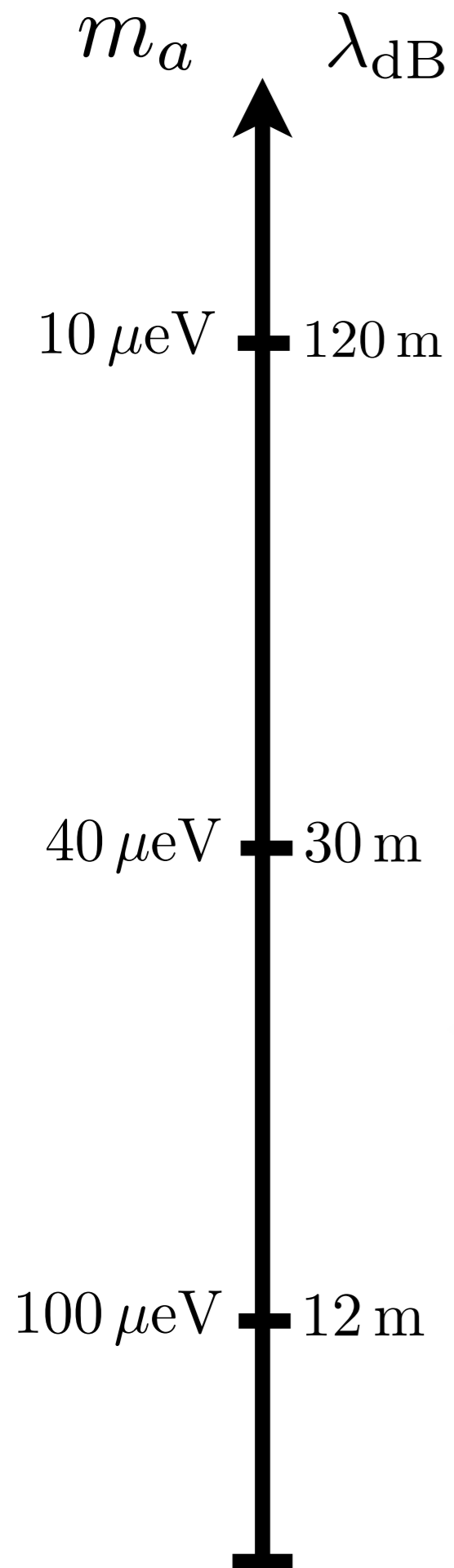
# Axion wavelength needs to be a “reasonable” size



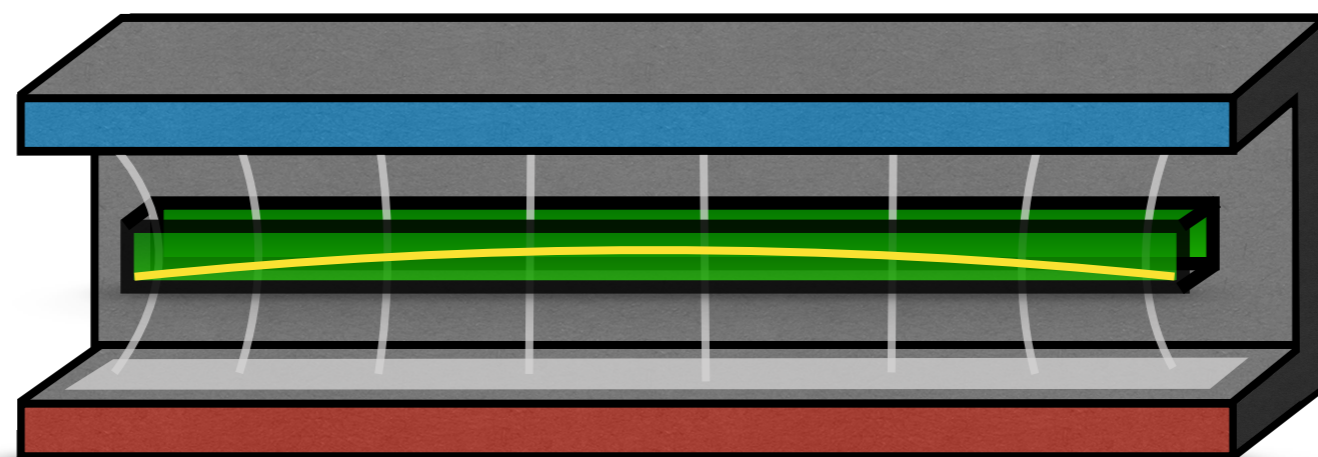
Irastorza &  
Redondo  
[1801.08127]



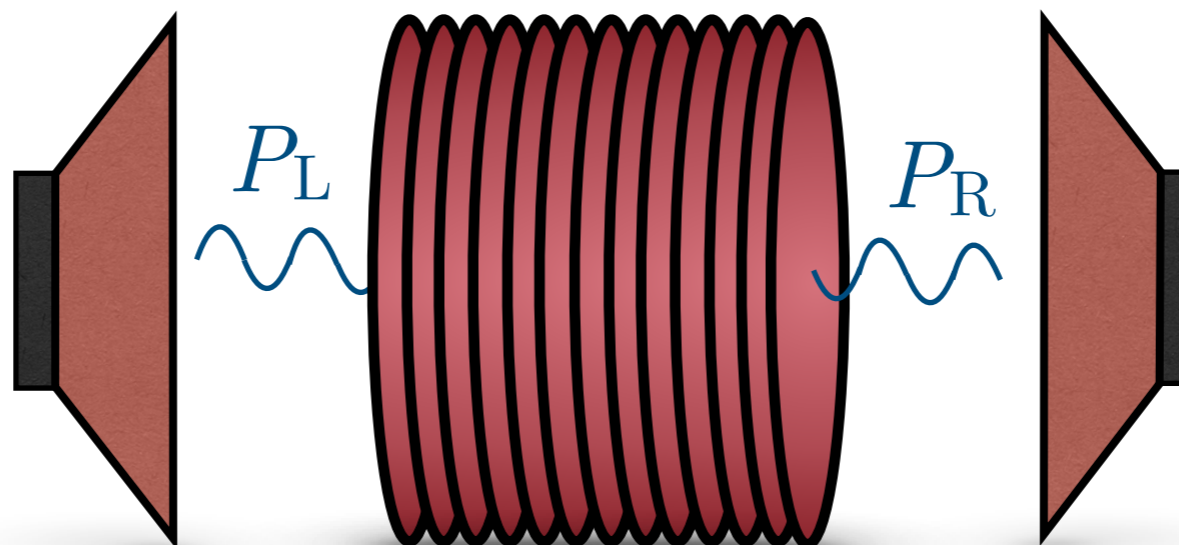
$\lambda_a$



**Partially  
magnetised  
cavity  
(q-type)**



**Thin cavity  
(q-type)**



**Dielectric disks  
(l or q-type)**

**What can you do with it?**



# What I won't talk about

**“Non-directional” signals** (from freq. dependence)

→ 5% annual modulation

→ 0.2% daily modulation

→ 2% gravitational focusing by Sun [Foster+\[1711.10489\]](#)

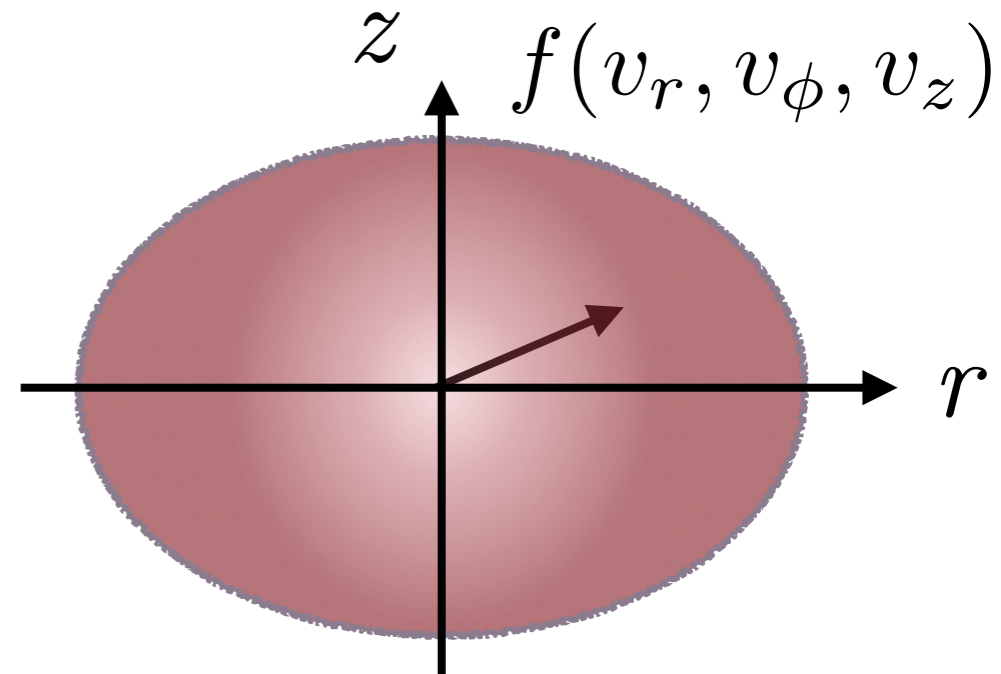
## **Axion astronomy**

- Measurement of Solar velocity [O'Hare+\[1701.03118\]](#)
  - ADMX can reach astrometric accuracy ~1 year after detecting axion
  - +directional detector can do it in 4 days. [\[see paper 1806.05927\]](#)
- Measurement of a dark disk [Foster+\[1711.10489\]](#)
- Measuring streams from miniclusters [\[see extra slides\]](#)

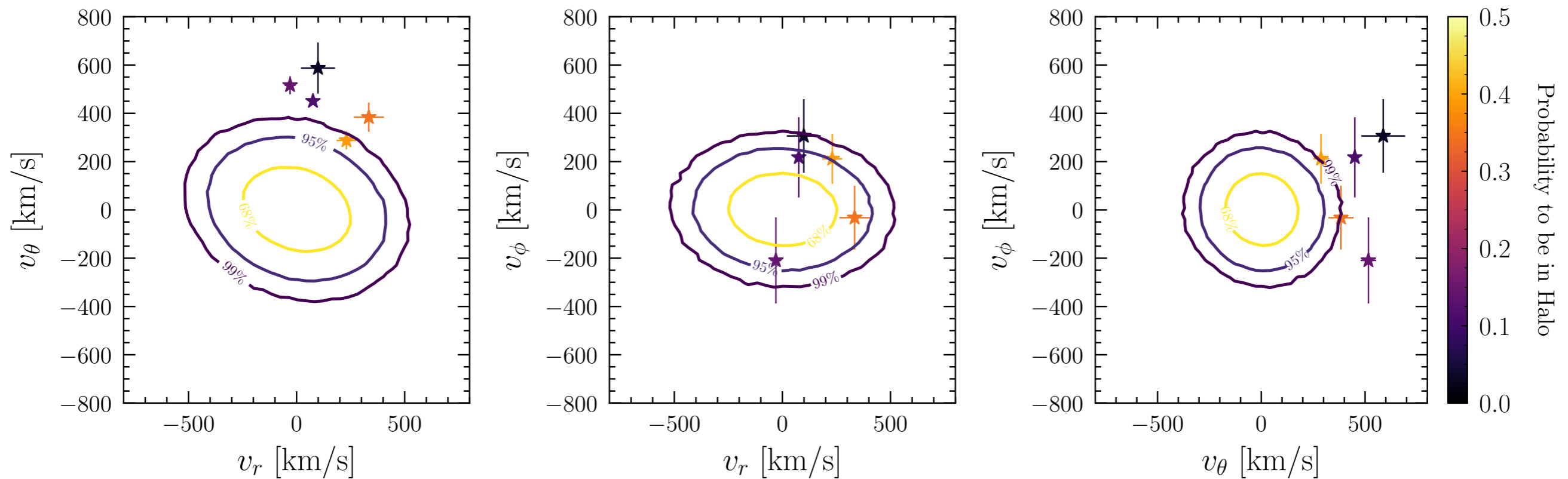
# Anisotropy of velocity ellipsoid

- Halos cannot be perfectly isotropic
- Radial infall  $\rightarrow$  typically leads to  $f(\mathbf{v})$  hotter in radial direction

$$\sigma_r > \sigma_{z,\phi}$$

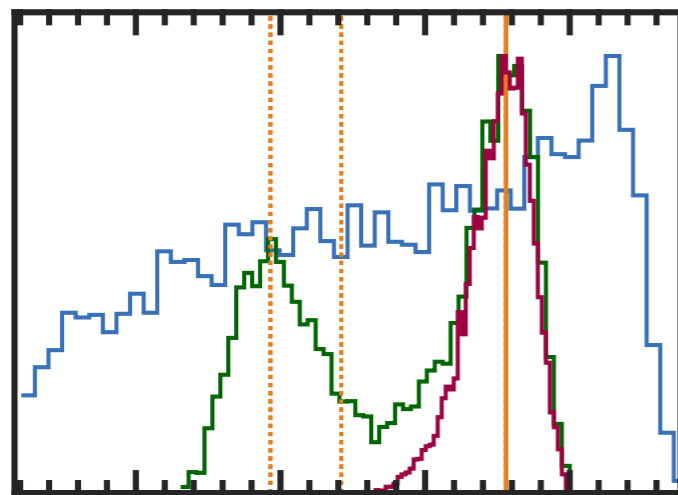


Herzog-Arbeitman [1708.03635]



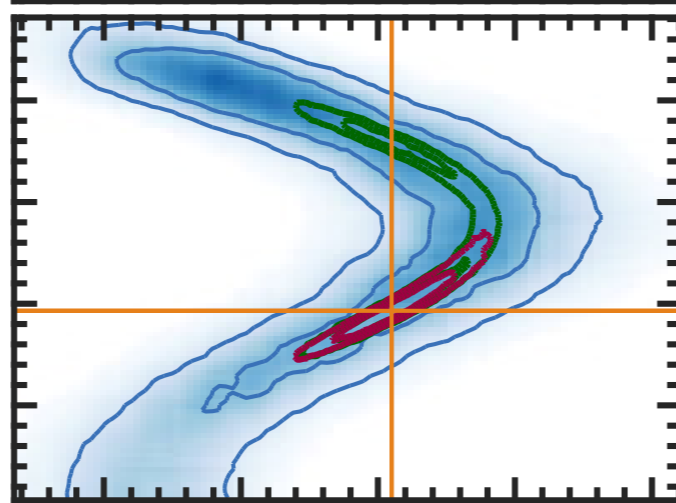
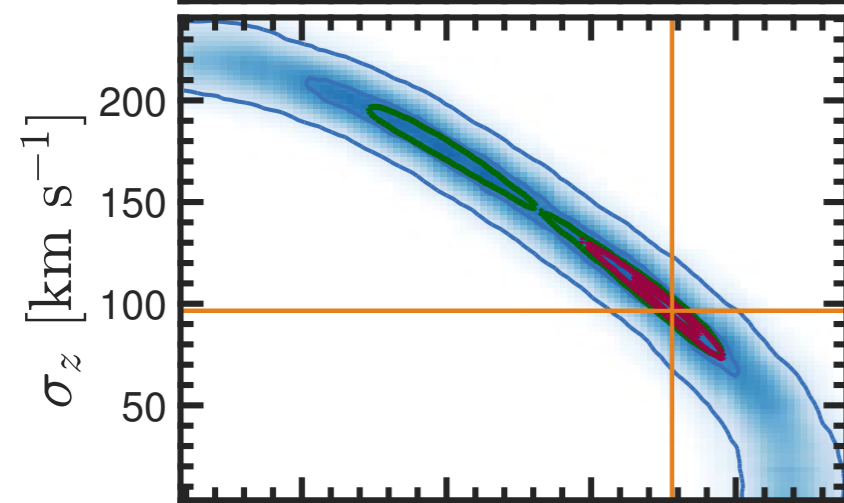
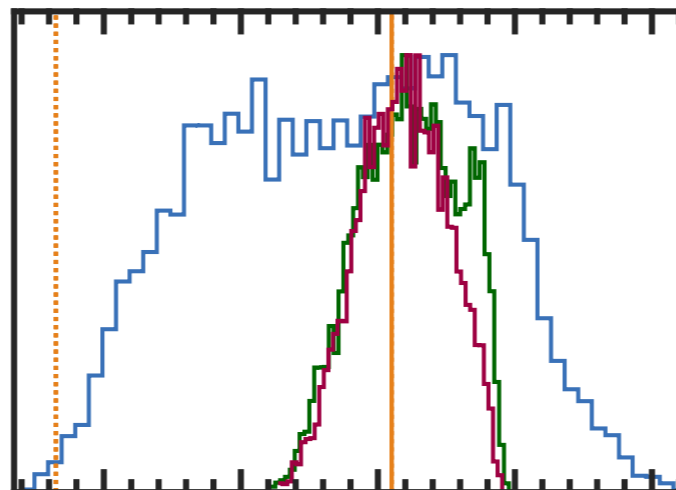
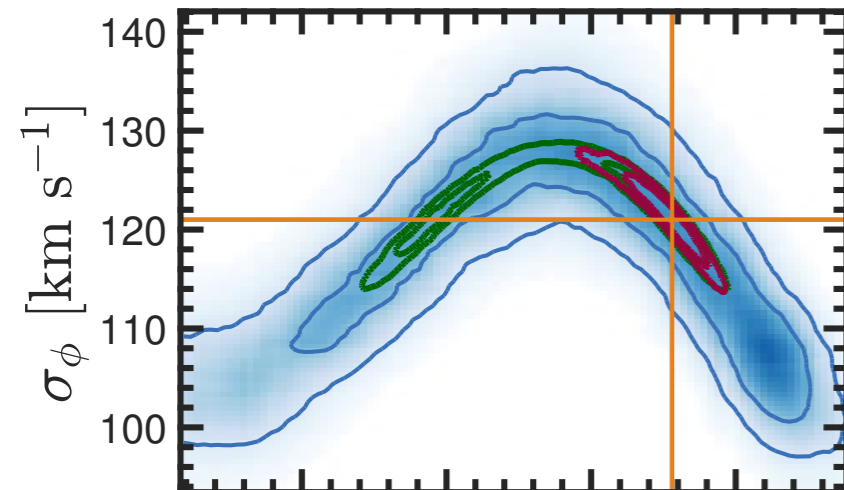
# Measuring halo anisotropy

## Radial

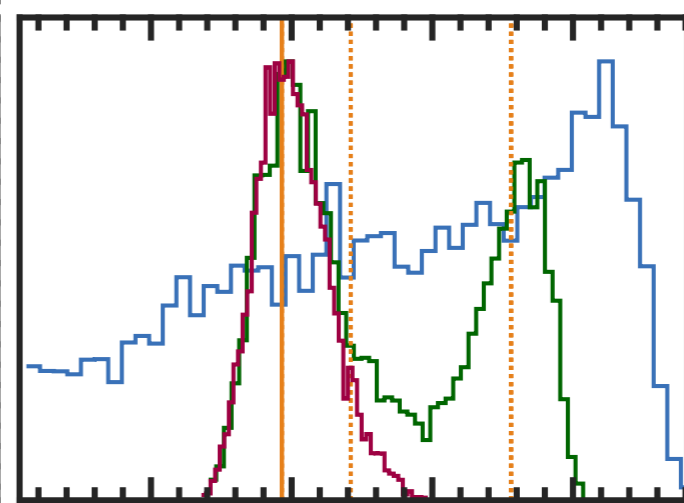


- Non-directional
- $\ell$ -type
- $q$ -type

## Azimuthal

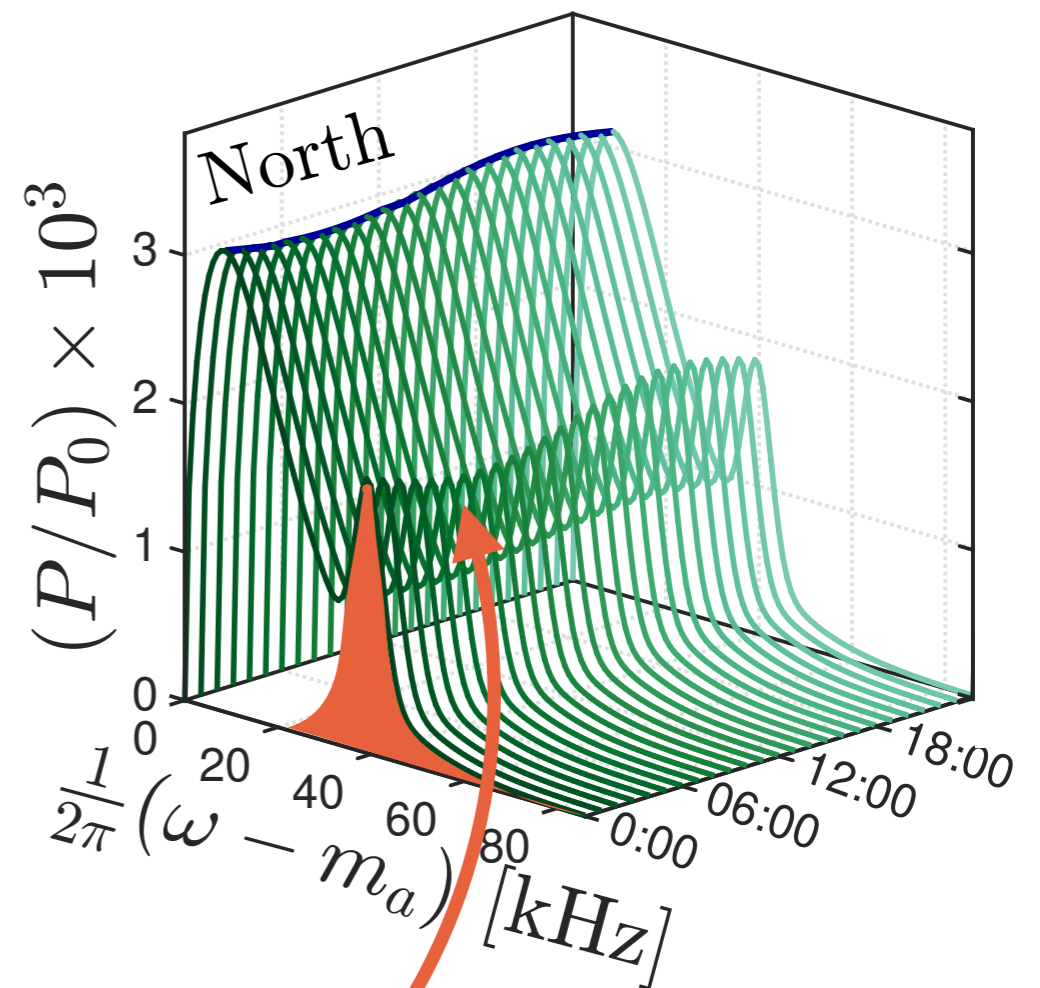
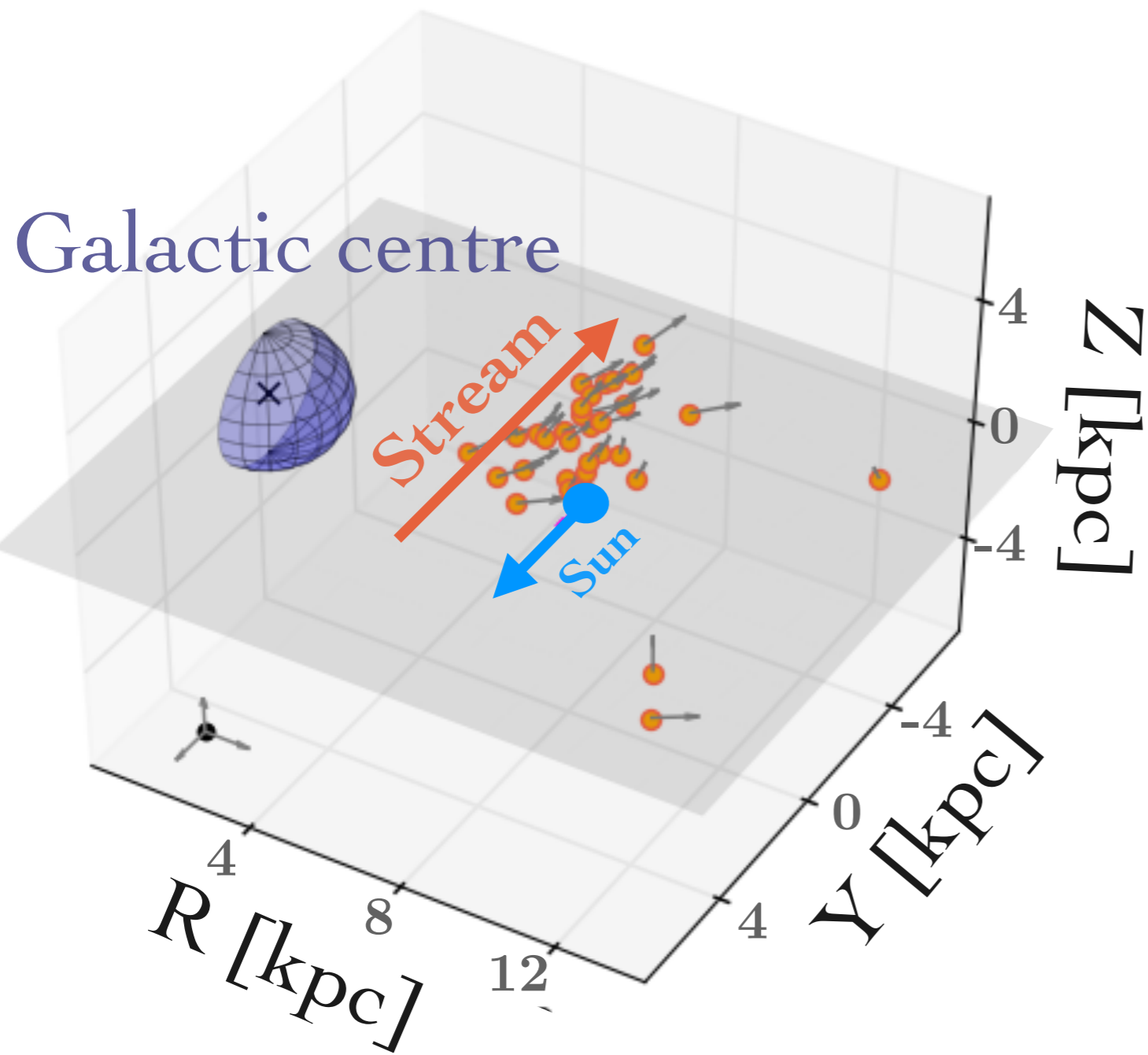


## Vertical

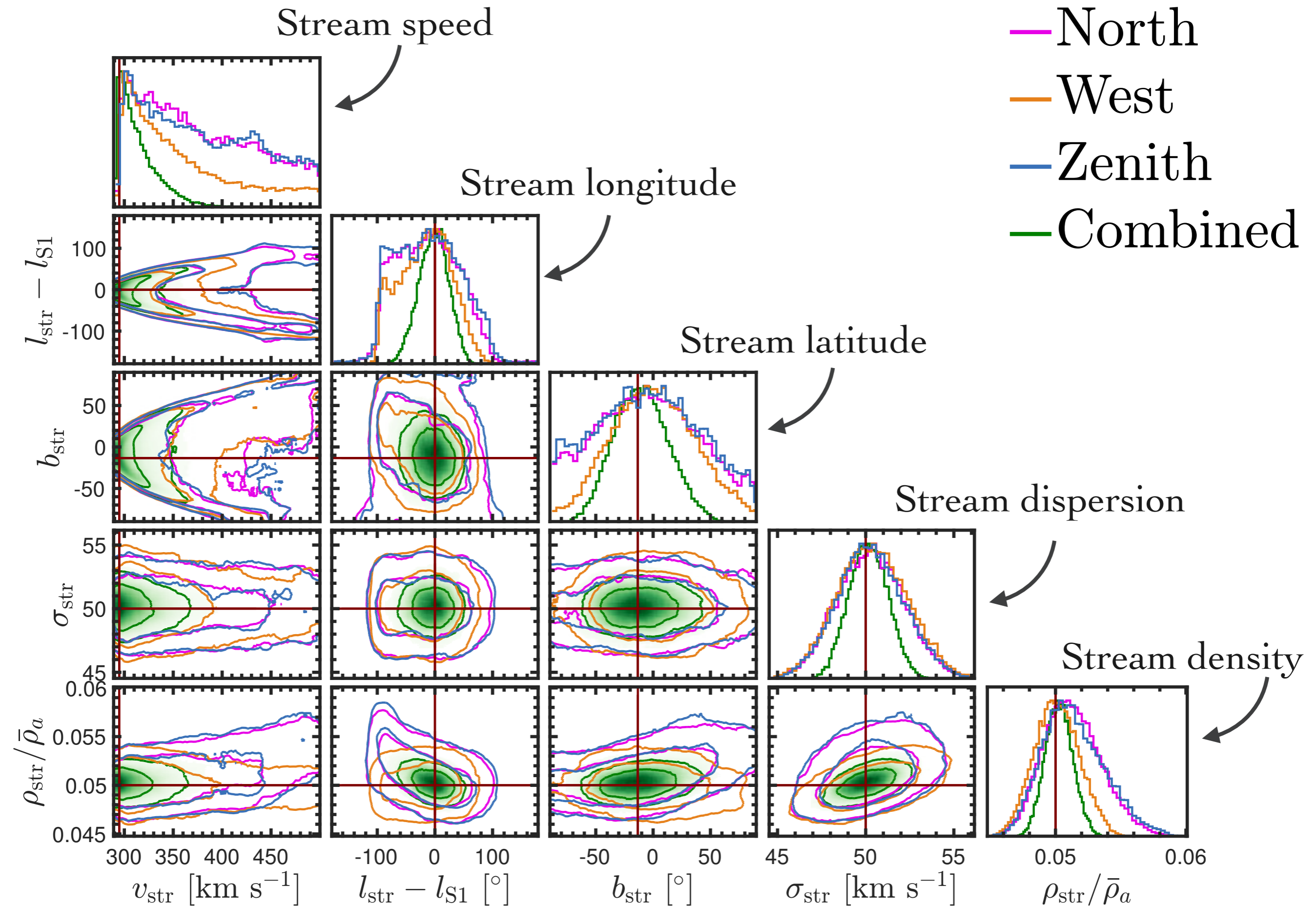


# The “S1 stream”

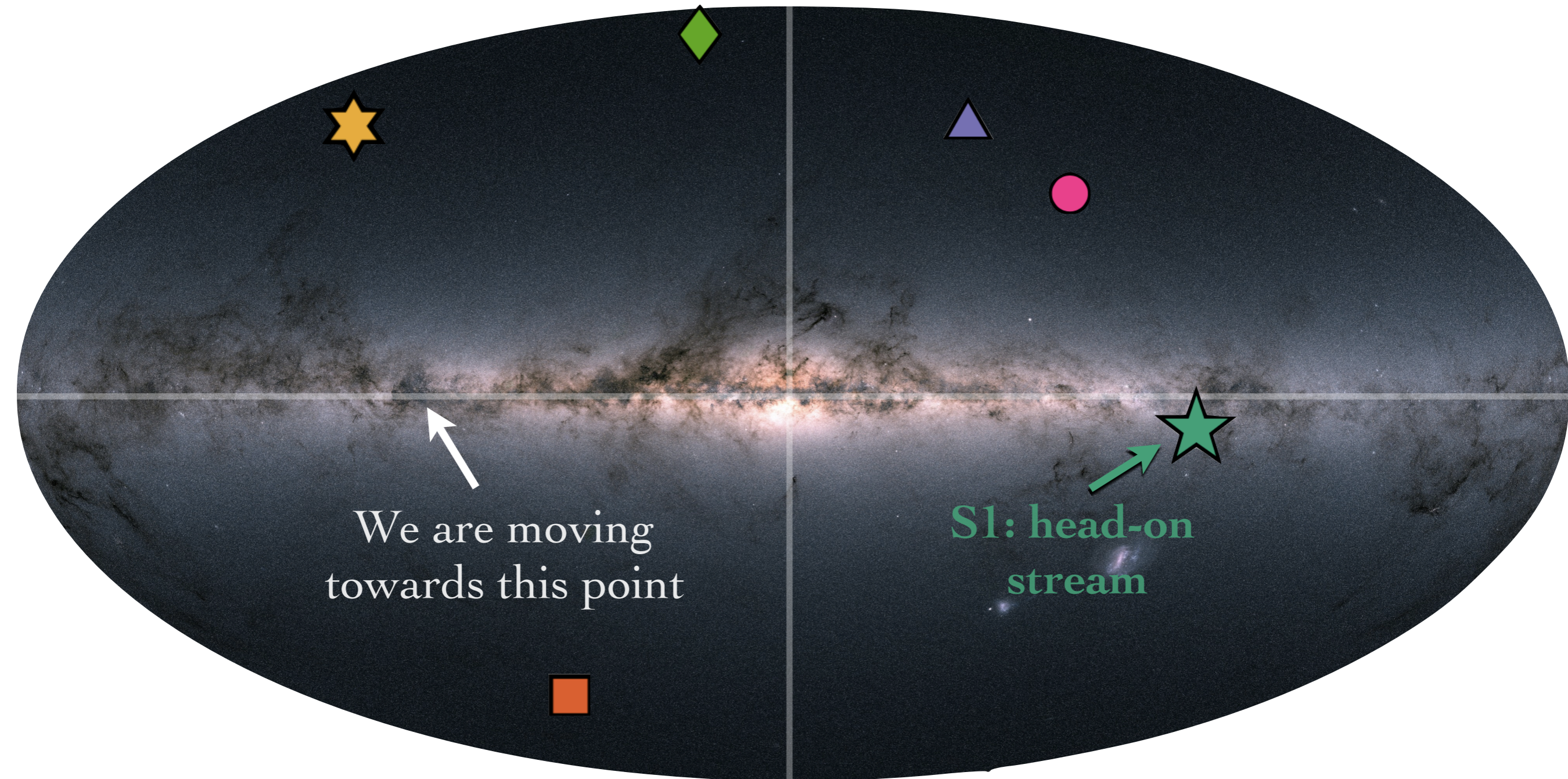
Stellar stream discovered in *Gaia* intersecting our Galactic position  
Myeong+[1712.04071], Myeong+[1804.07050], Evans, McCabe, O’Hare [in prep]



Signal with 5% S1 stream

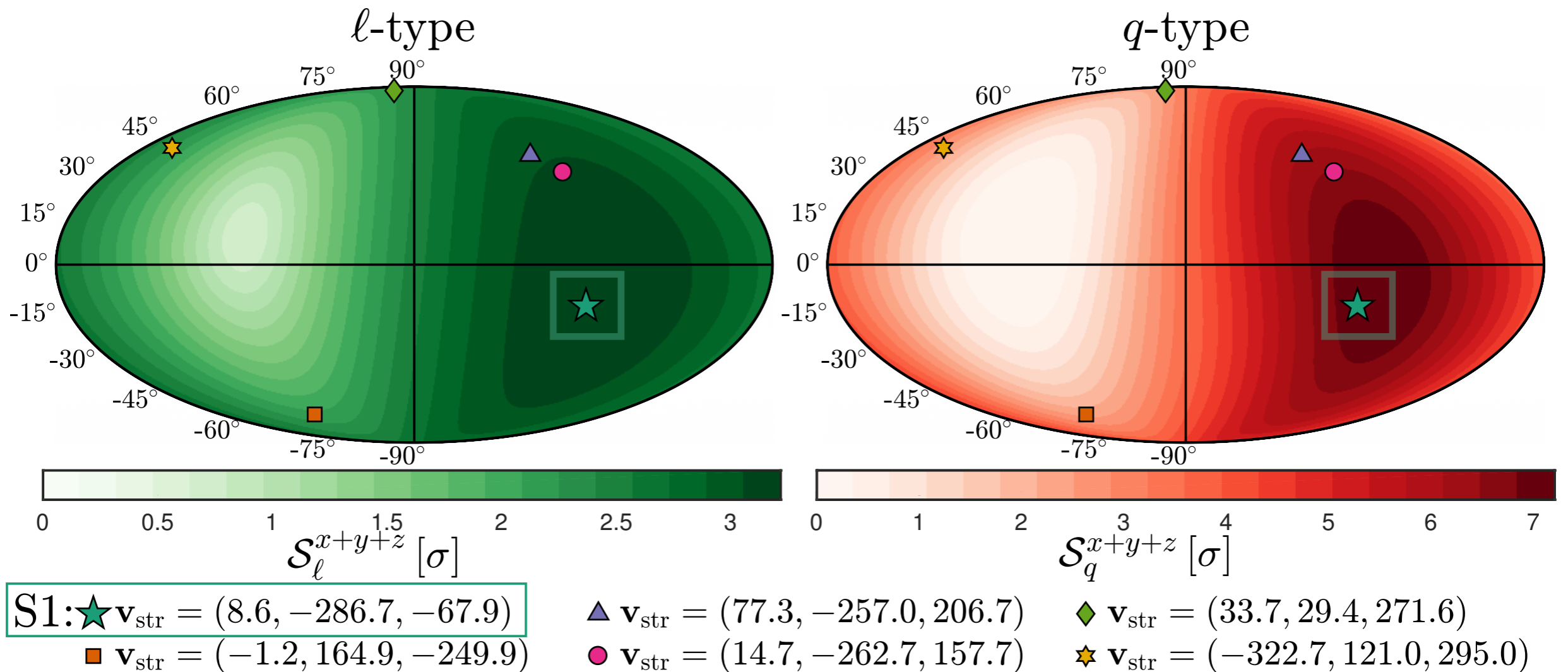


# Stream candidates



Sky map from *Gaia*

# Measuring general streams



**Linear experiments** - Streams measured consistently well across sky

**Quadratic experiments** - Can only detect head-on streams but with greater significance

# A directional axion experiment?

- Is it possible in theory?
  - **Yes:** Axion phase differences across large experiments + the rotation of the Earth gives you an  $O(1)$  directional effect
- Is it possible in practice?
  - Well, it's not *impossible* using a long cavity or dielectric disks
- Is it worth it?
  - **Maybe in the future... But,** this is how you maximise sensitivity to  $f(\mathbf{v})$  in 3d. You can measure the Solar velocity, anisotropy of the halo, nearby streams, or minicluster debris +potentially more...



# Miniclusters

Post-inflation scenario axion:

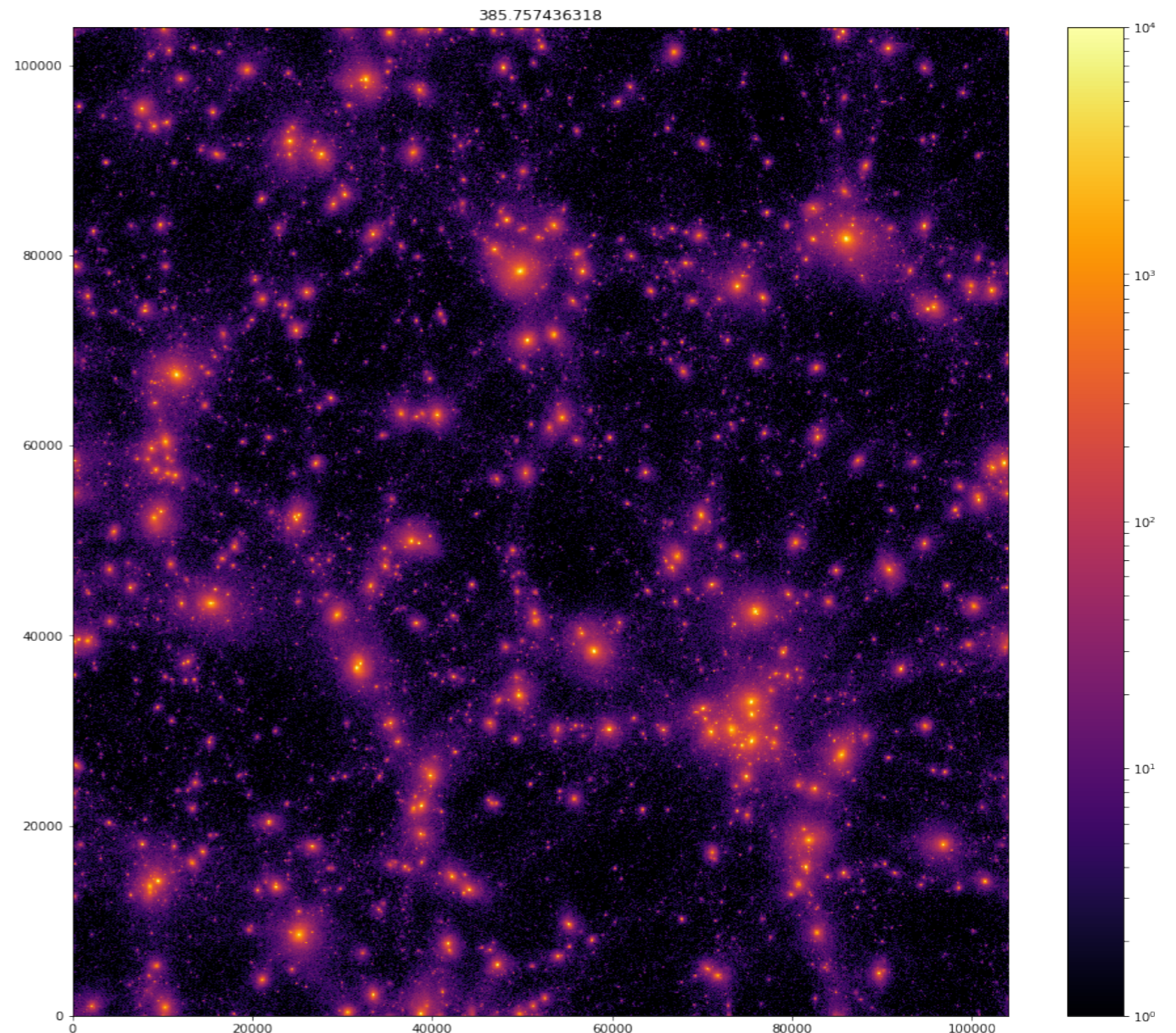
→ Collapsed over densities in axion field that decouple from Hubble flow around after QCD

Javier Redondo

$$\rho_{\text{mc}} \sim 10^6 \text{ GeV cm}^{-3}$$

$$R_{\text{mc}} \sim 10^7 \text{ km} \sim 0.2 \text{ AU}$$

$$M_{\text{mc}} \sim 10^{-12} M_{\odot}$$

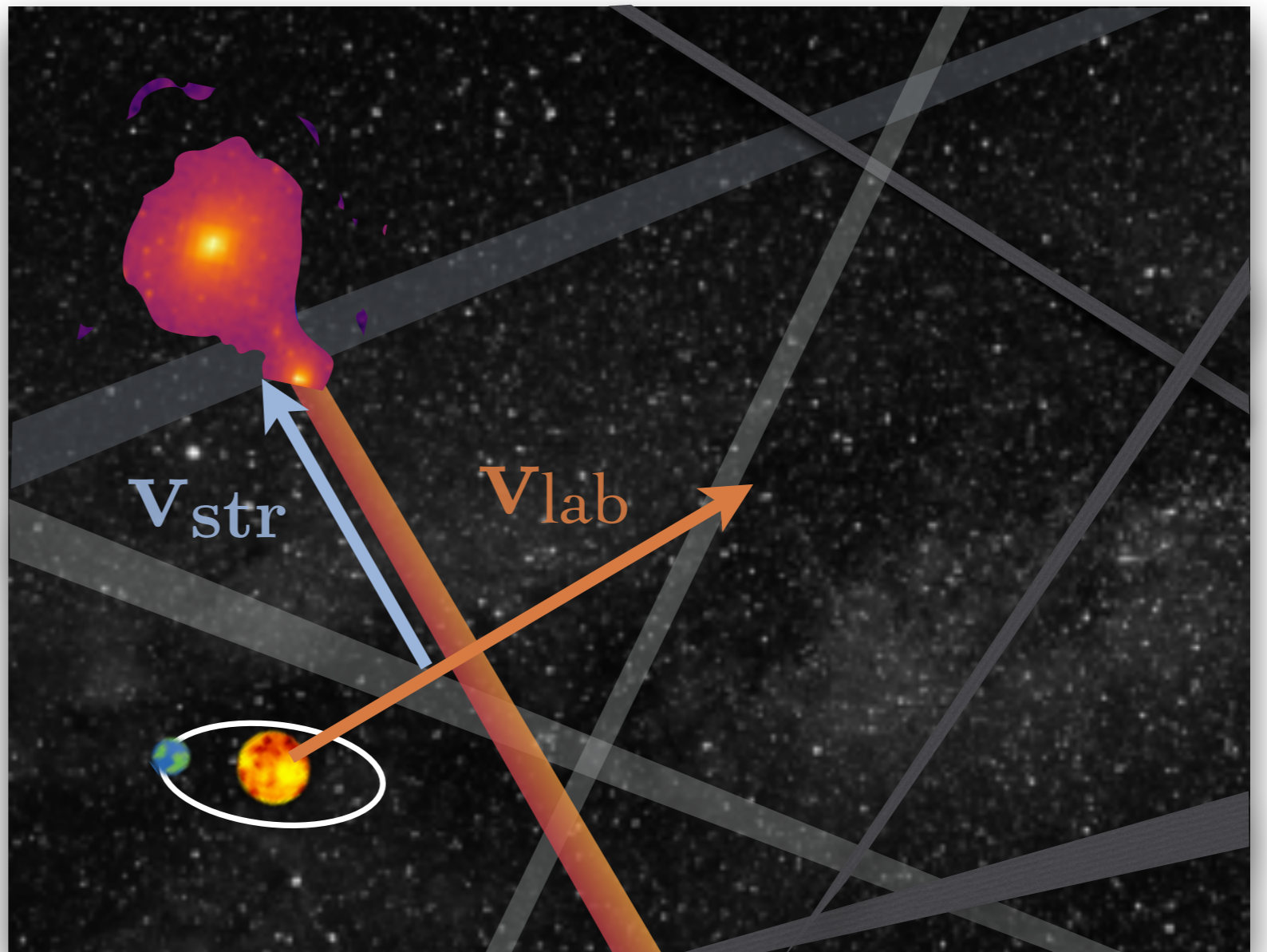


# “Ministreams”

- Miniclusters tidally disrupted by stars
- Temporary enhancements in signal:

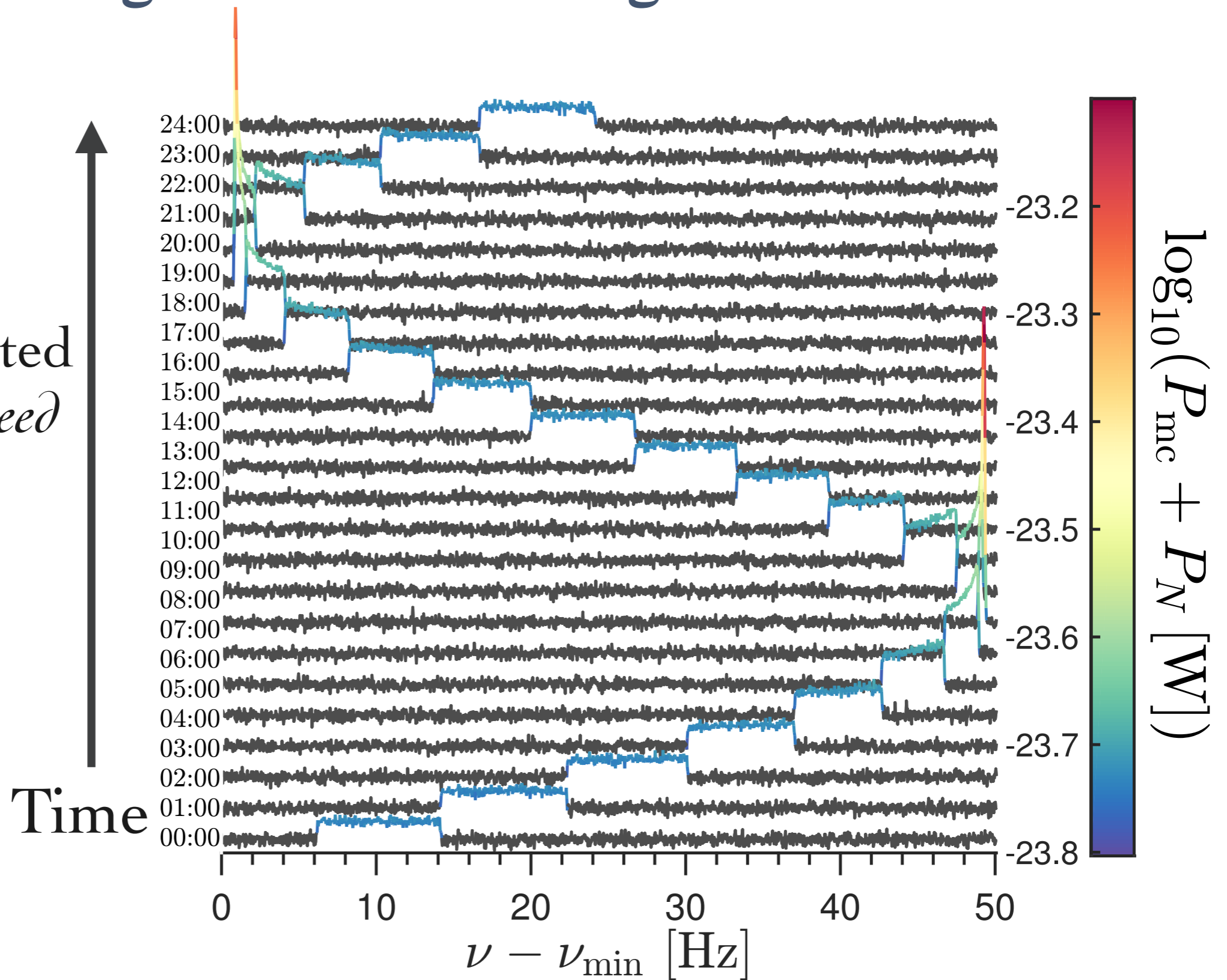
$$\tau = \frac{2R_{\text{mc}}}{v_{\text{lab}} \sin \vartheta_{\text{str}}}$$

$\sim \mathcal{O}(\text{hours} - \text{days})$



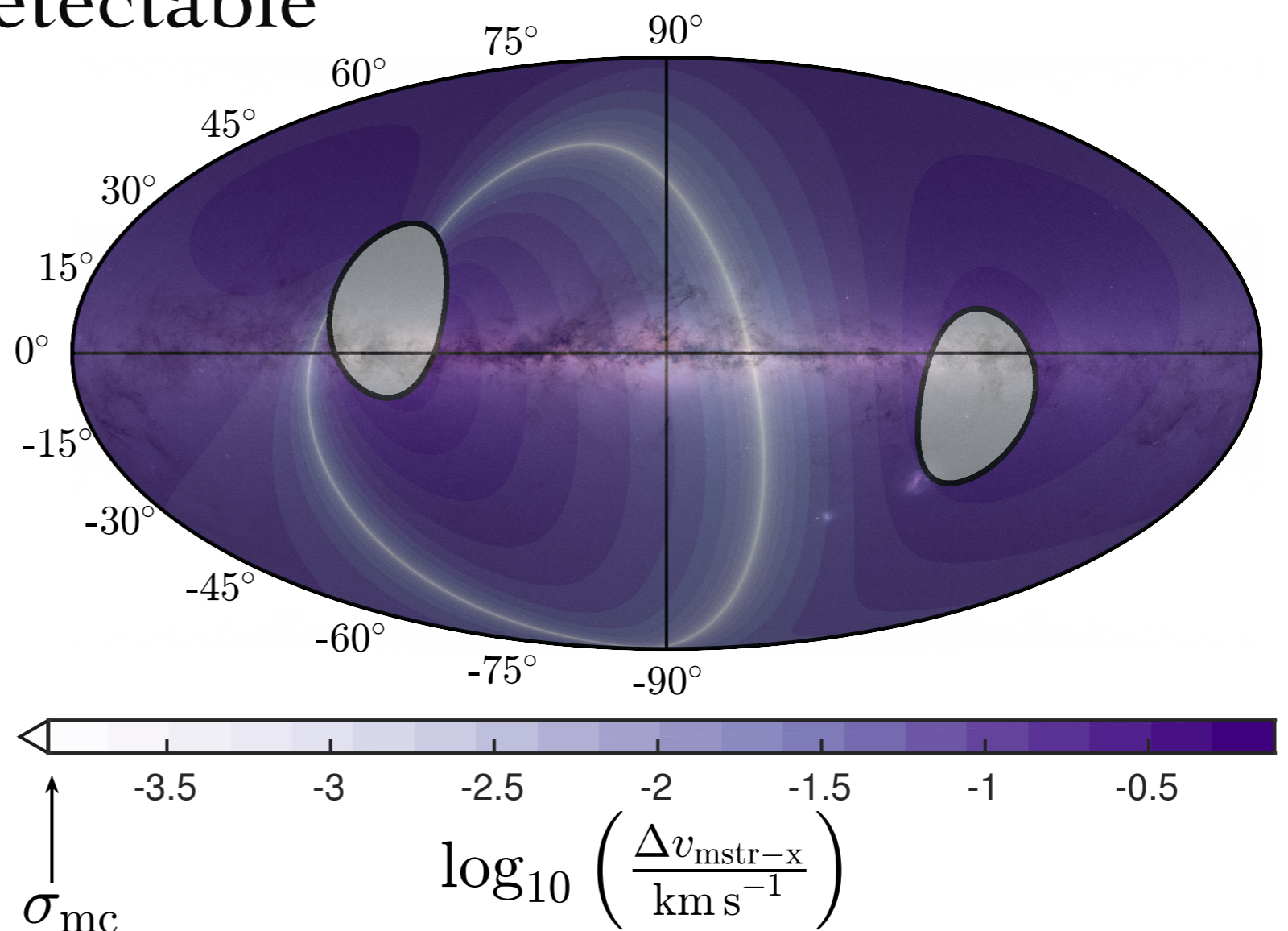
# Simulated signal from crossing of a ministream

Signal modulated  
by rotation *speed*  
of earth



# Minicluster streams

- Ministreams with directions in the light band would not give a sufficient daily modulation without directionality to be detectable



\*Band potentially wider if miniclusters are significantly heated during tidal disruption

# Phase of daily modulation from a stream

