



THE UNIVERSITY OF
SYDNEY



Axions as dark matter

Ciaran O'Hare
U. Sydney

Part 1: Axion theory & searches

Part 2: Axion dark matter simulations

CAJO & Vitagliano [[2010.03889](#)]
Caputo, Millar, CAJO, Vitagliano [[2105.04565](#)]
CAJO, Pierobon, Redondo, Wong [in prep.]
cajohare.github.io/AxionLimits/

CP violation and the neutron electric dipole moment

CP violation and the neutron electric dipole moment

Theory: Vacuum structure of QCD (instantons) generates a term

$$\mathcal{L}_{\text{QCD}} = \dots - \frac{\alpha_s}{8\pi} \theta_{\text{QCD}} G_{\mu\nu a} \tilde{G}_a^{\mu\nu}$$

Some angle, not fixed by theory,
so presumably $\mathcal{O}(1)$

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$$\bar{\theta} = \theta_{\text{QCD}} + \theta_q$$

Where it sets the electric dipole moment of the neutron

$$d_n = (2.4 \pm 1.0) \bar{\theta} \times 10^{-3} e \text{ fm}$$

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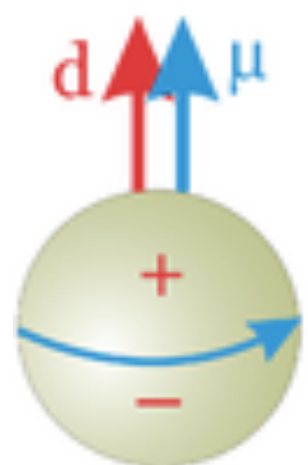
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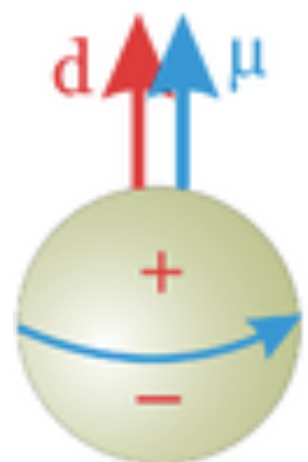
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Put some spin-polarised neutrons in E, B fields \longrightarrow Measure spin precession frequencies



$$\nu_{\pm} = 2|\mu_n B \pm d_n E|$$

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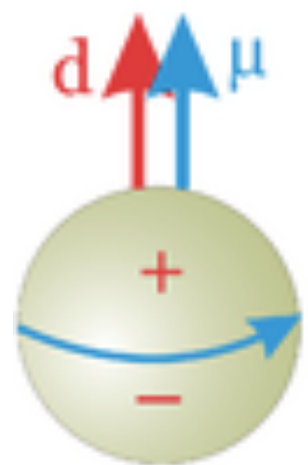
Where it sets the electric dipole moment of the neutron

$$d_n = (2.4 \pm 1.0) \bar{\theta} \times 10^{-3} e \text{ fm}$$

Put some spin-polarised neutrons in E, B fields

Measure spin precession frequencies

Calculate neutron EDM



$$\nu_{\pm} = 2|\mu_n B \pm d_n E|$$

d_n

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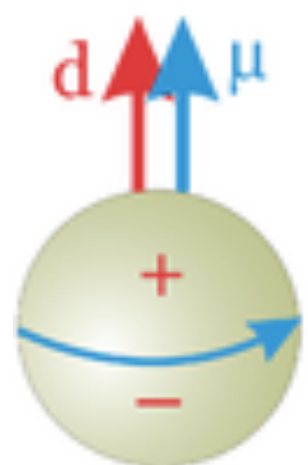
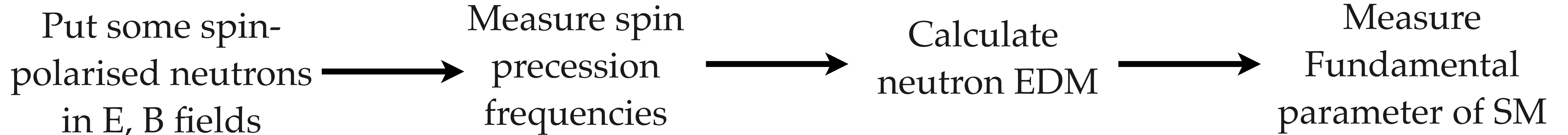
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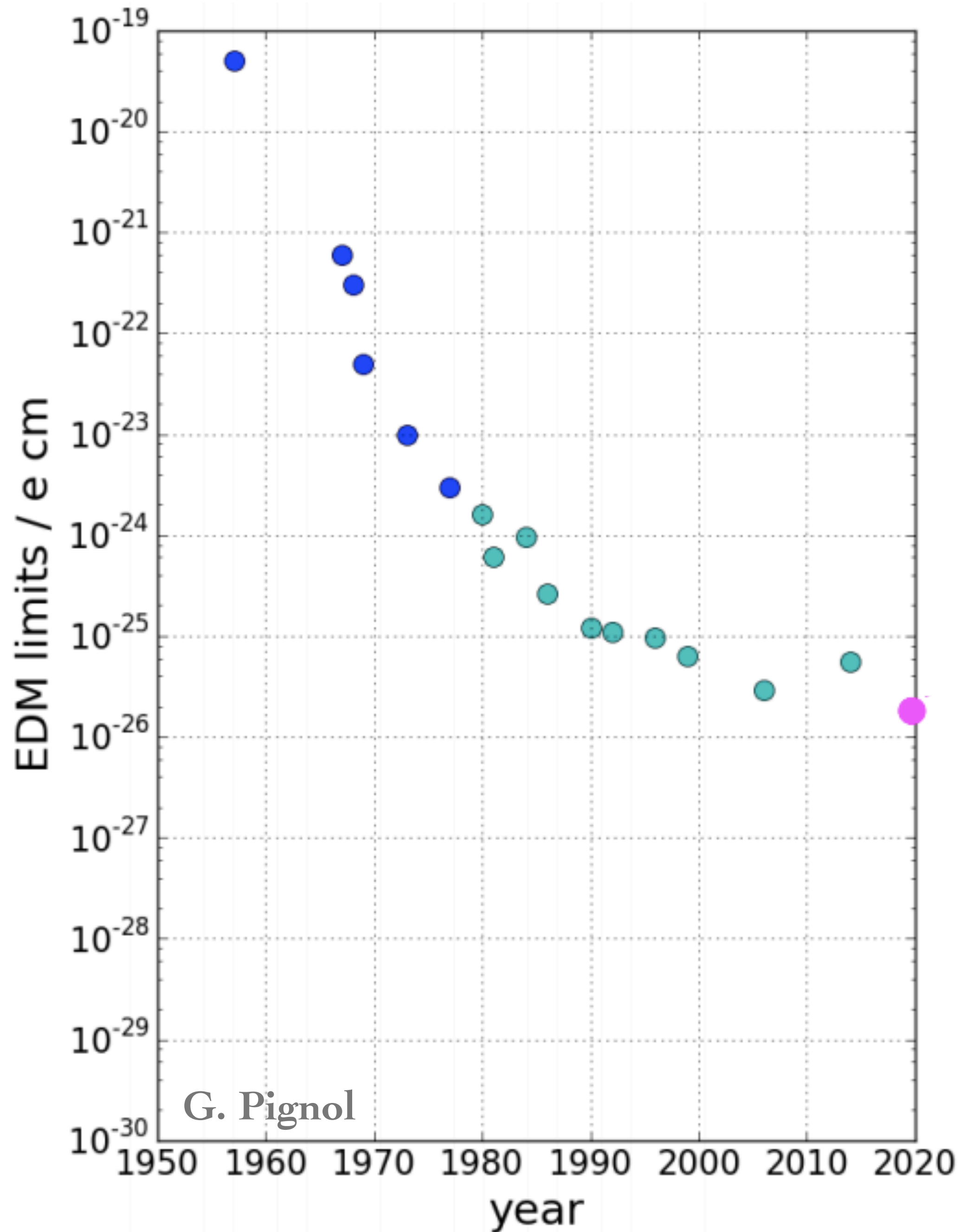
θ_{QCD}

What do they see?

Recent measurement [2001.11966]

$$|d_n| < 1.8 \times 10^{-26} \text{ e cm} \quad (90\% \text{ CL})$$

$$\Rightarrow \theta \lesssim 10^{-10}$$



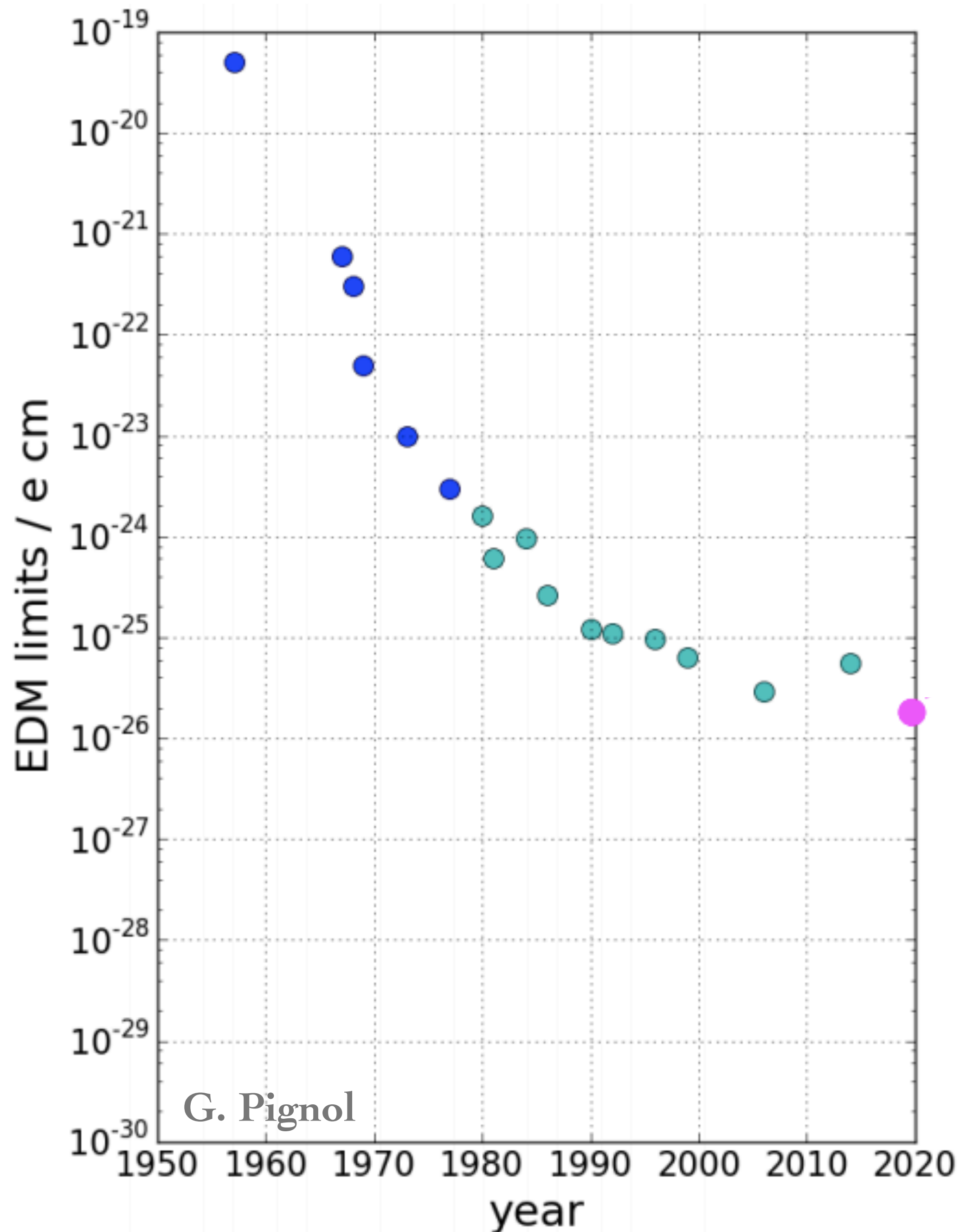
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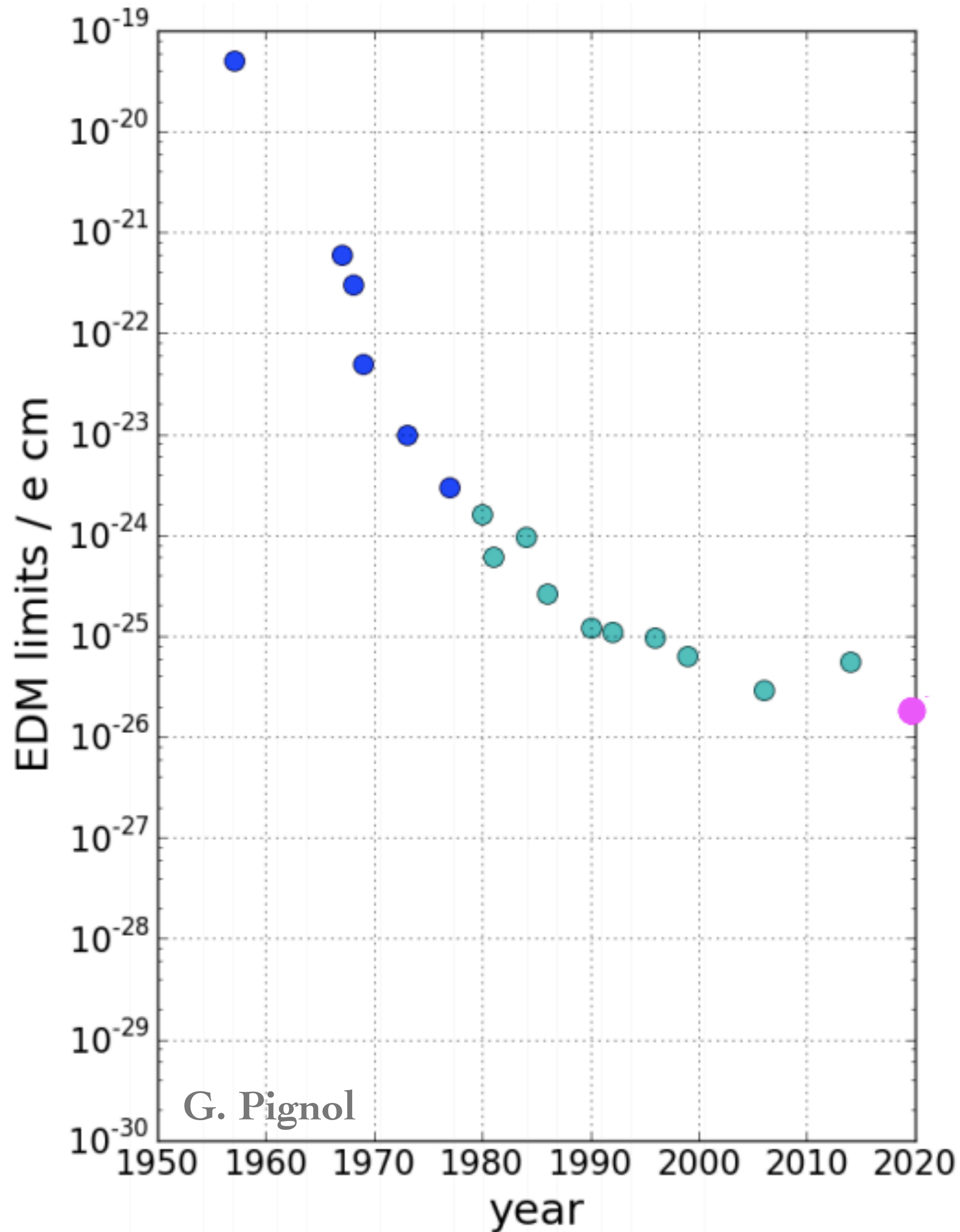
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Conclusion: The strong interaction seems to be conserving CP when it generically shouldn't
→ **The strong CP problem**





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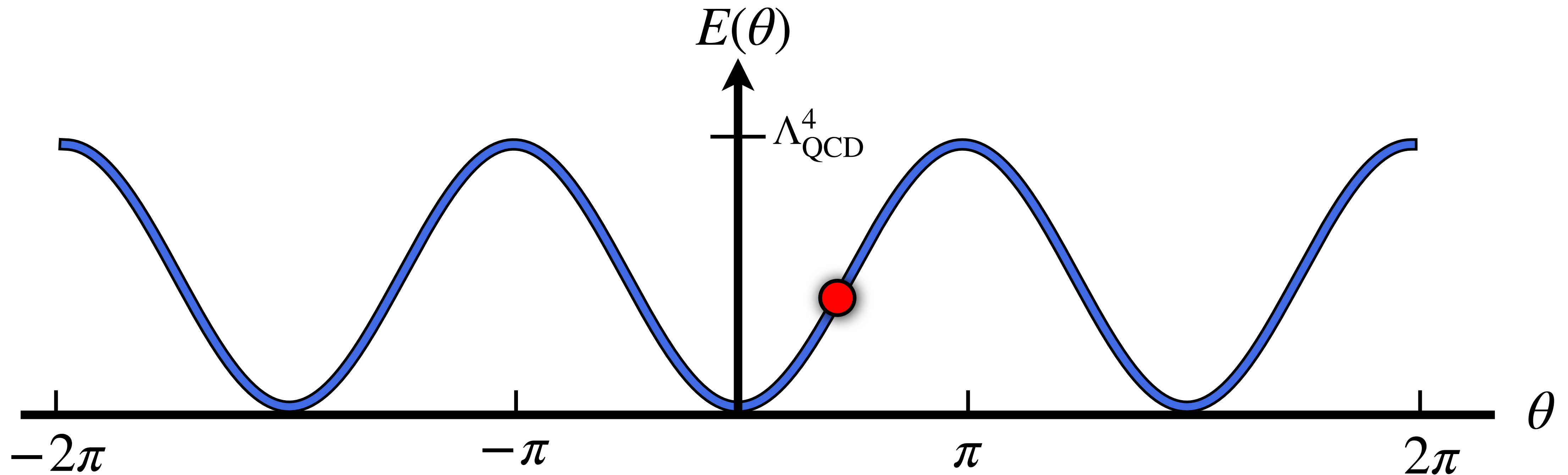
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The real problem: why are two completely unrelated numbers cancelling each other < ppb?

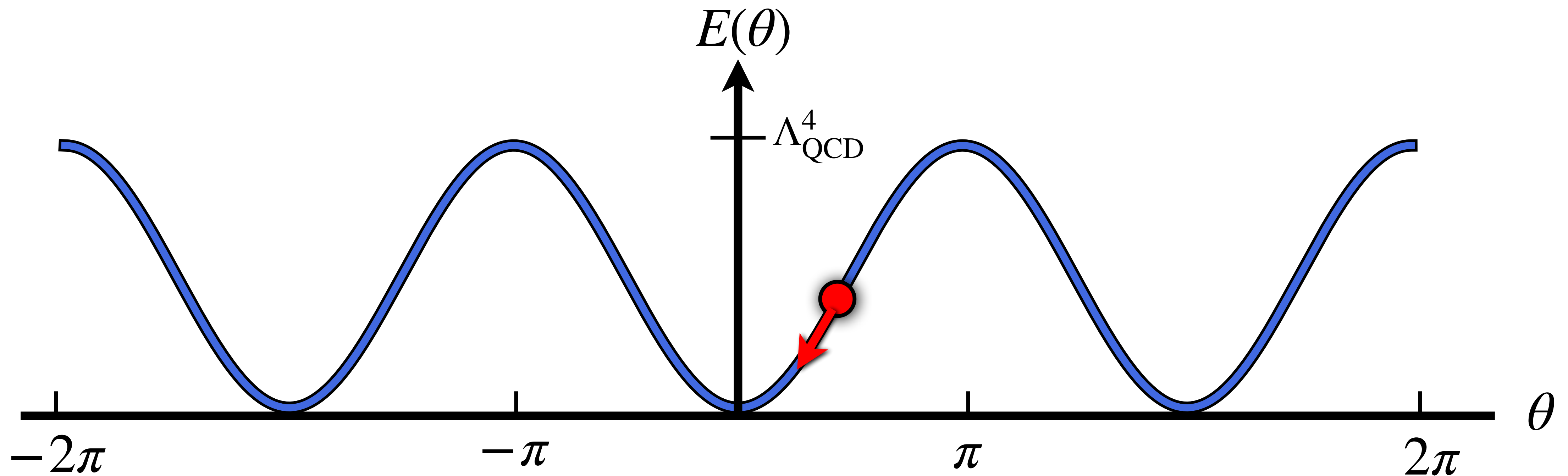
The solution, a la Peccei-Quinn

QCD vacuum energy density already has a minimum at $\theta = 0$ (Vafa-Witten theorem). However θ is just a parameter, there is no mechanism to cause it to want to minimise energy



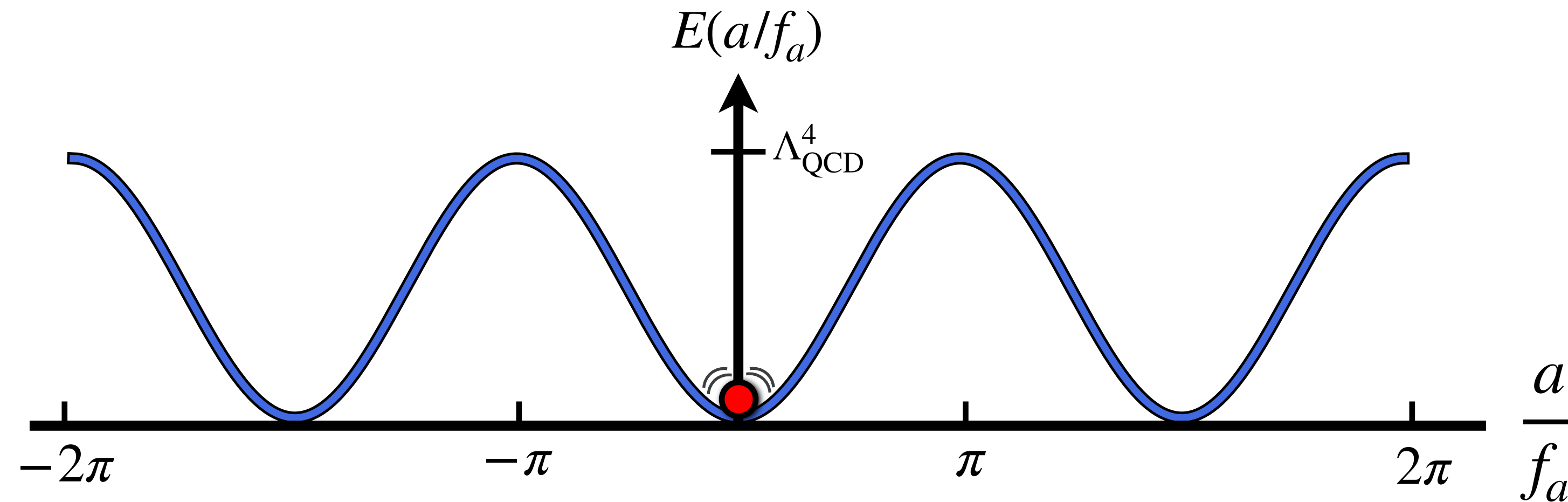
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PQ mechanism: what if there was?

The axion



- Introduce field, a , that couples to gluons $\propto (a/f_a) G\tilde{G}$. It will have a shift symmetry that can be used to cancel off any unwanted CP violation while VW theorem ensures $\langle a \rangle = 0$
- QCD vacuum implies a potential for the axion and thus a small mass

$$V(a) \approx \Lambda_{\text{QCD}}^4 \left[1 - \cos \left(\bar{\theta} + \frac{a}{f_a} \right) \right] \longrightarrow m_a \simeq \frac{\Lambda_{\text{QCD}}^2}{f_a} \simeq 6 \text{ meV} \left(\frac{10^9 \text{ GeV}}{f_a} \right)$$

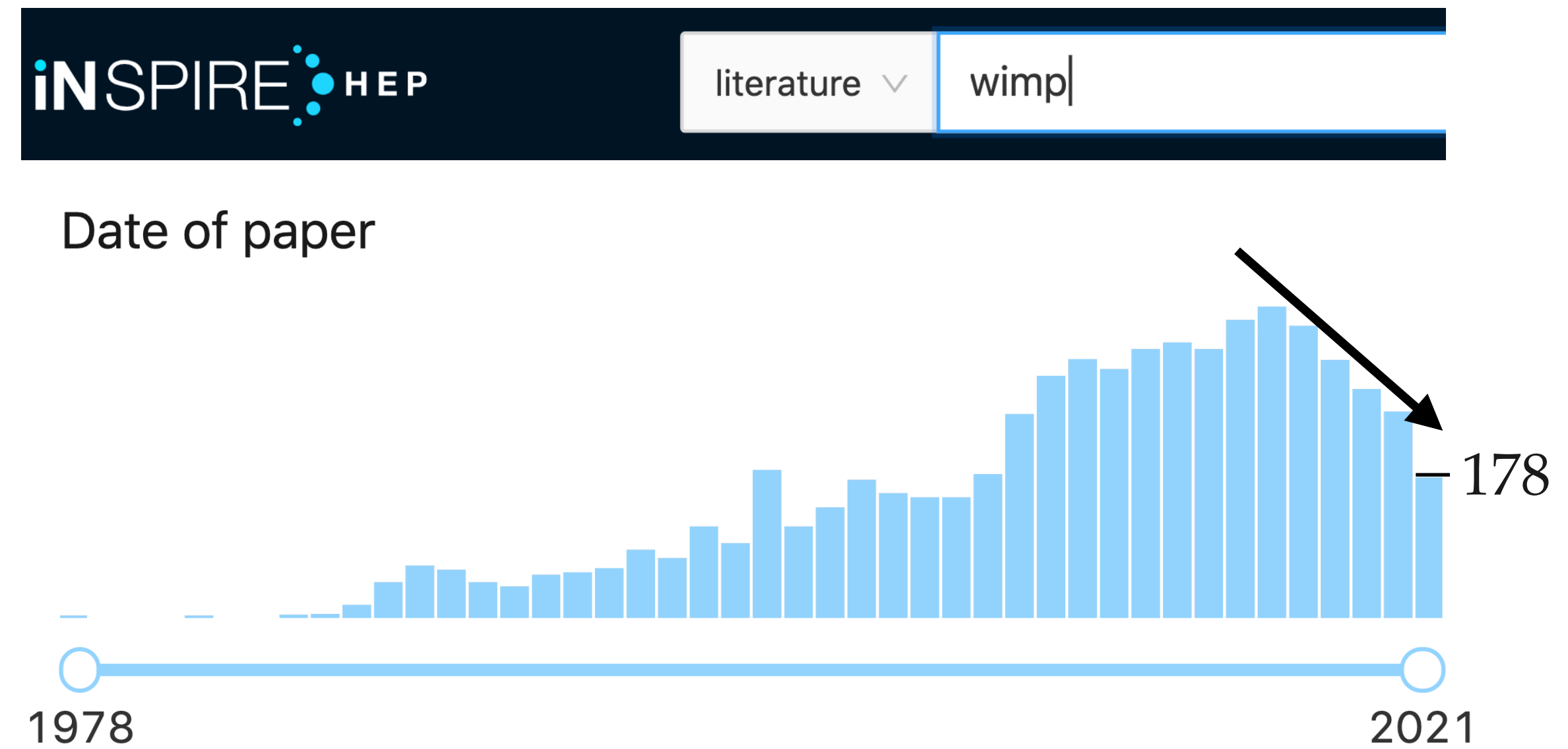
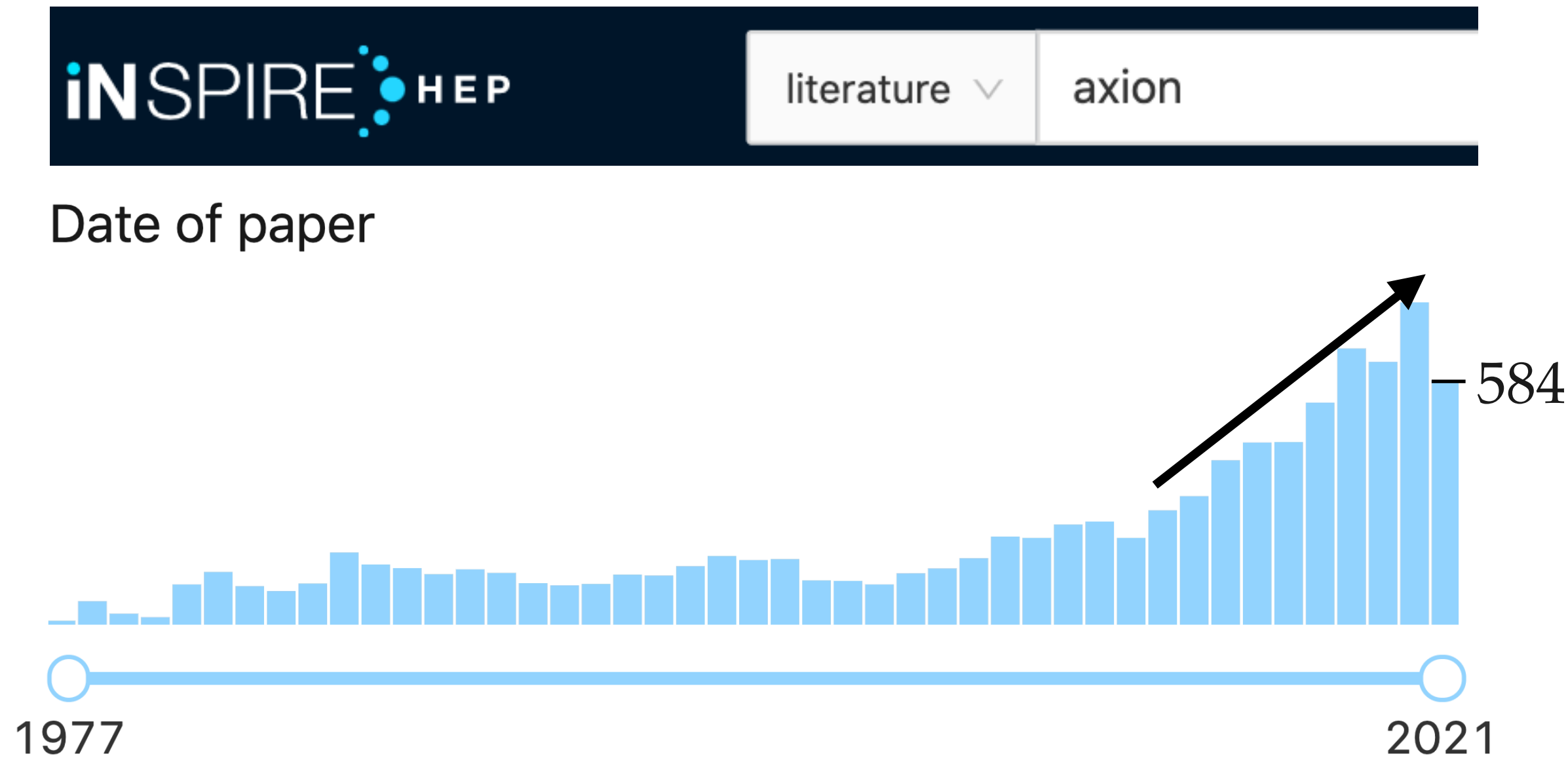
The axion effective theory

Introduce axion as the pseudo-Goldstone boson of a new global $U(1)$, spontaneously broken at scale f_a . After some extra work, it can also couple to the photon and fermions

$$\mathcal{L} = \frac{1}{2} (\partial_\mu a) (\partial^\mu a) - \frac{1}{2} m_a^2 a^2 - \frac{g_{a\gamma}}{4} a F_{\mu\nu} \tilde{F}^{\mu\nu} + \partial_\mu a \sum_\psi \frac{g_{a\psi}}{2m_\psi} (\bar{\psi} \gamma^\mu \gamma^5 \psi)$$

Importantly, all couplings suppressed by $g \sim f_a^{-1}$. So set symmetry breaking scale as high as you like to evade observational constraints
→ ideal candidate for **dark matter**

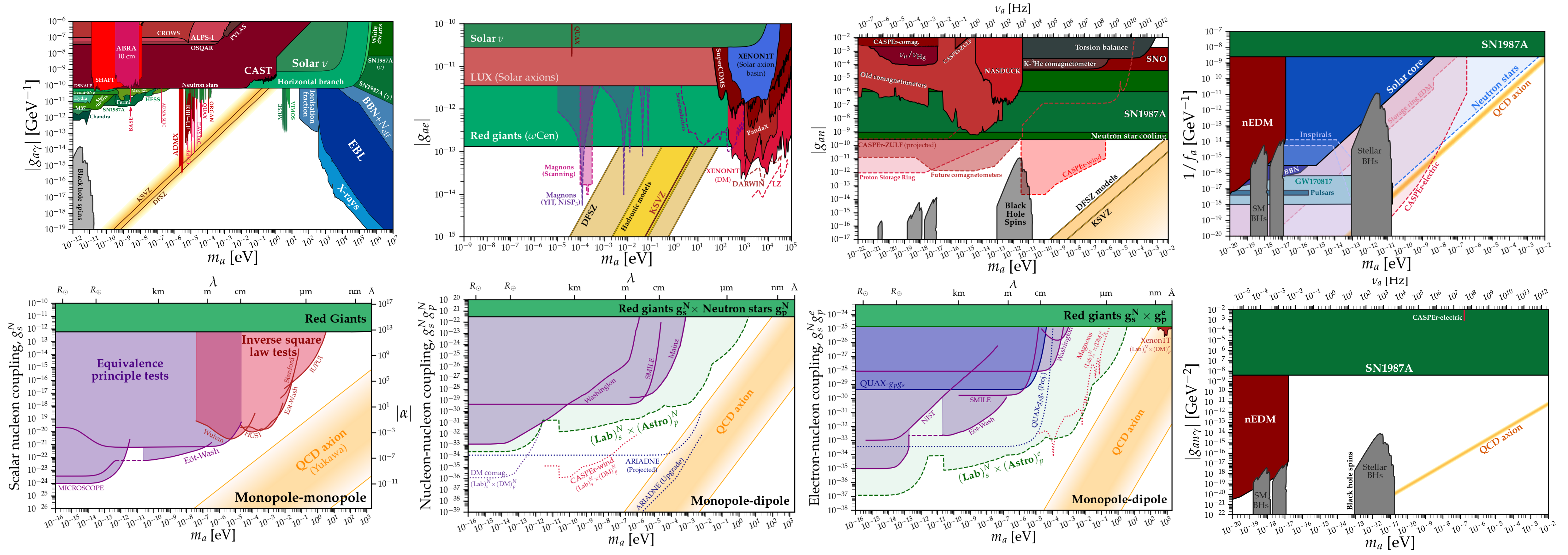
The axion is fashionable



- Solves outstanding problem of the SM
- Cosmologically relevant as (all or some of) DM
- Many laboratory tests possible, almost totally falsifiable
- Testable in astrophysical environments as well

Lots of activity, but potentially many years away from a discovery

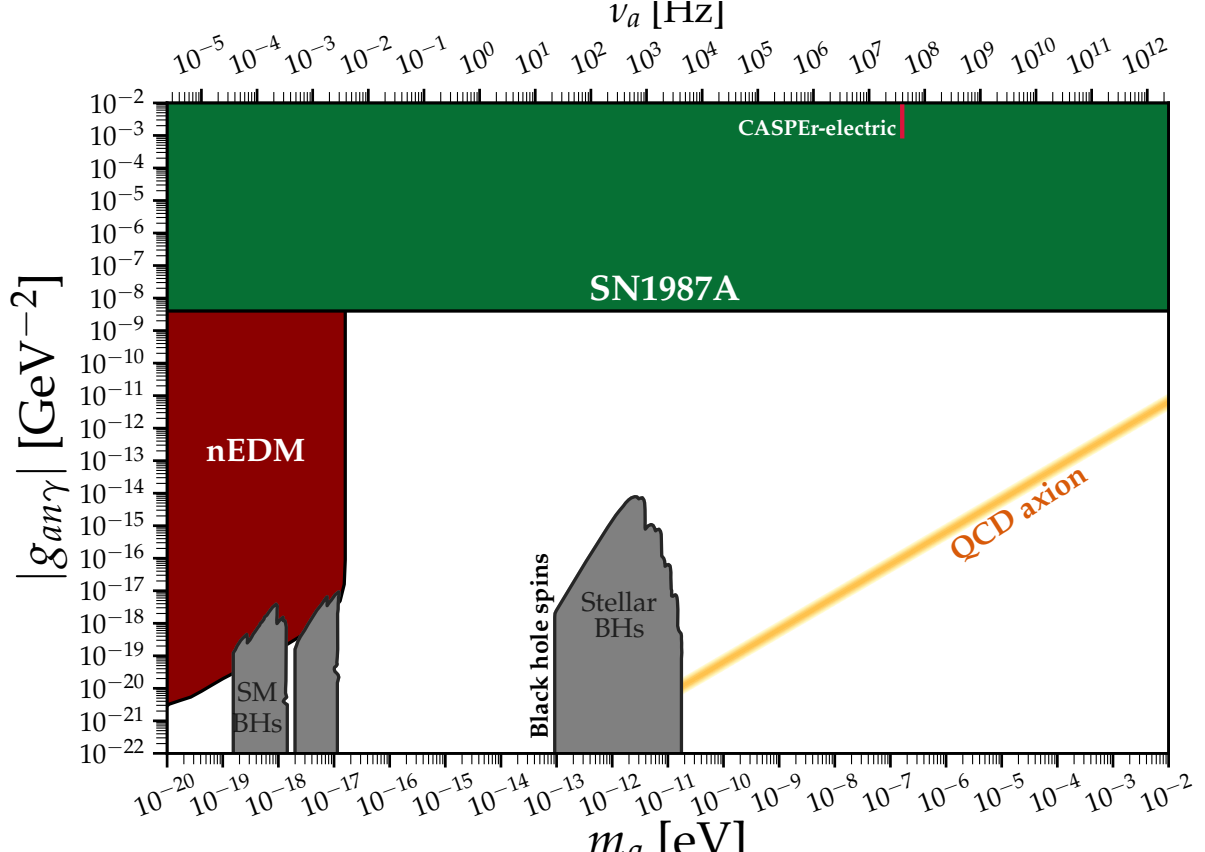
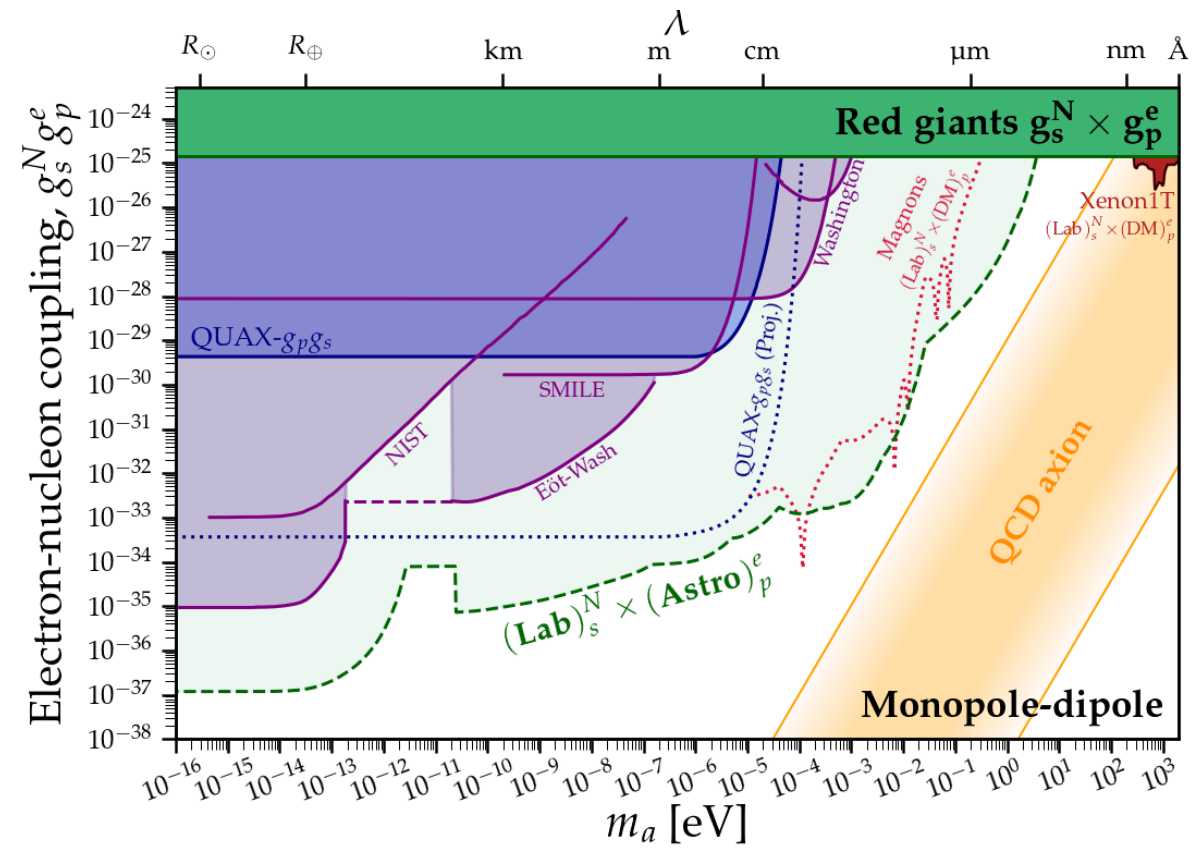
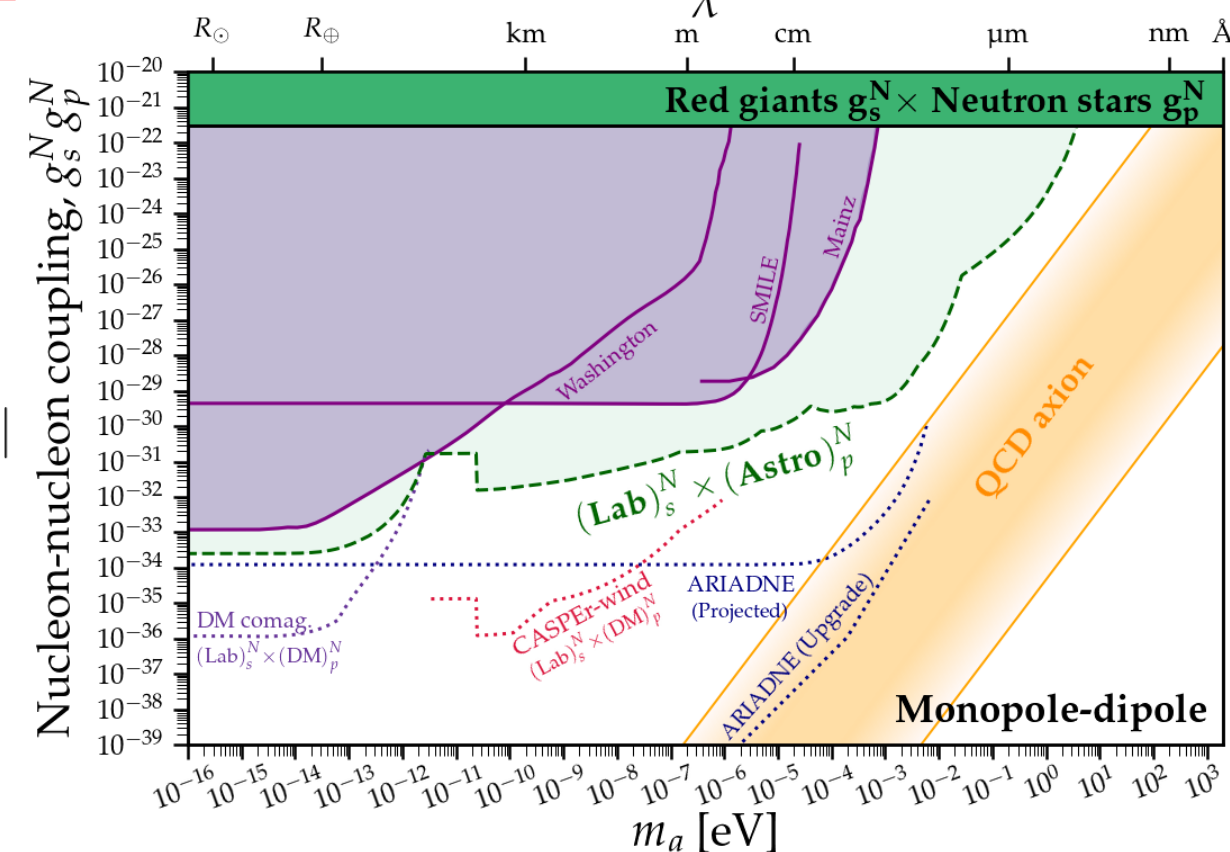
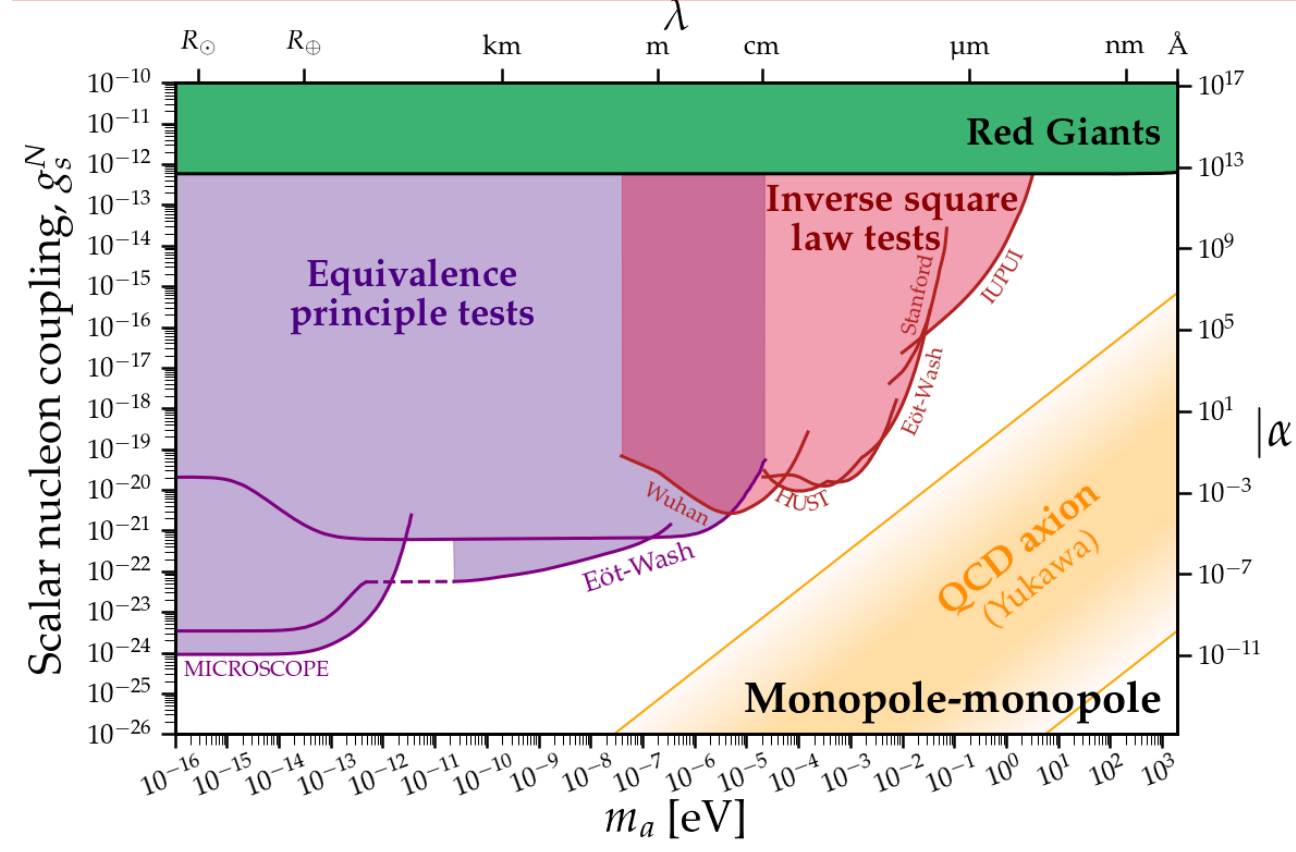
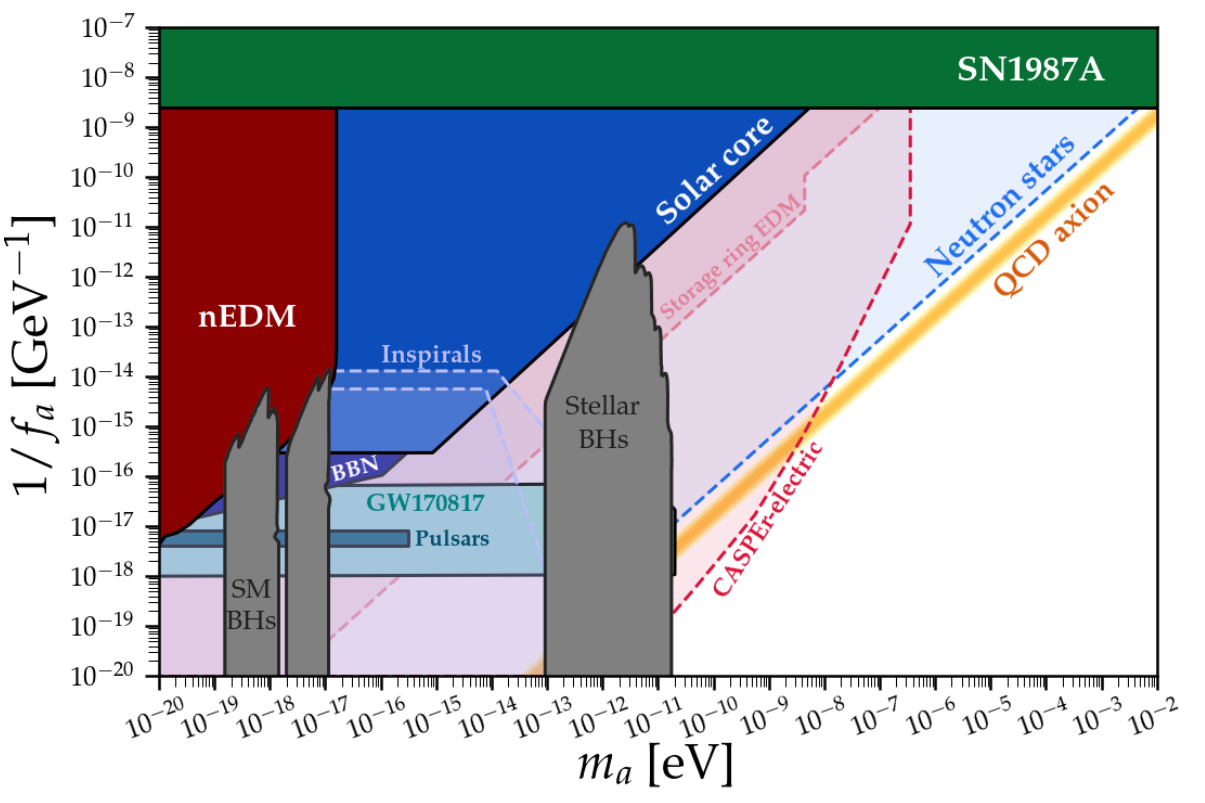
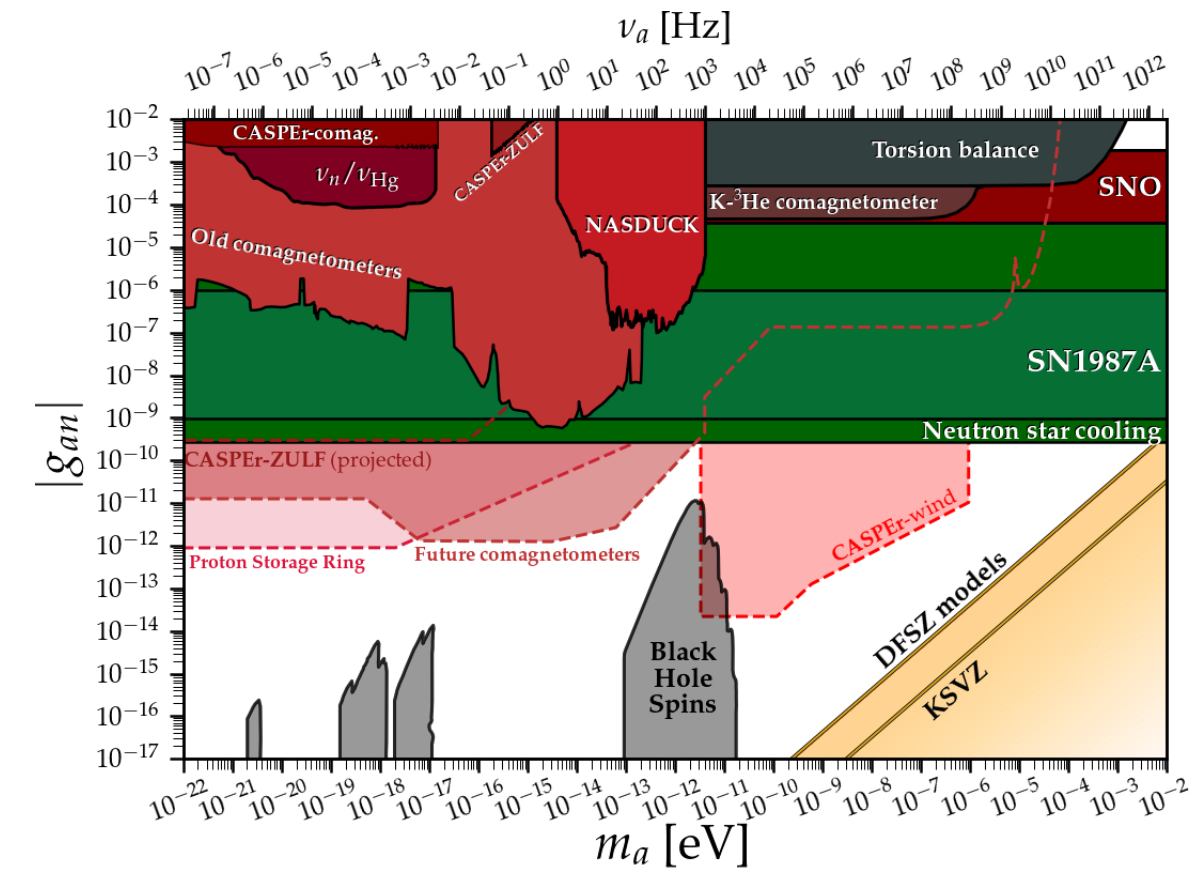
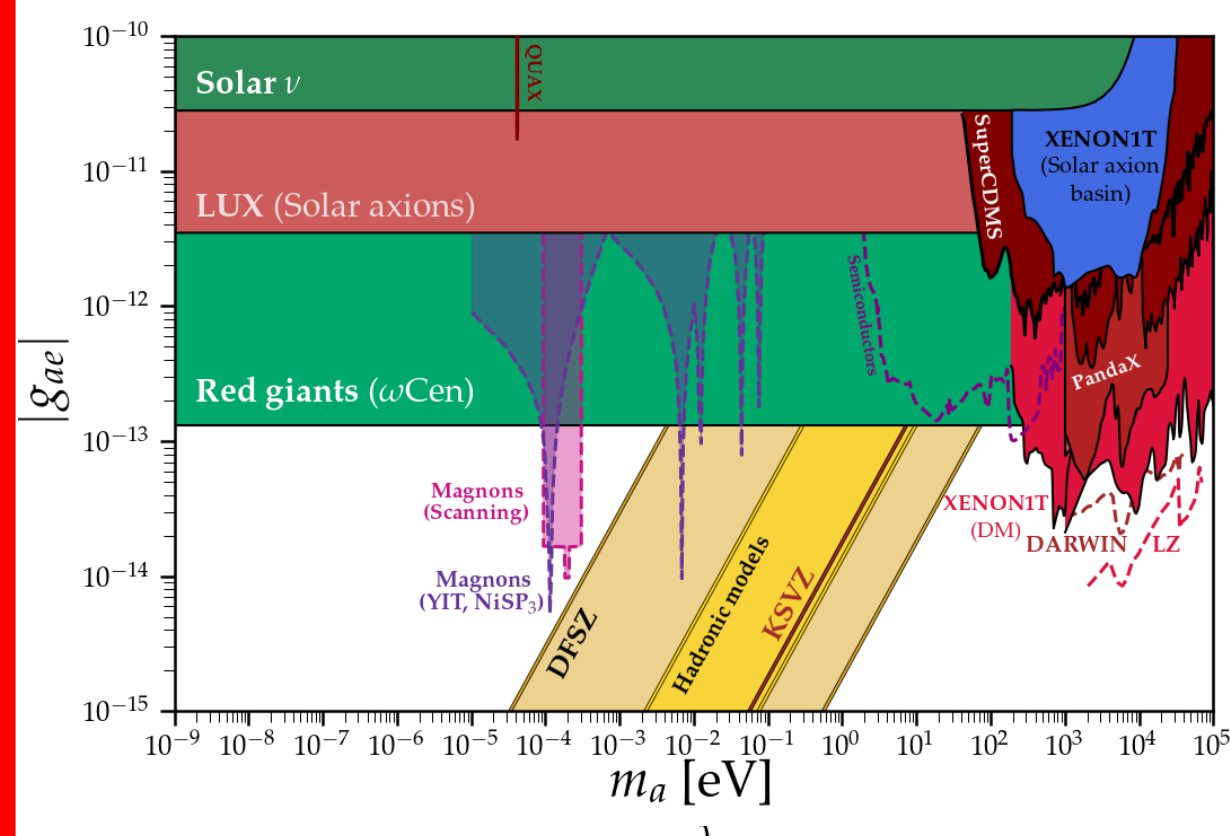
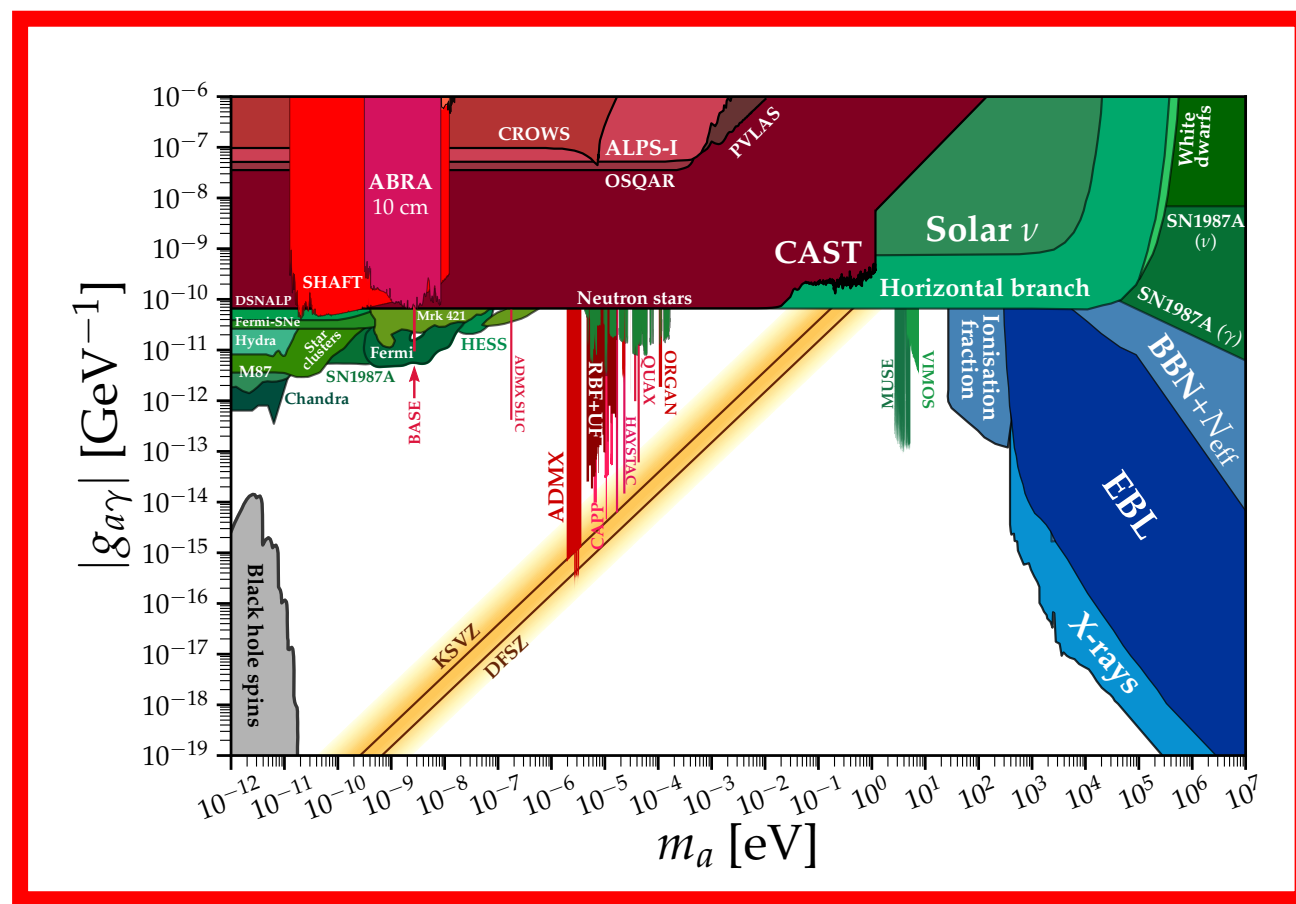
This talk: Can we do anything theoretically to accelerate us towards one?



For more, see cajohare.github.io/AxionLimits/ → Now hosts results from >200 publications!

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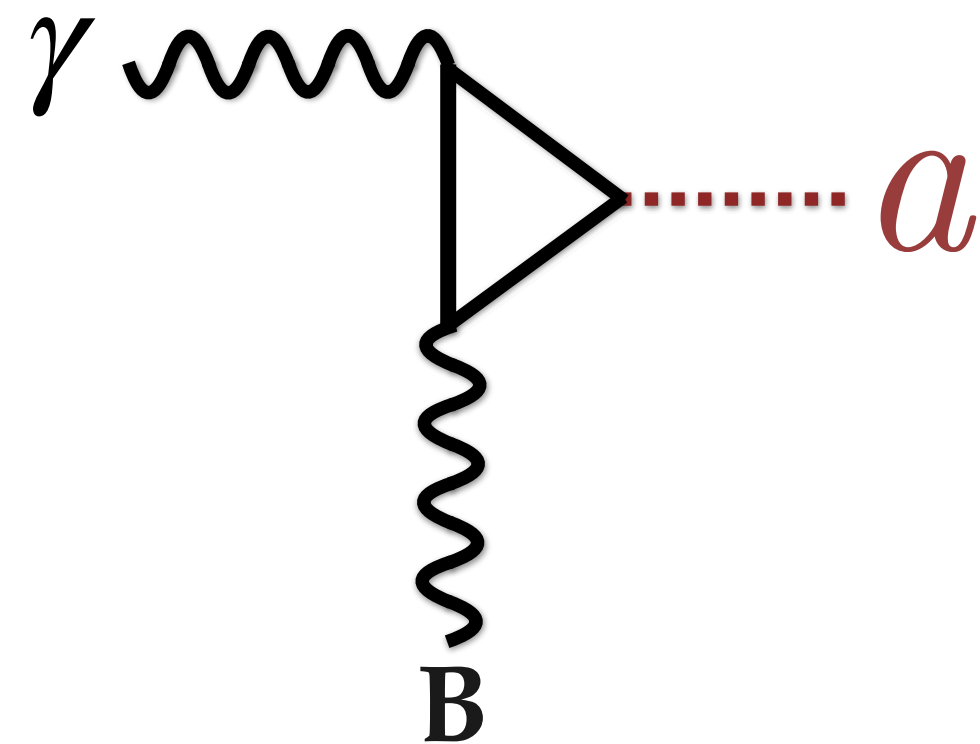
Coupling to the photon

$$\mathcal{L} = -\frac{1}{4}g_{a\gamma}a(\mathbf{x}, t)F_{\mu\nu}\tilde{F}^{\mu\nu} = g_{a\gamma}a(\mathbf{x}, t)\mathbf{E} \cdot \mathbf{B}$$

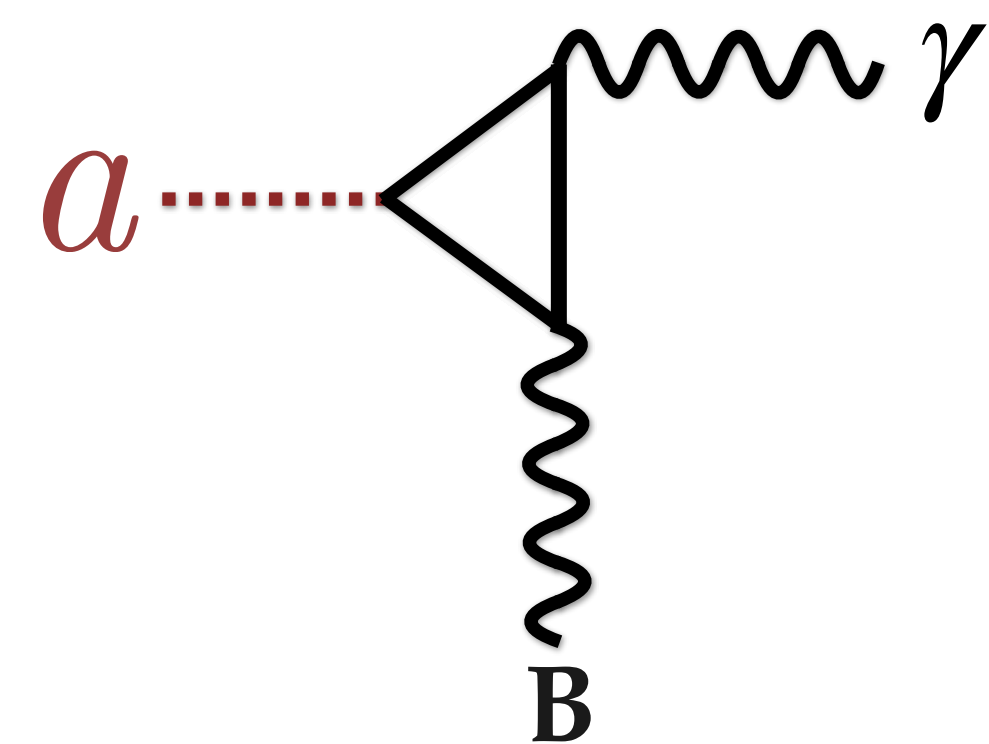
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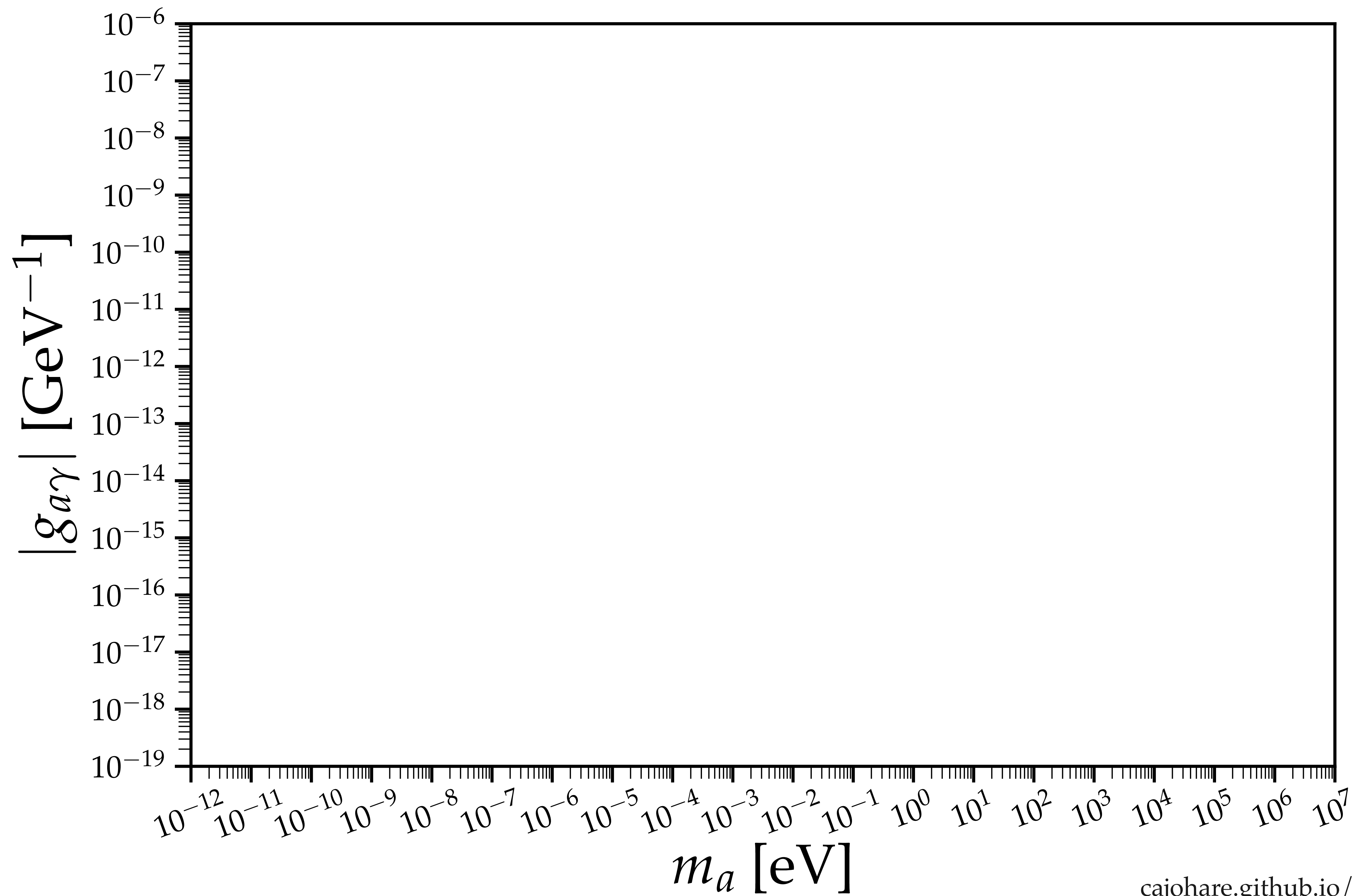
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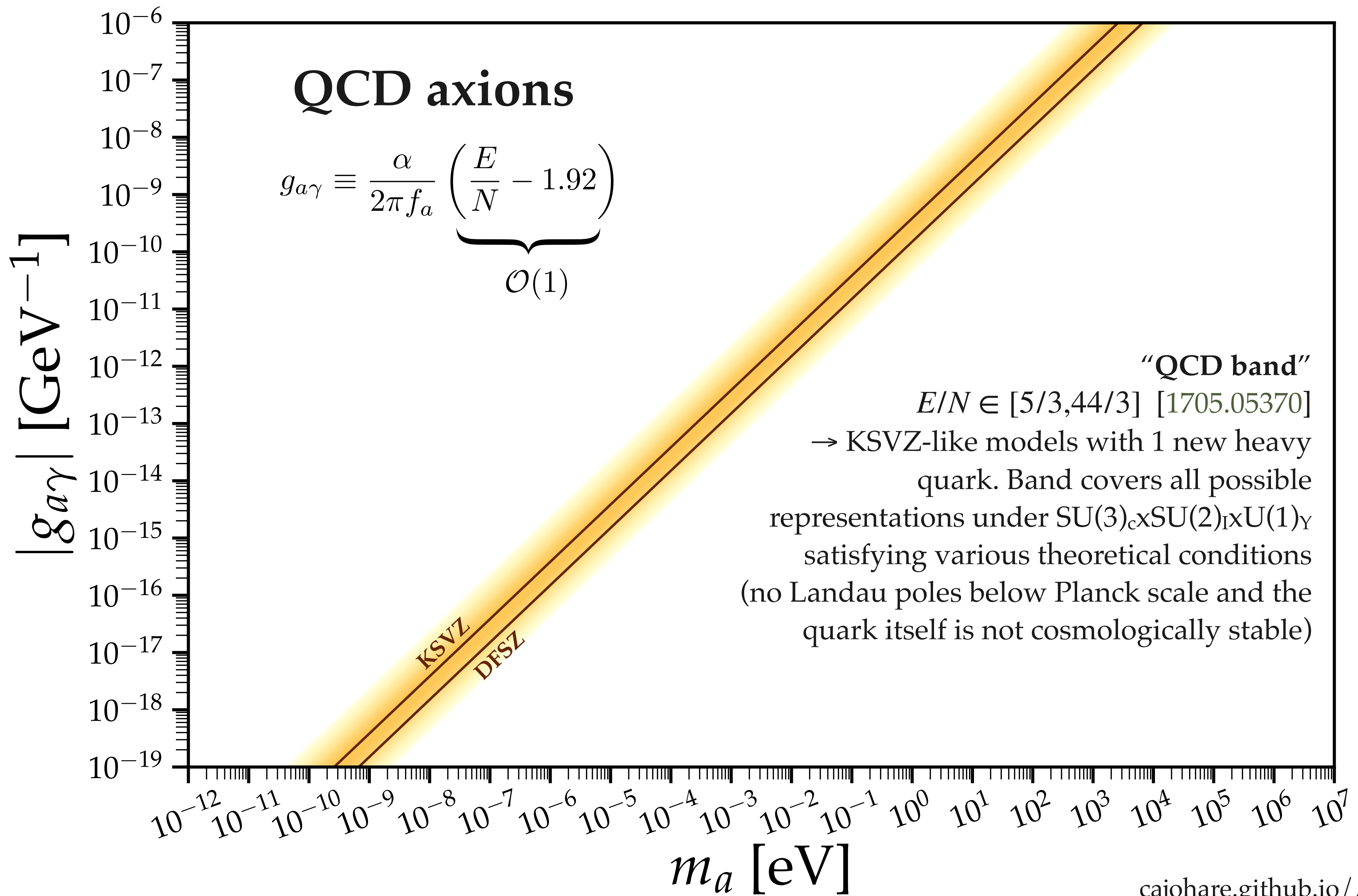
Photon \rightarrow Axion

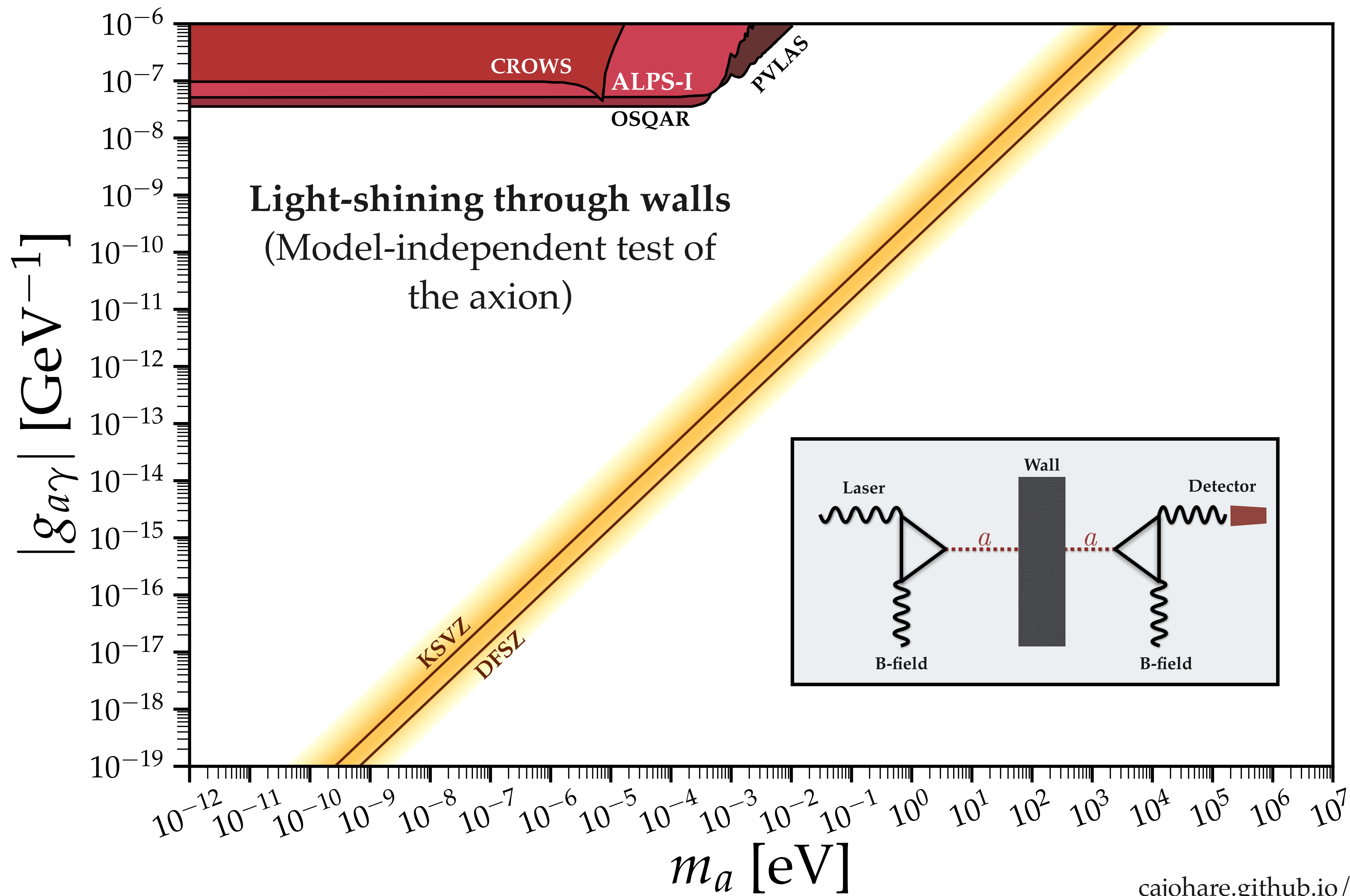


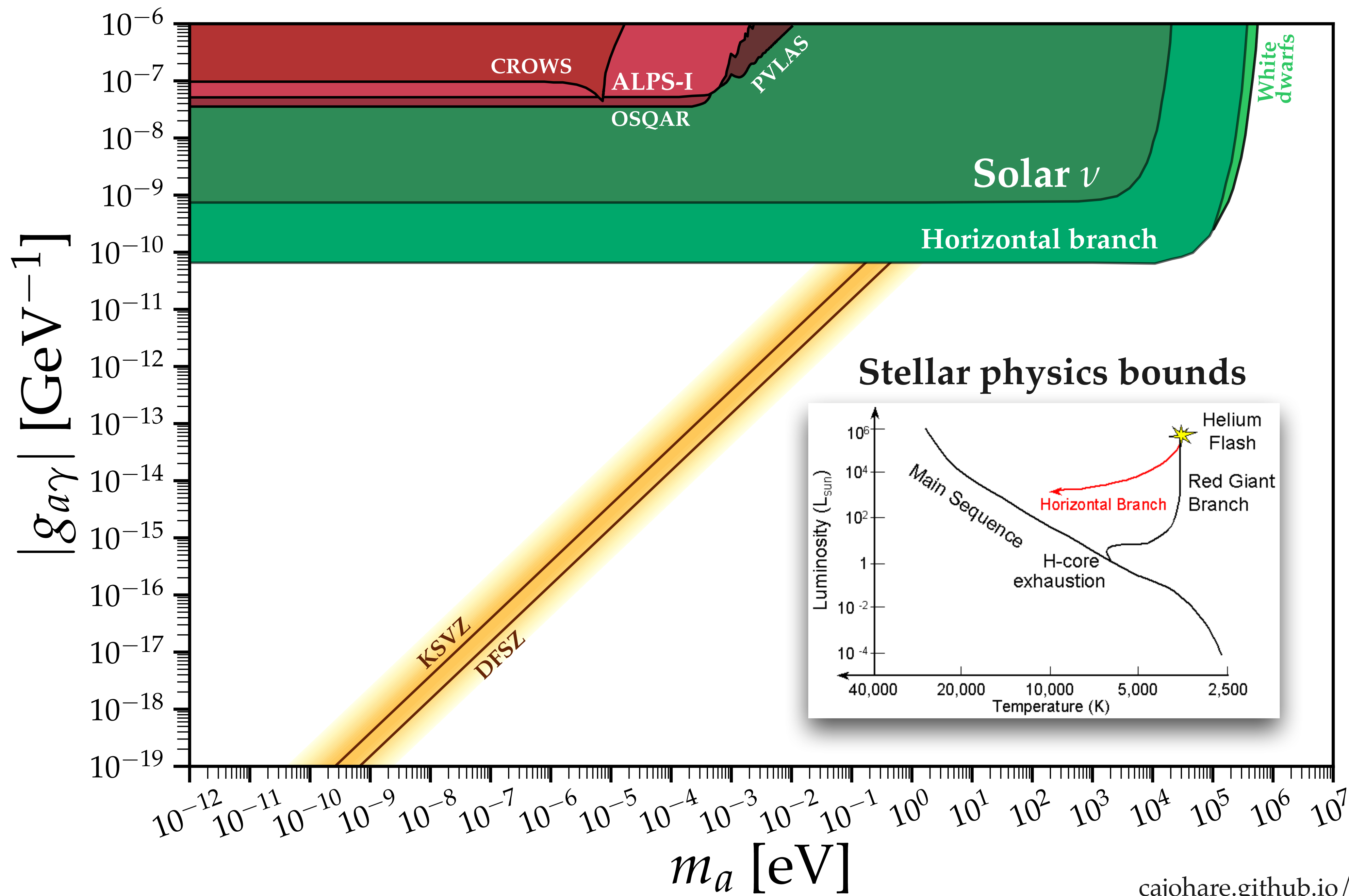
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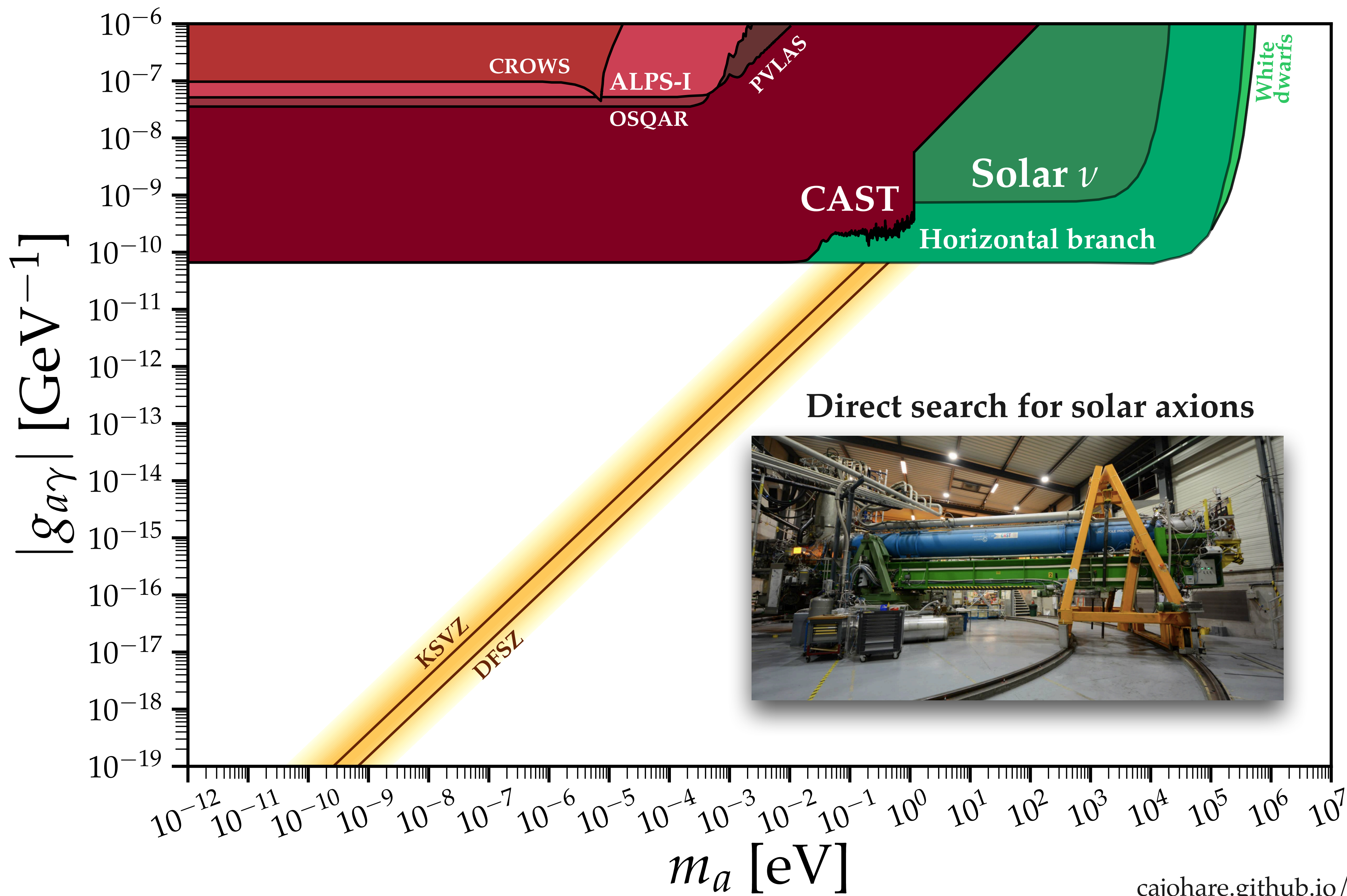


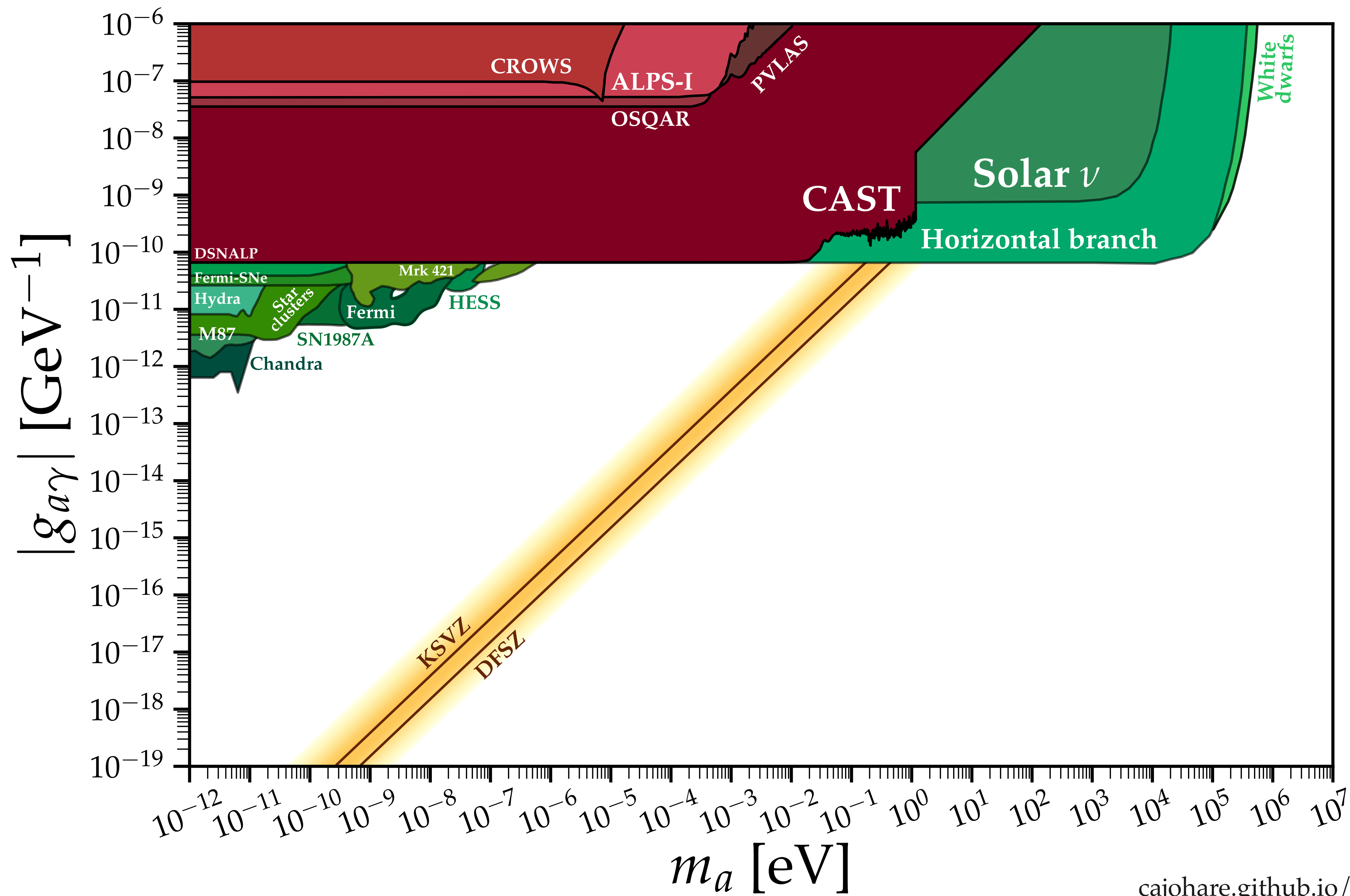


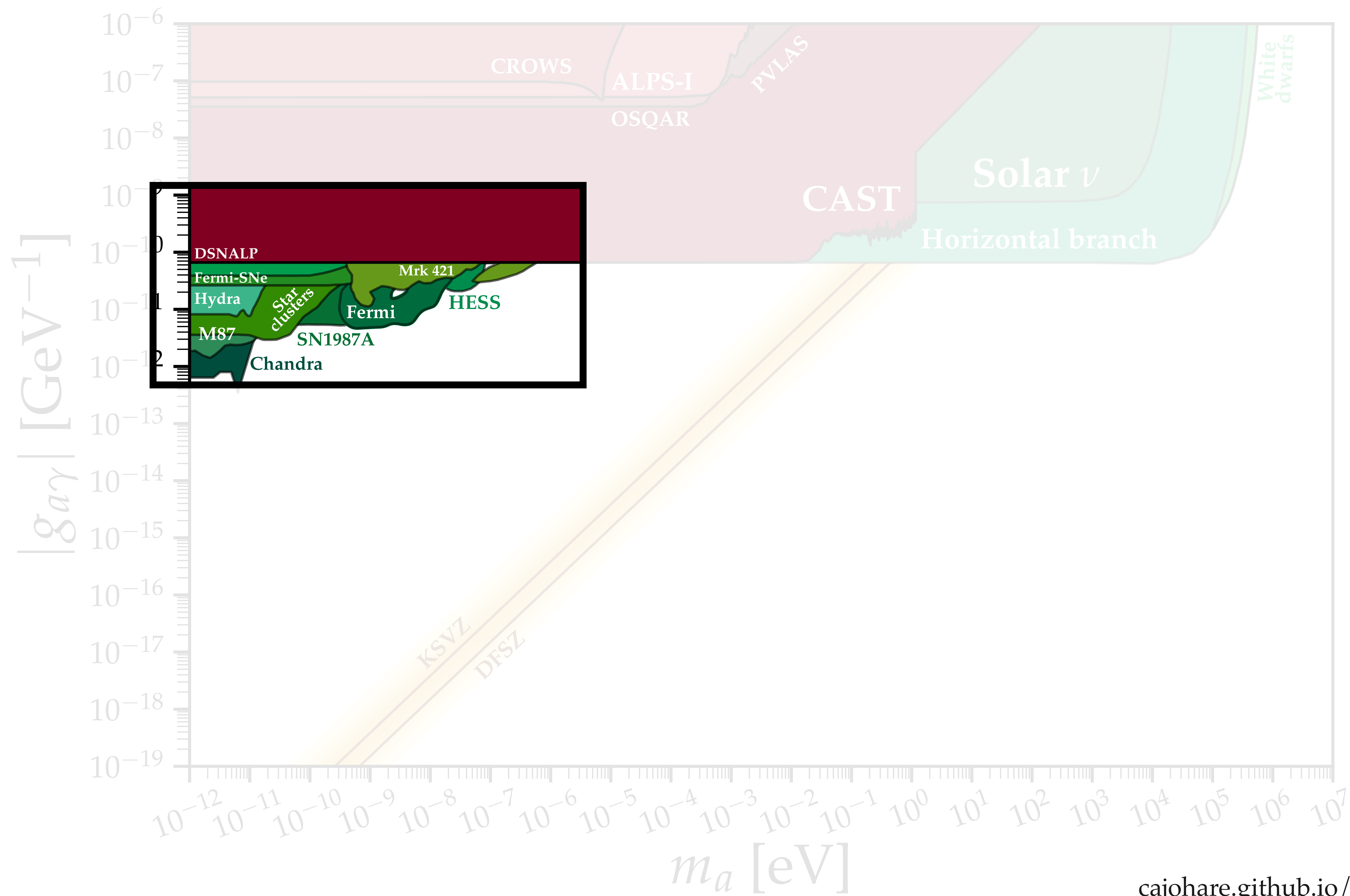




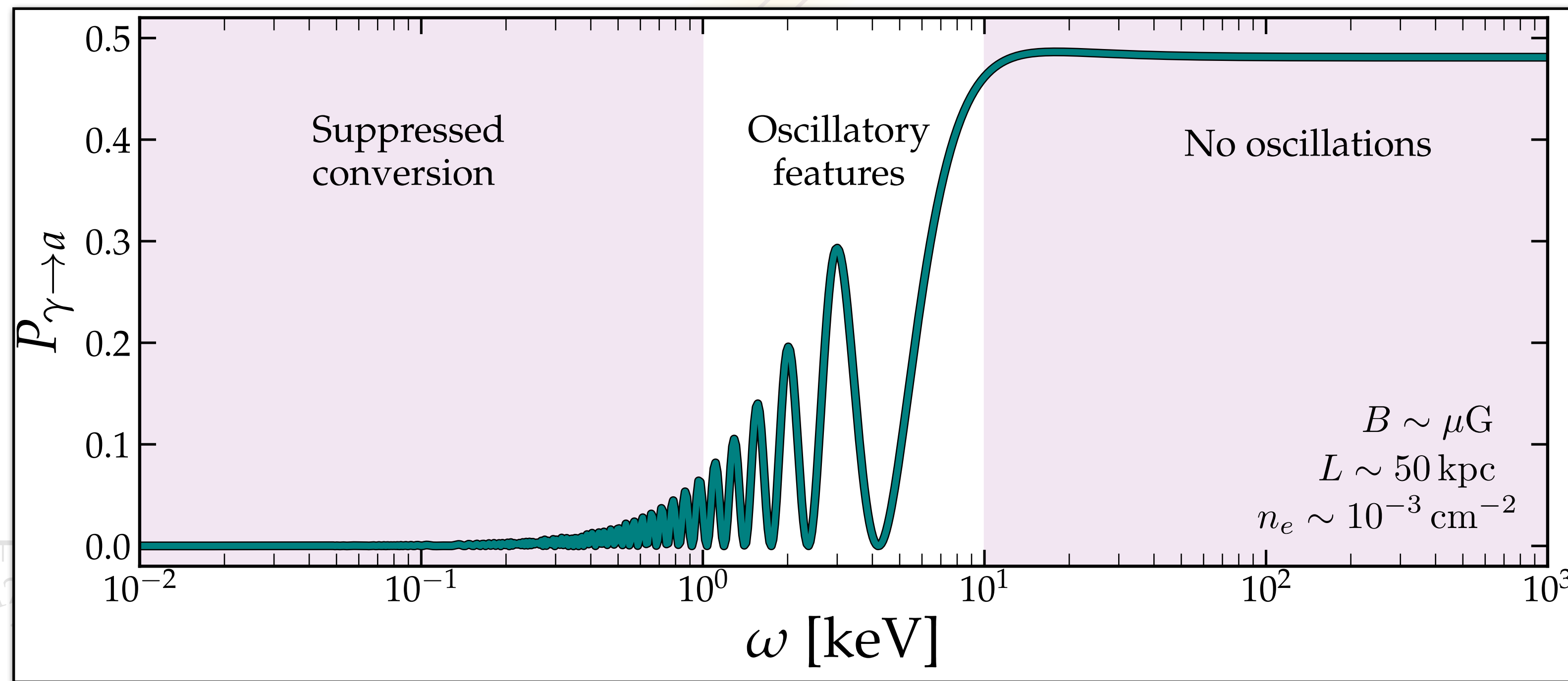
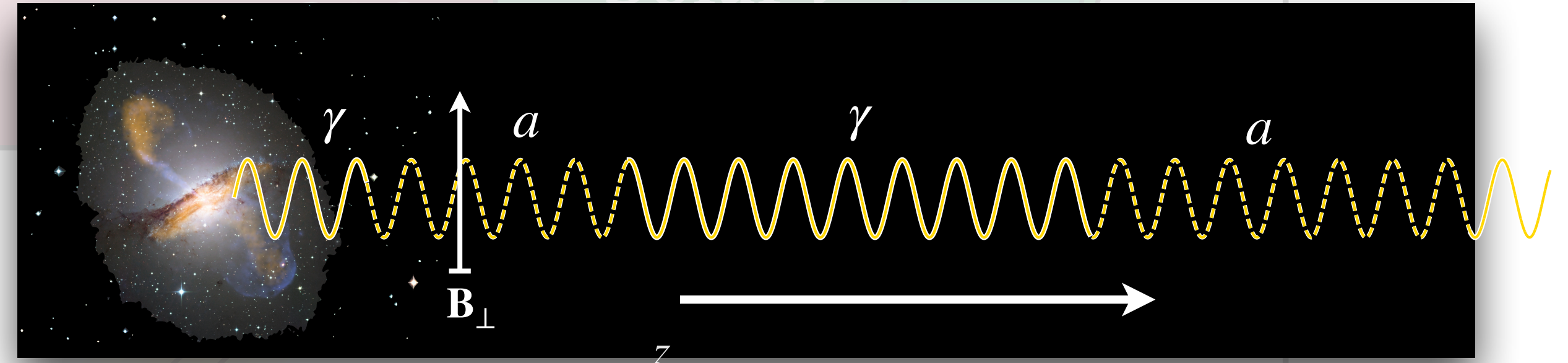
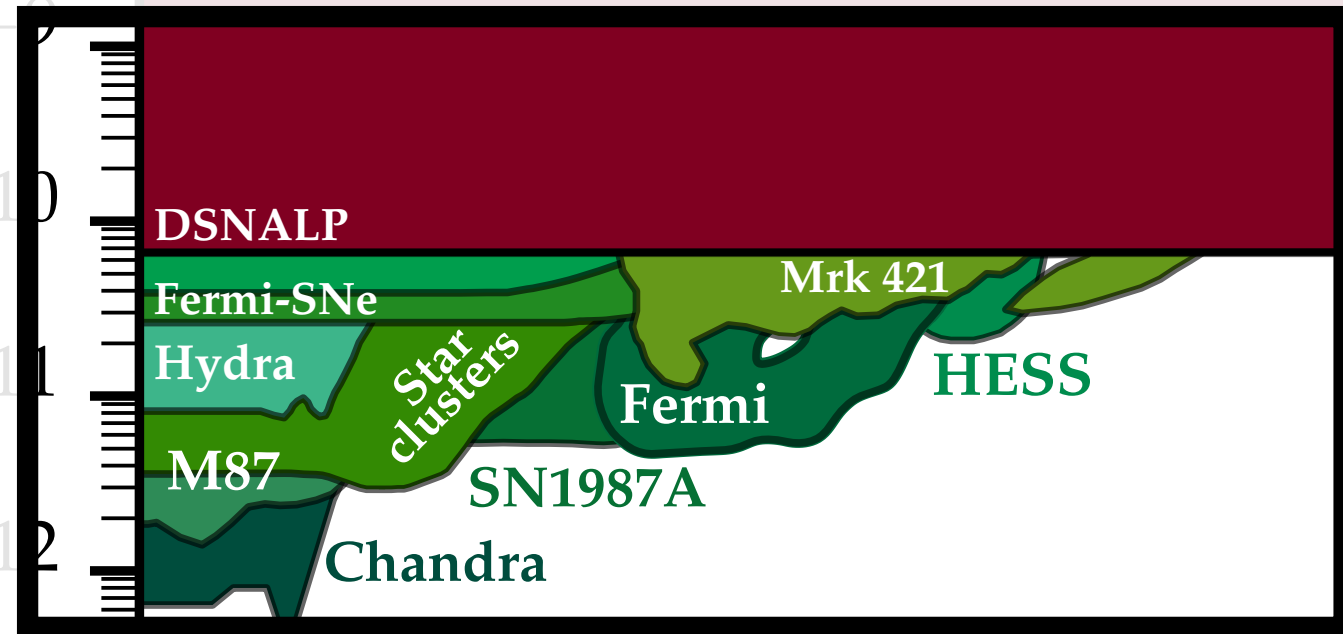


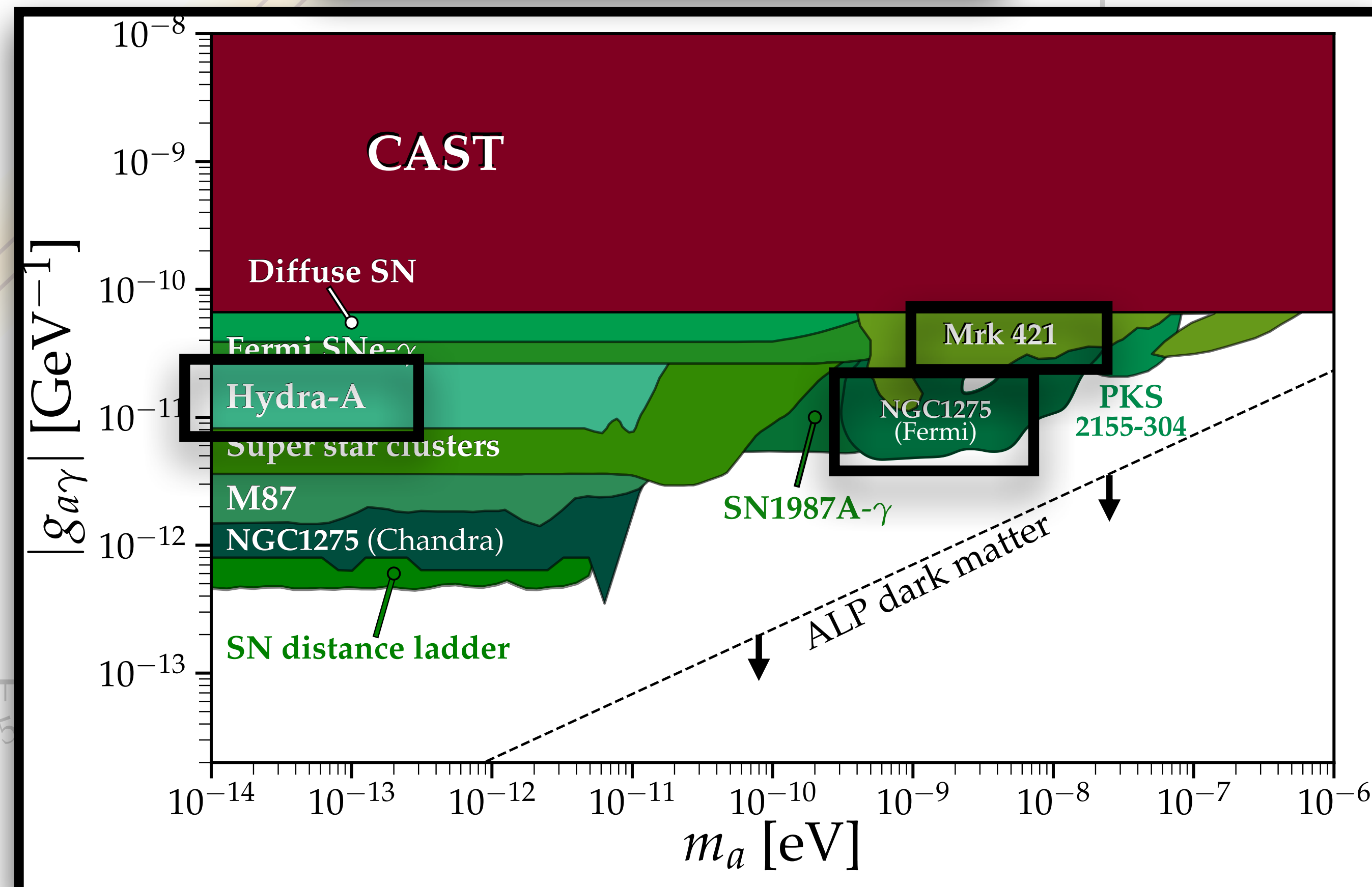
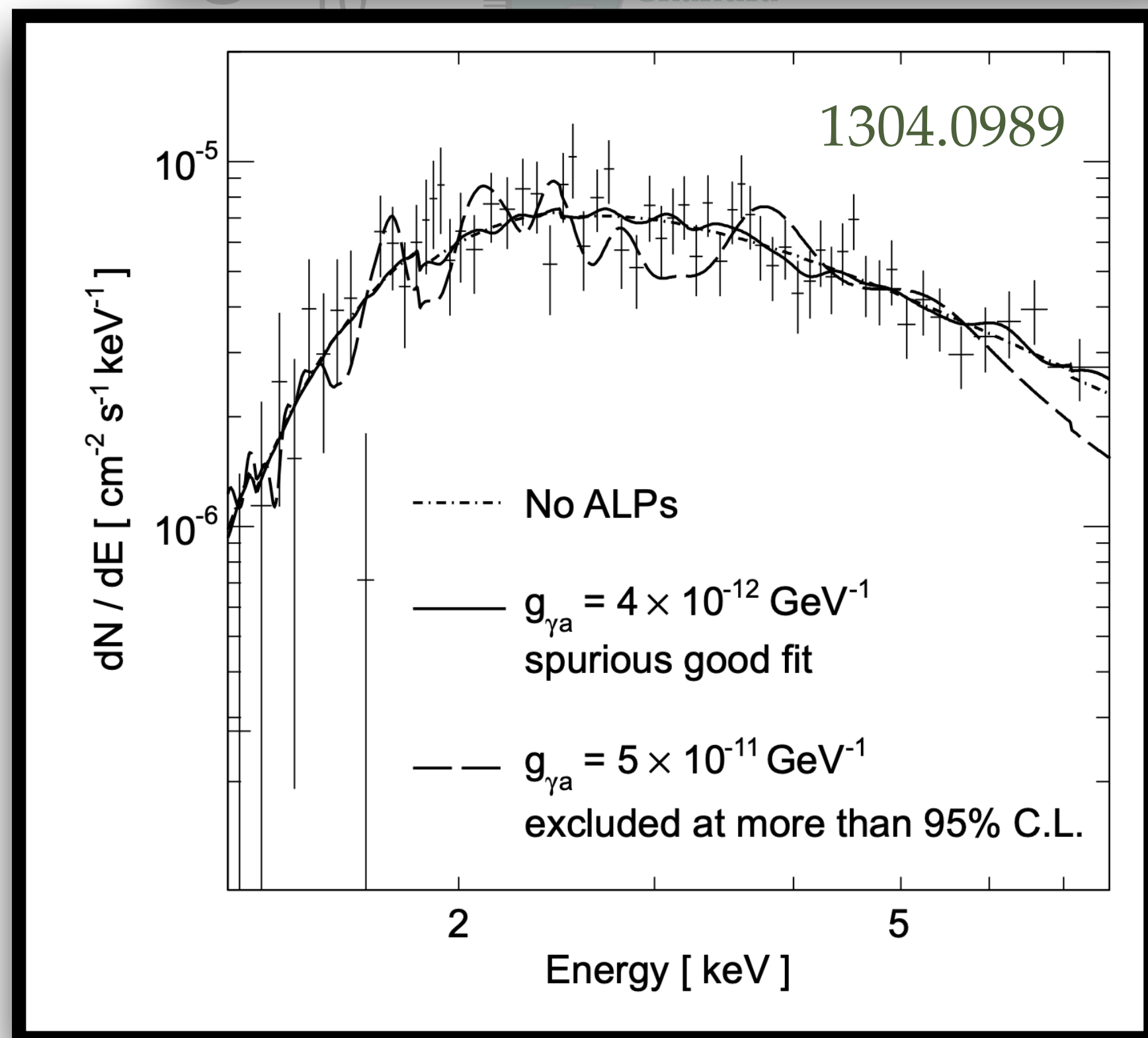
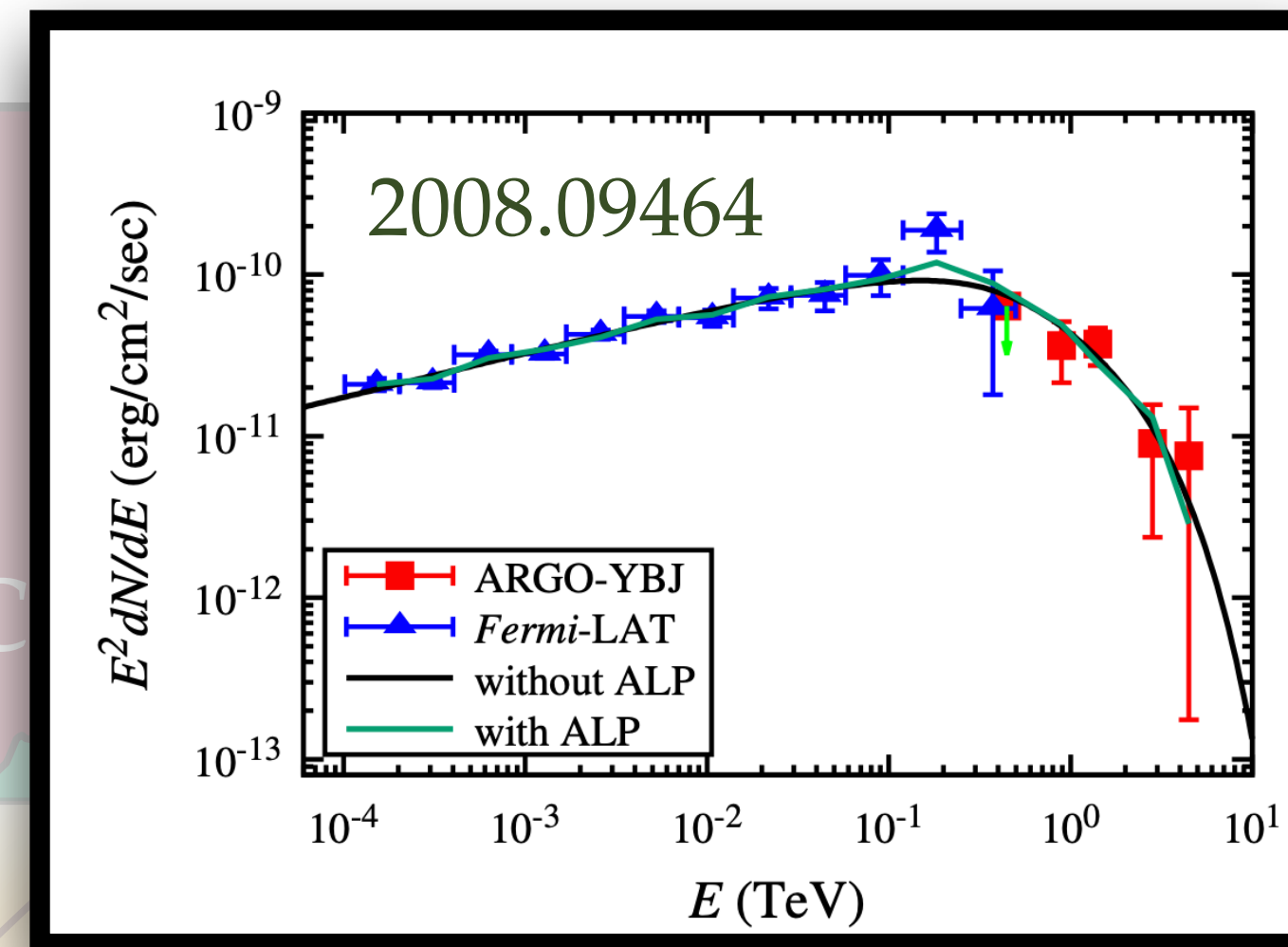
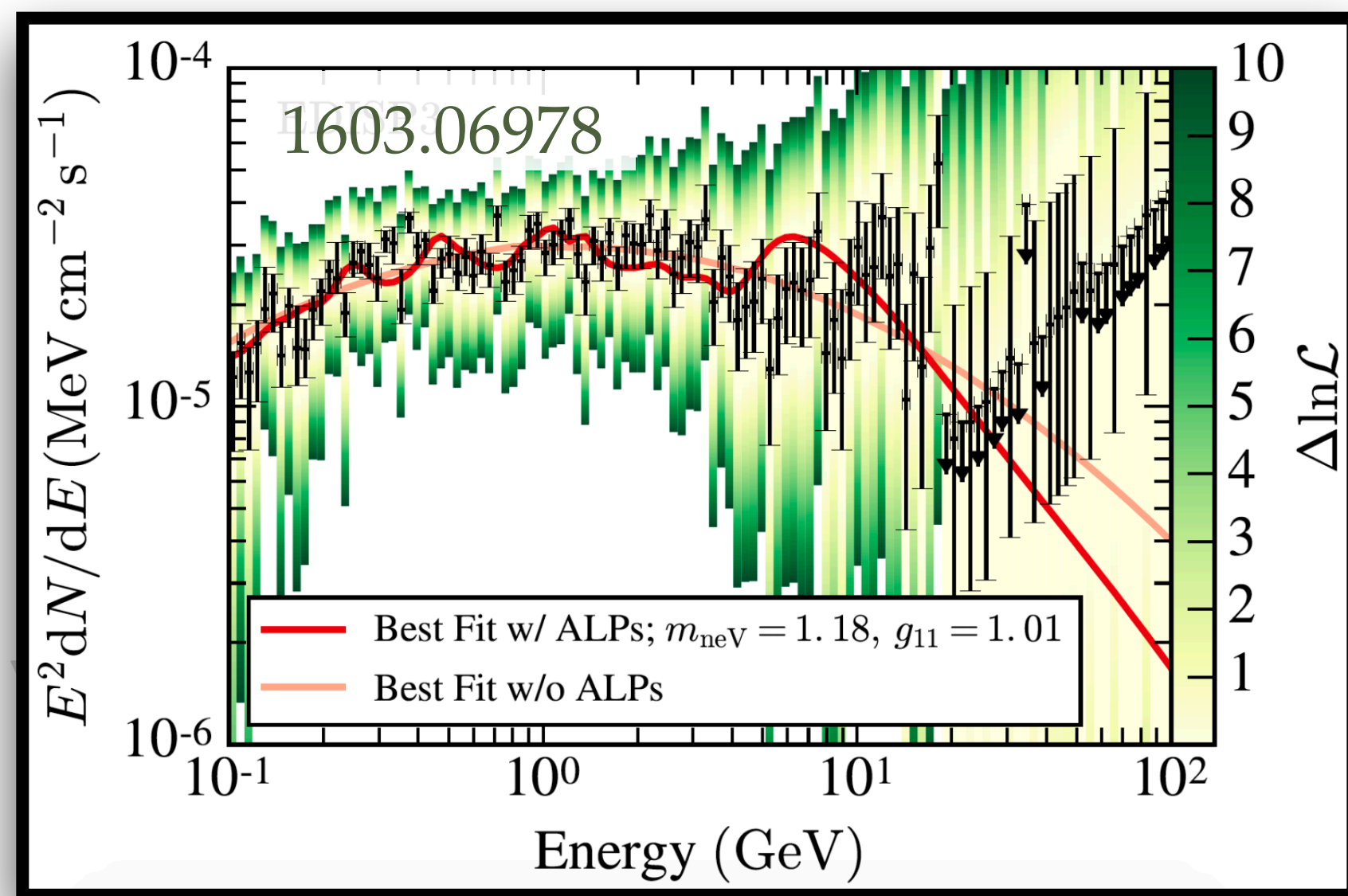


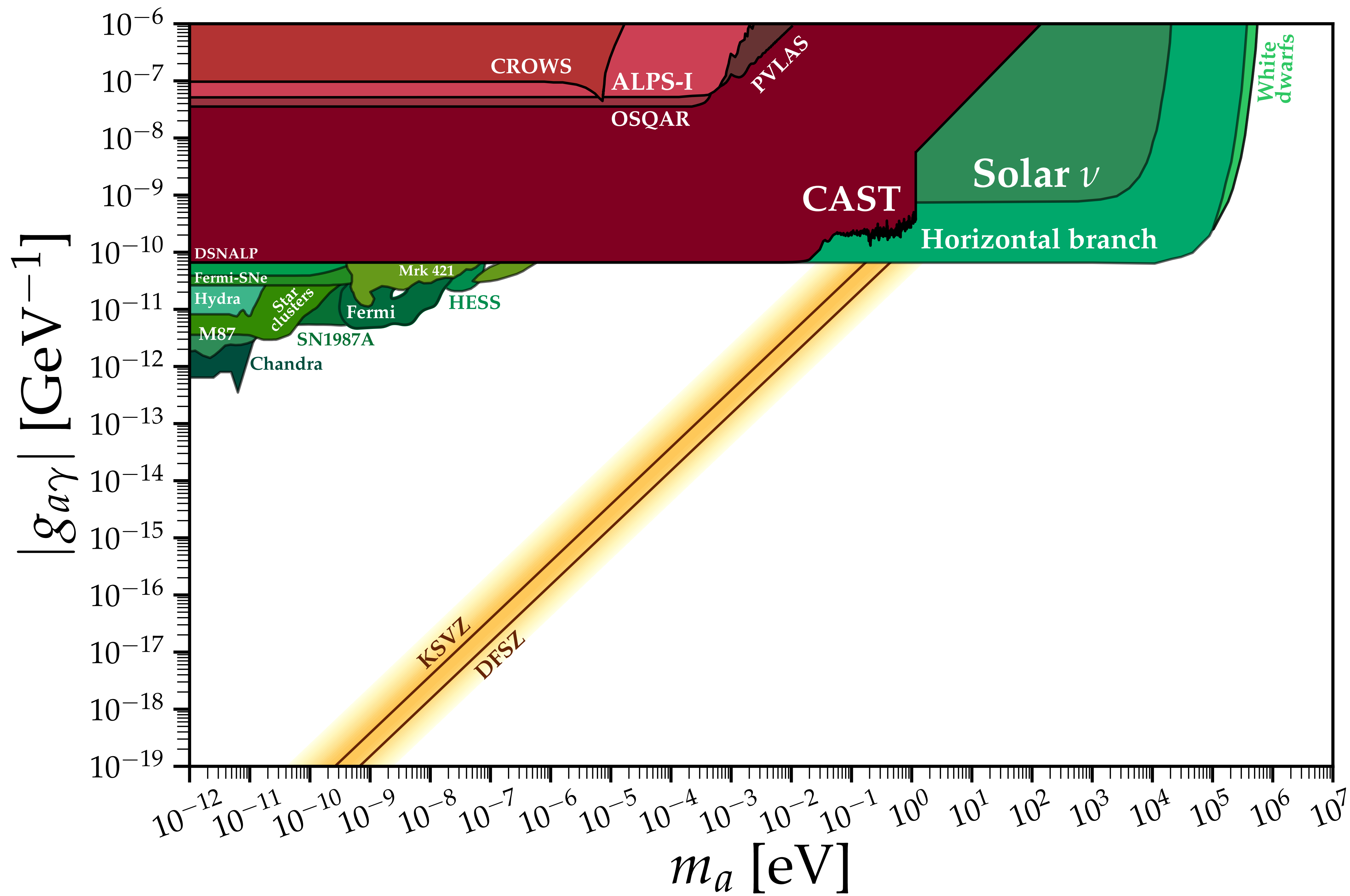


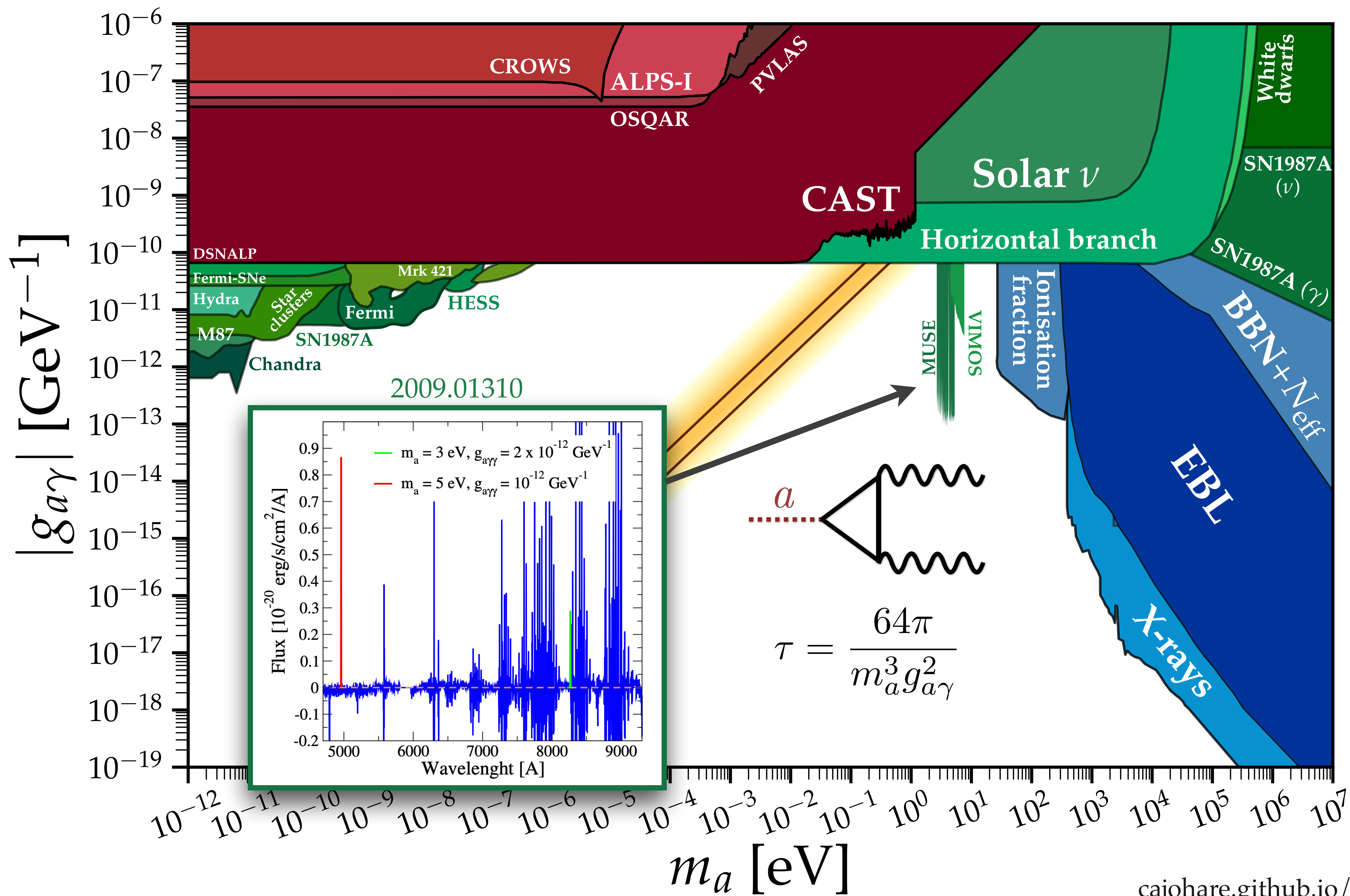


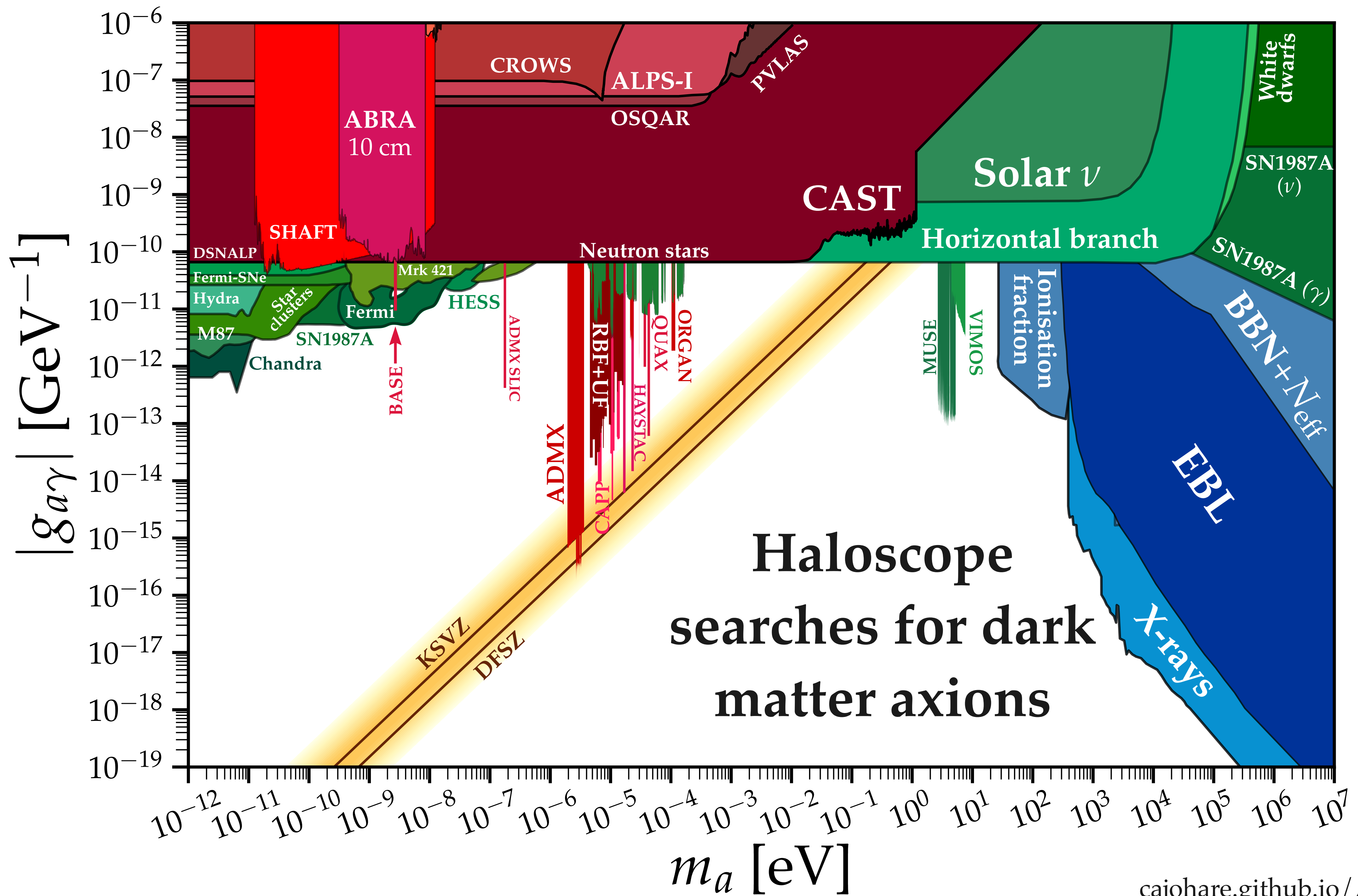
Light ALP-photon oscillations in astrophysical B-fields (Galaxies, galaxy clusters, and the Milky Way)

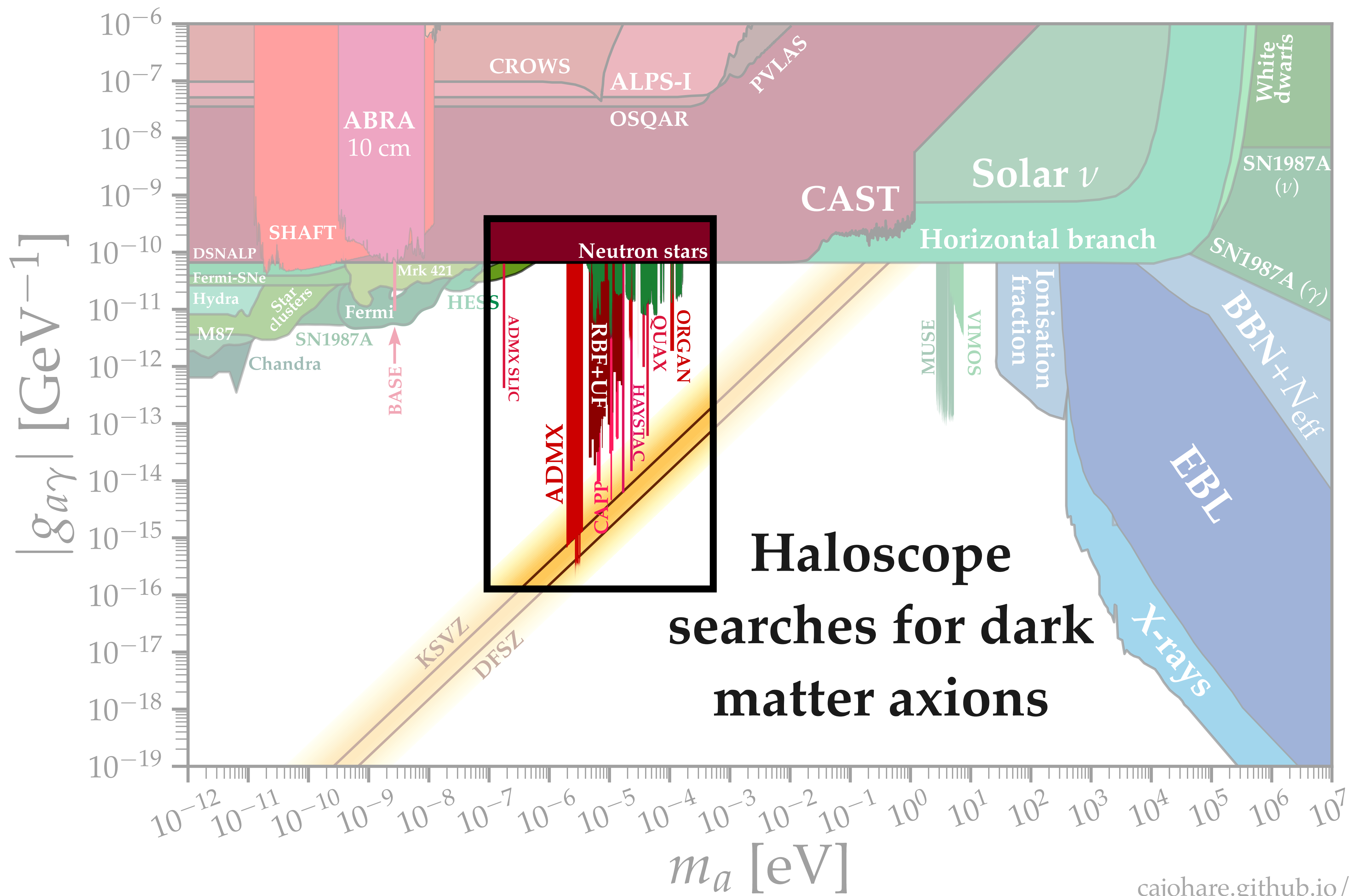




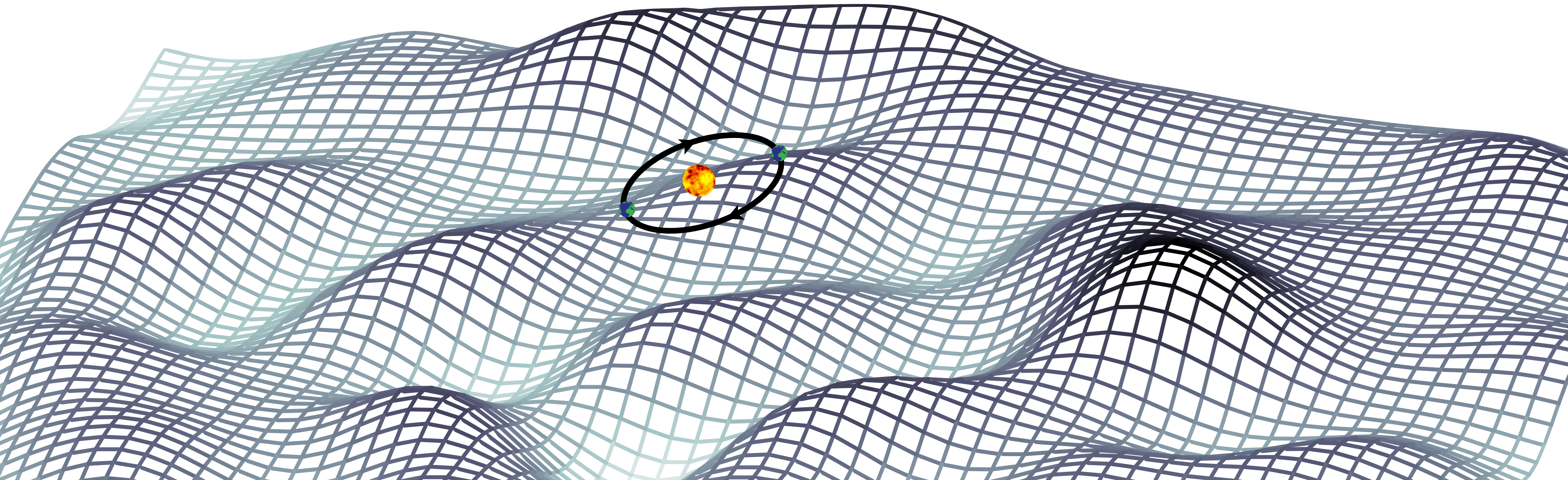








Dark matter axions

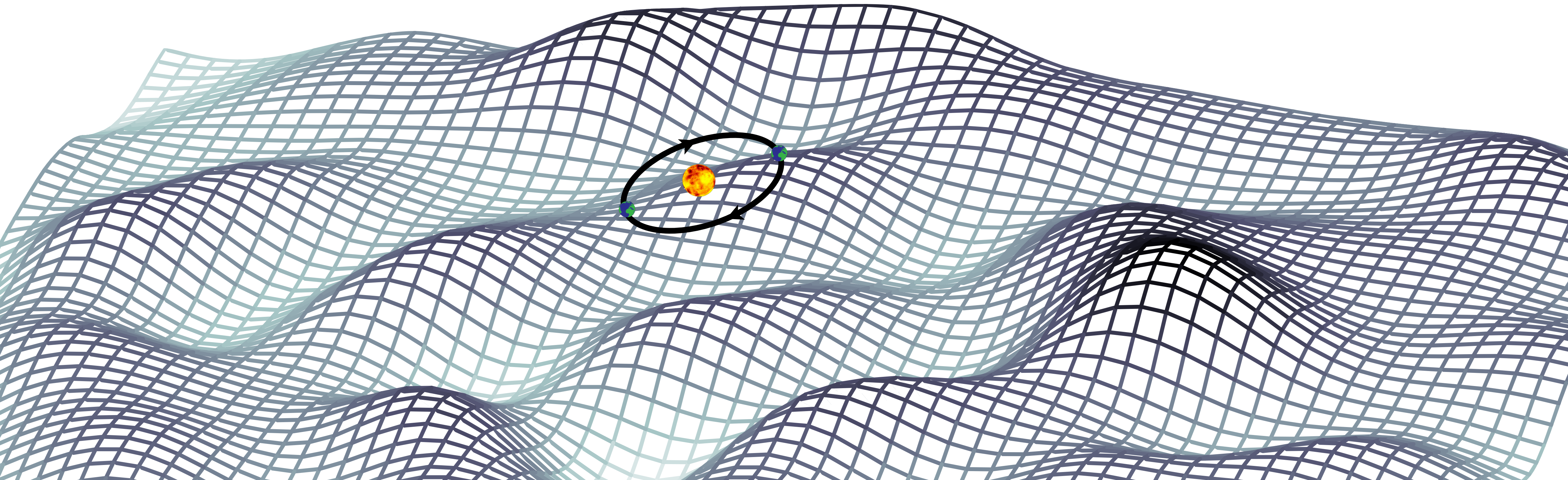


Dark matter axions

behave like a classical field : $a(\mathbf{x}, t) \approx \frac{\sqrt{2\rho_a}}{m_a} \cos(\omega t - \mathbf{p} \cdot \mathbf{x} + \alpha)$

$$\omega \approx m_a$$

Oscillating at the axion mass

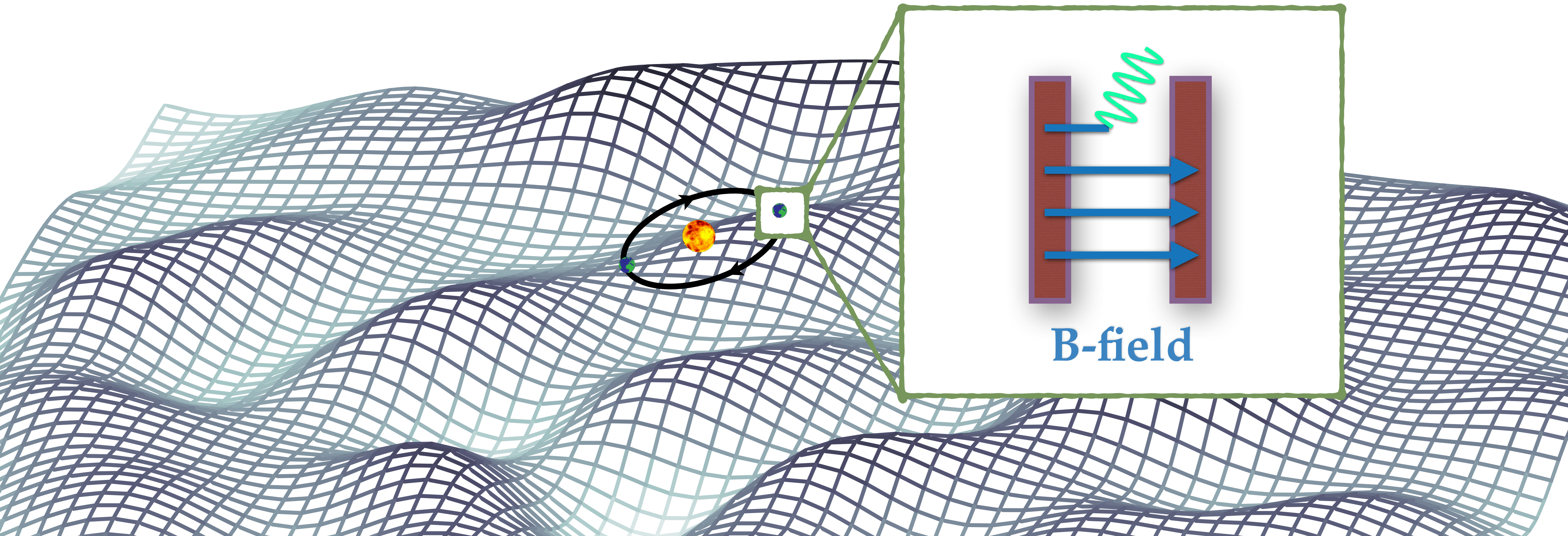


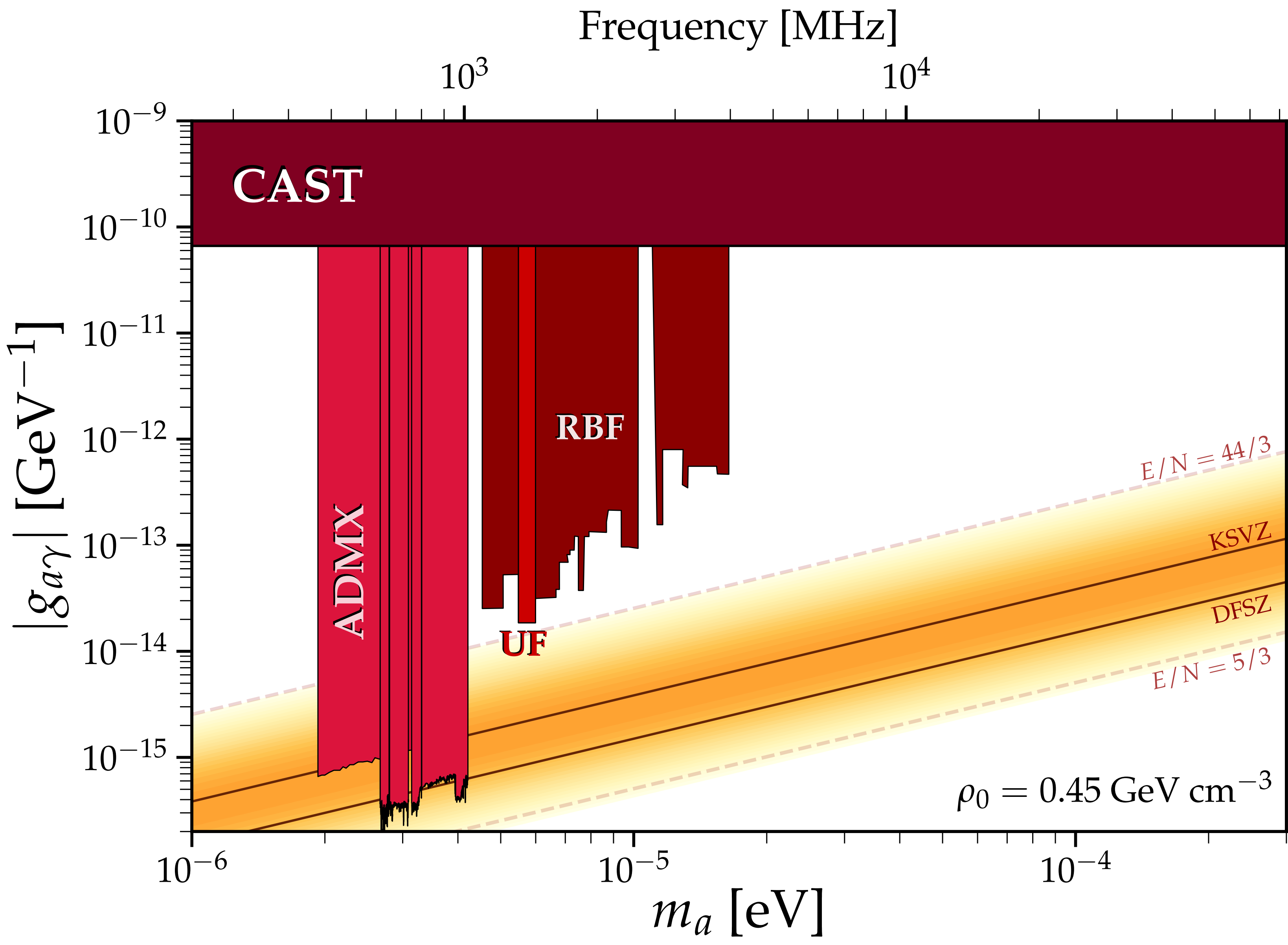
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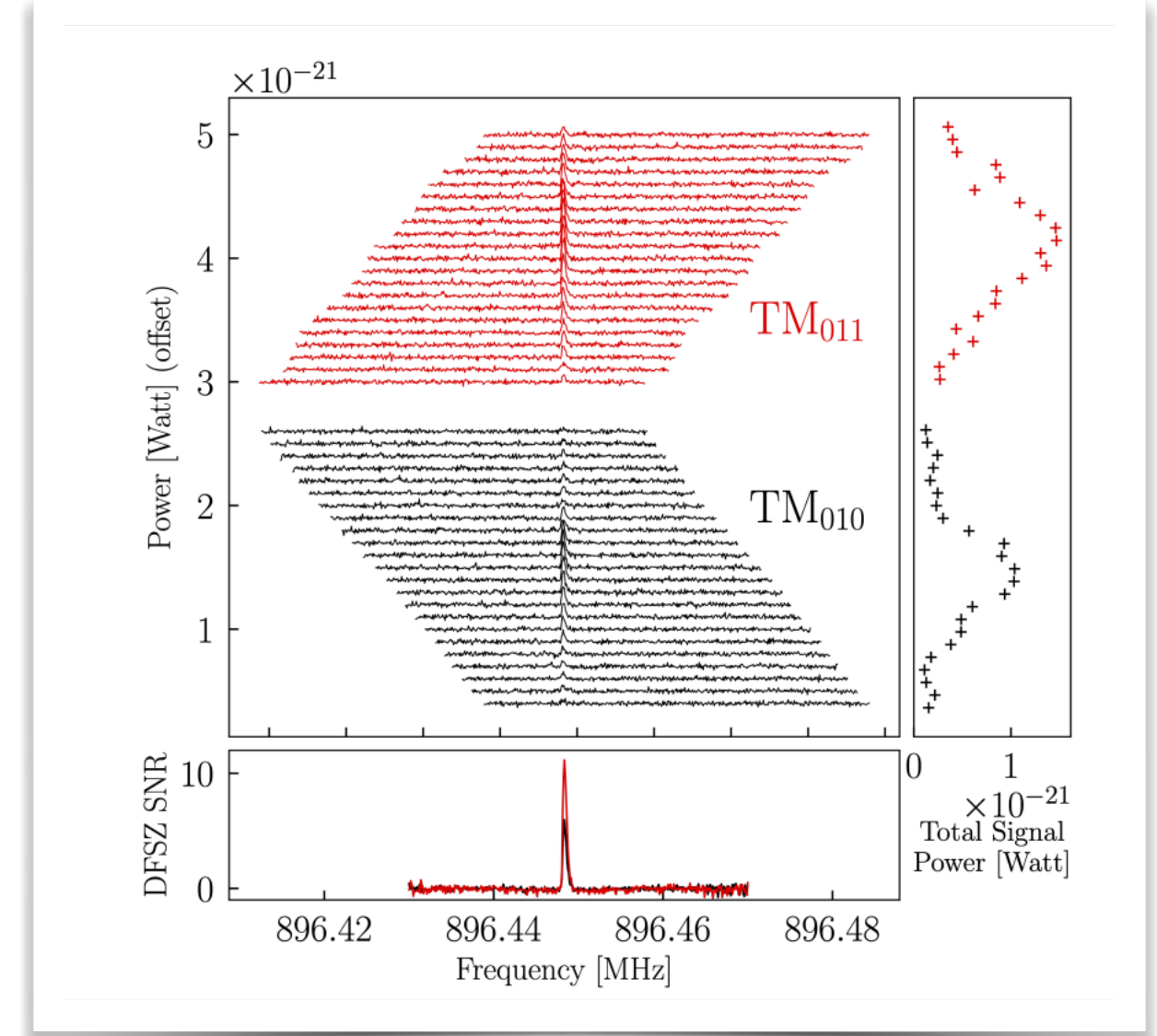
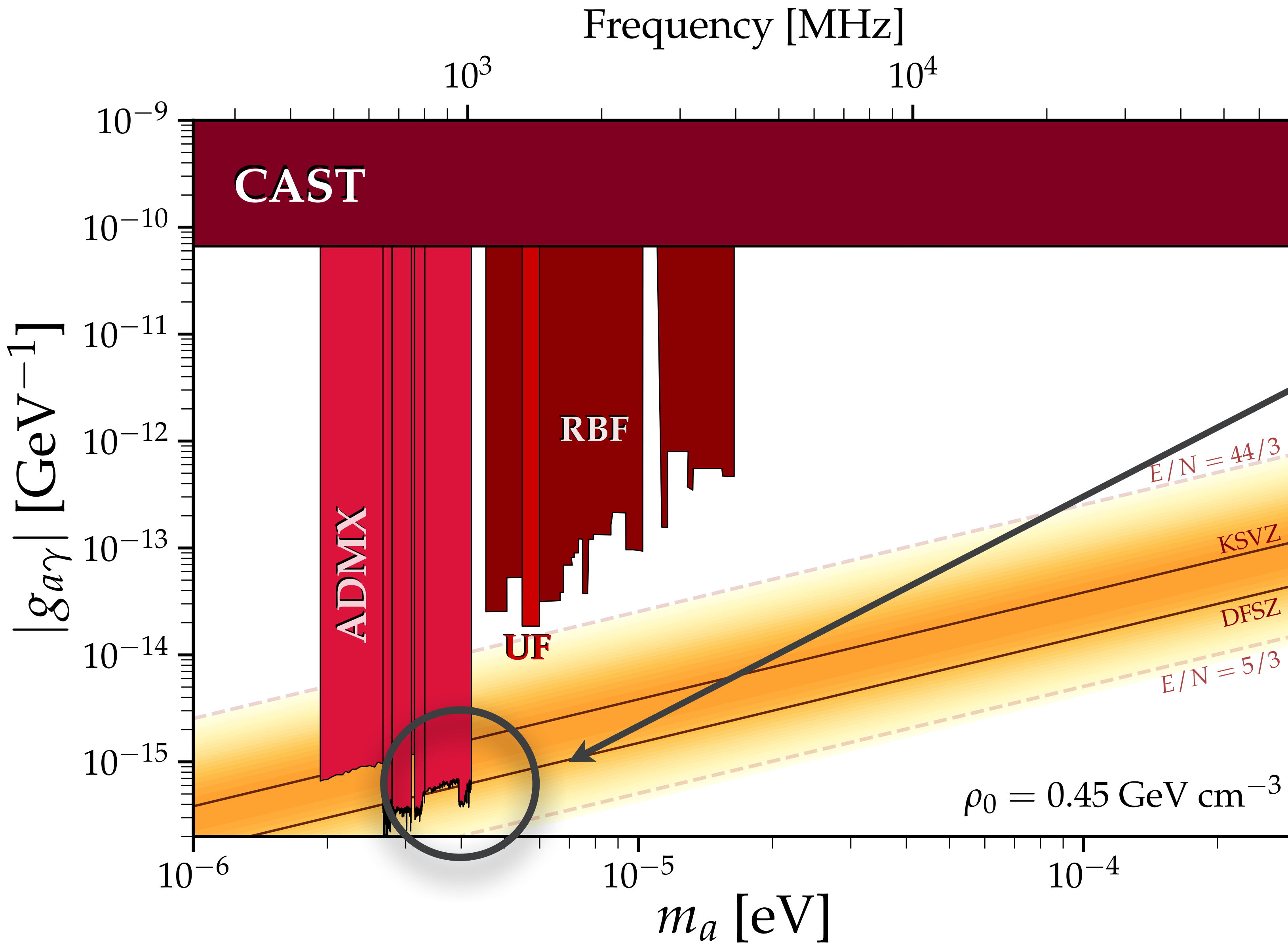
Brand new!

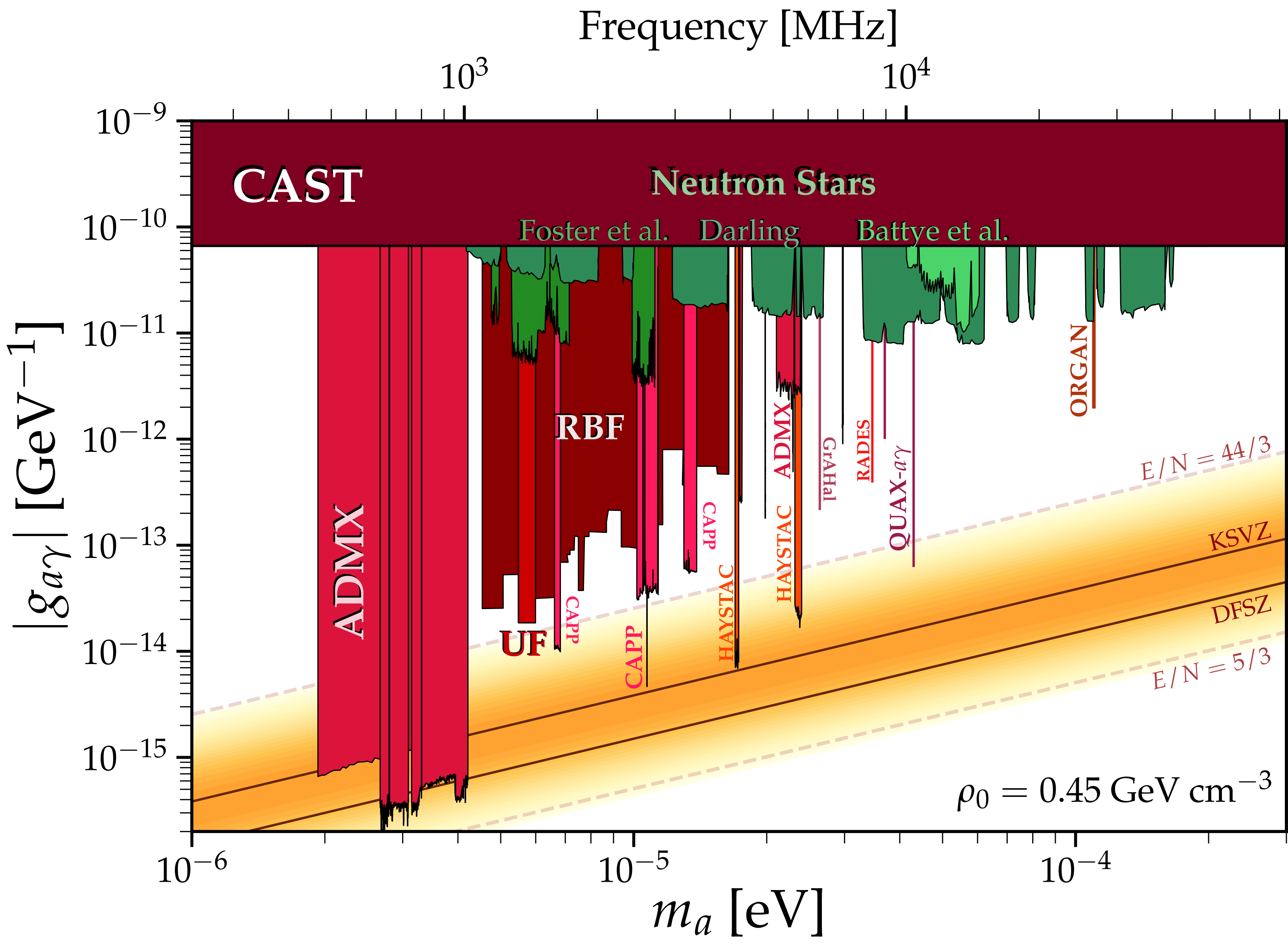
ADMX constrains DFSZ axions above $3 \mu\text{eV}$

[2110.06096]

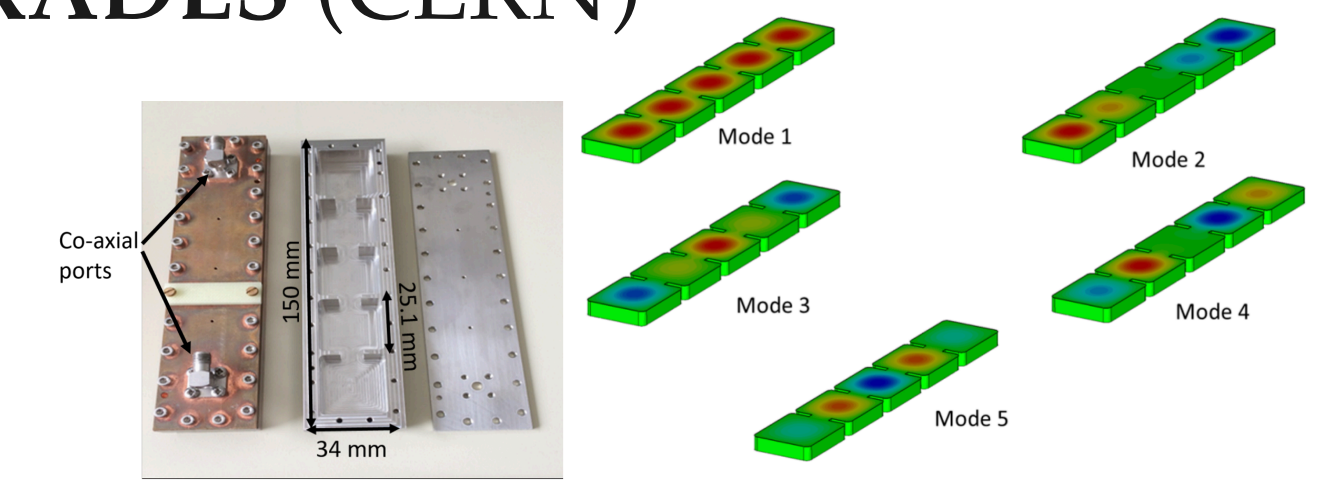
Search for “Invisible” Axion Dark Matter in the 3.3–4.2 μeV Mass Range

C. Bartram,¹ T. Braine,¹ E. Burns,¹ R. Cervantes,¹ N. Crisosto,¹ N. Du,¹ H. Korandla,¹ G. Leum,¹ P. Mohapatra,¹ T. Nitta,^{1,*} L. J. Rosenberg,¹ G. Rybka,¹ J. Yang,¹ John Clarke,² I. Siddiqi,² A. Agrawal,³ A. V. Dixit,³ M. H. Awida,⁴ A. S. Chou,⁴ M. Hollister,⁴ S. Knirck,⁴ A. Sonnenschein,⁴ W. Wester,⁴ J. R. Gleason,⁵ A.

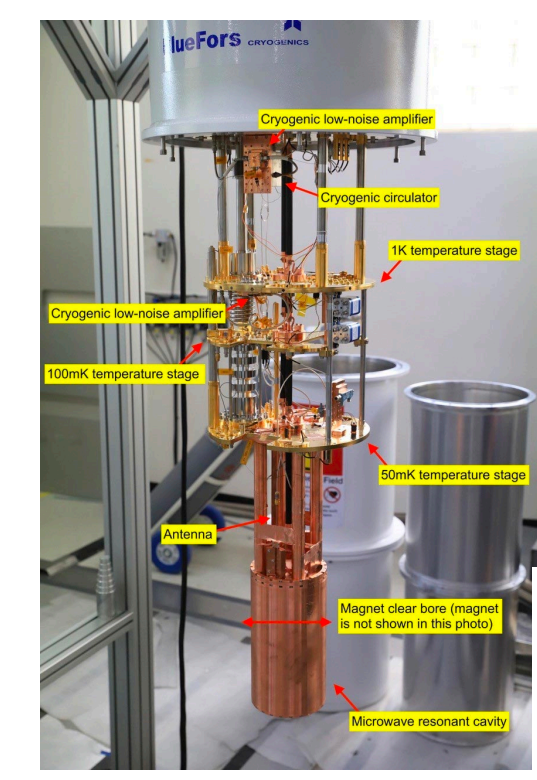




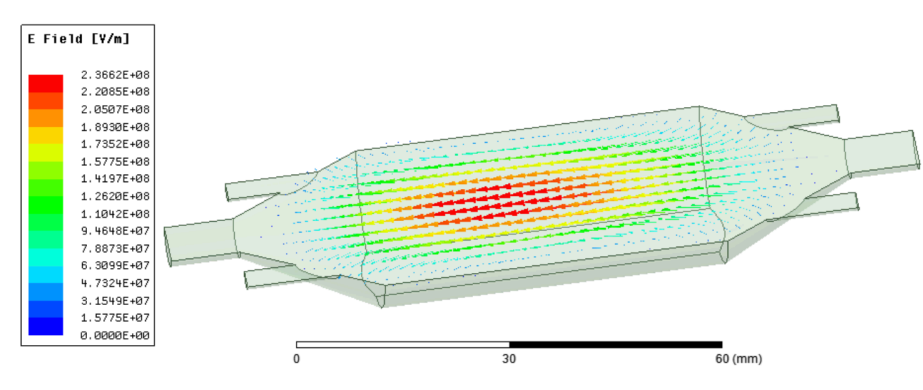
RADES (CERN)



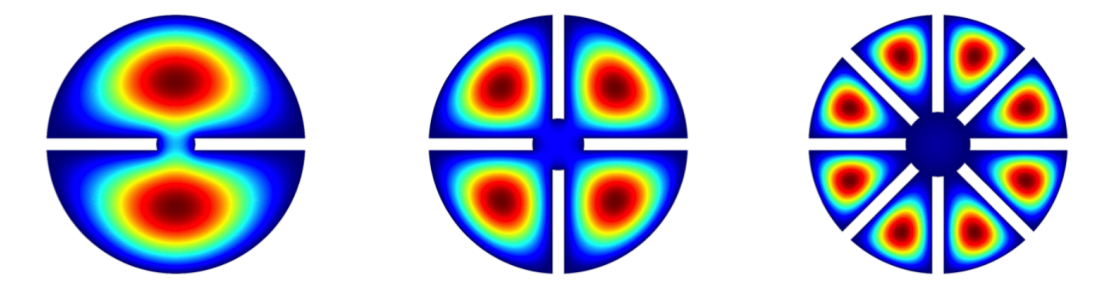
ORGAN (UWA)



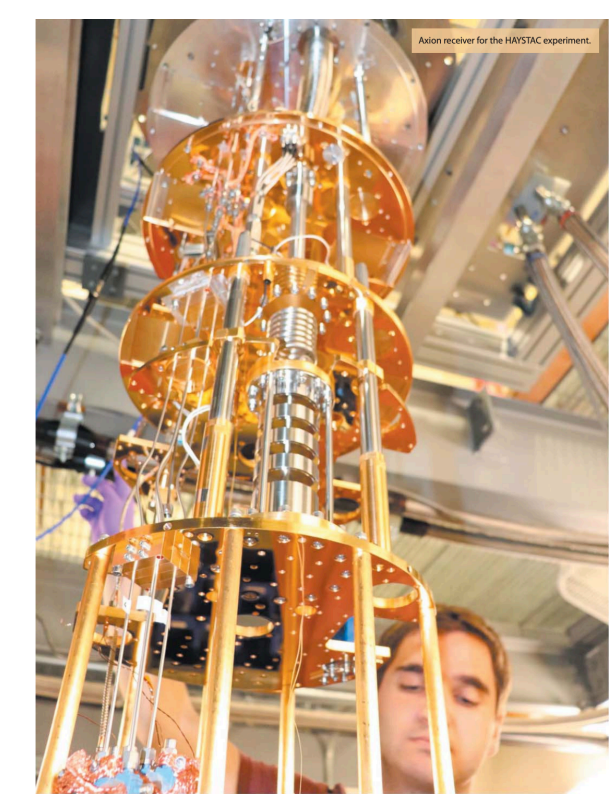
QUAX (Frascati)



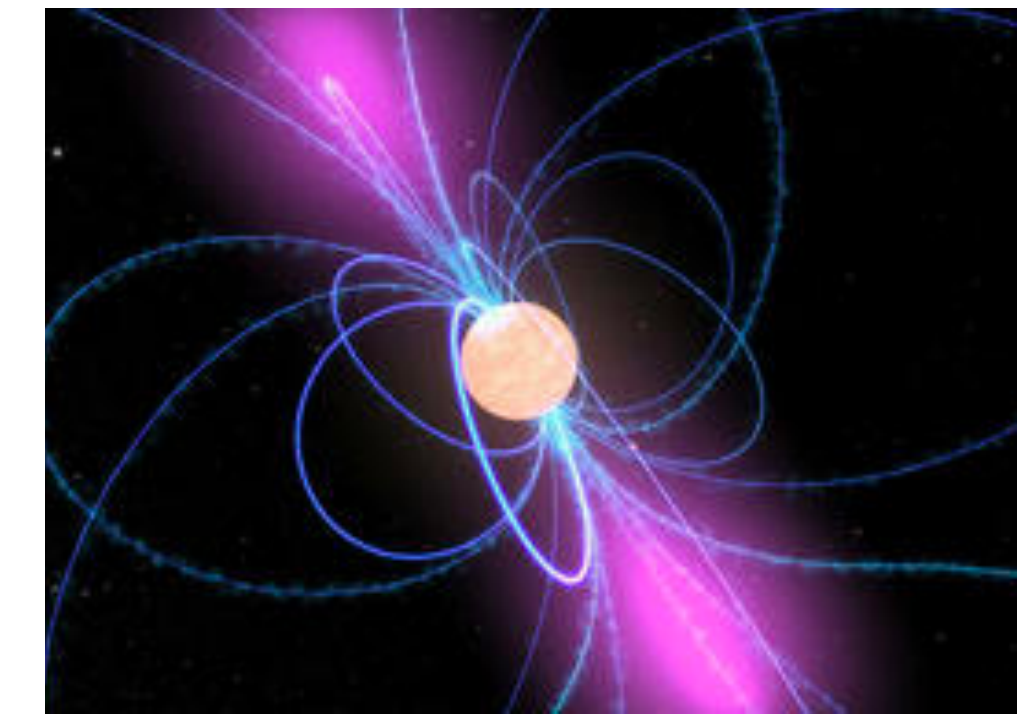
CAPP (IBS)



HAYSTAC (Yale)



Neutron stars

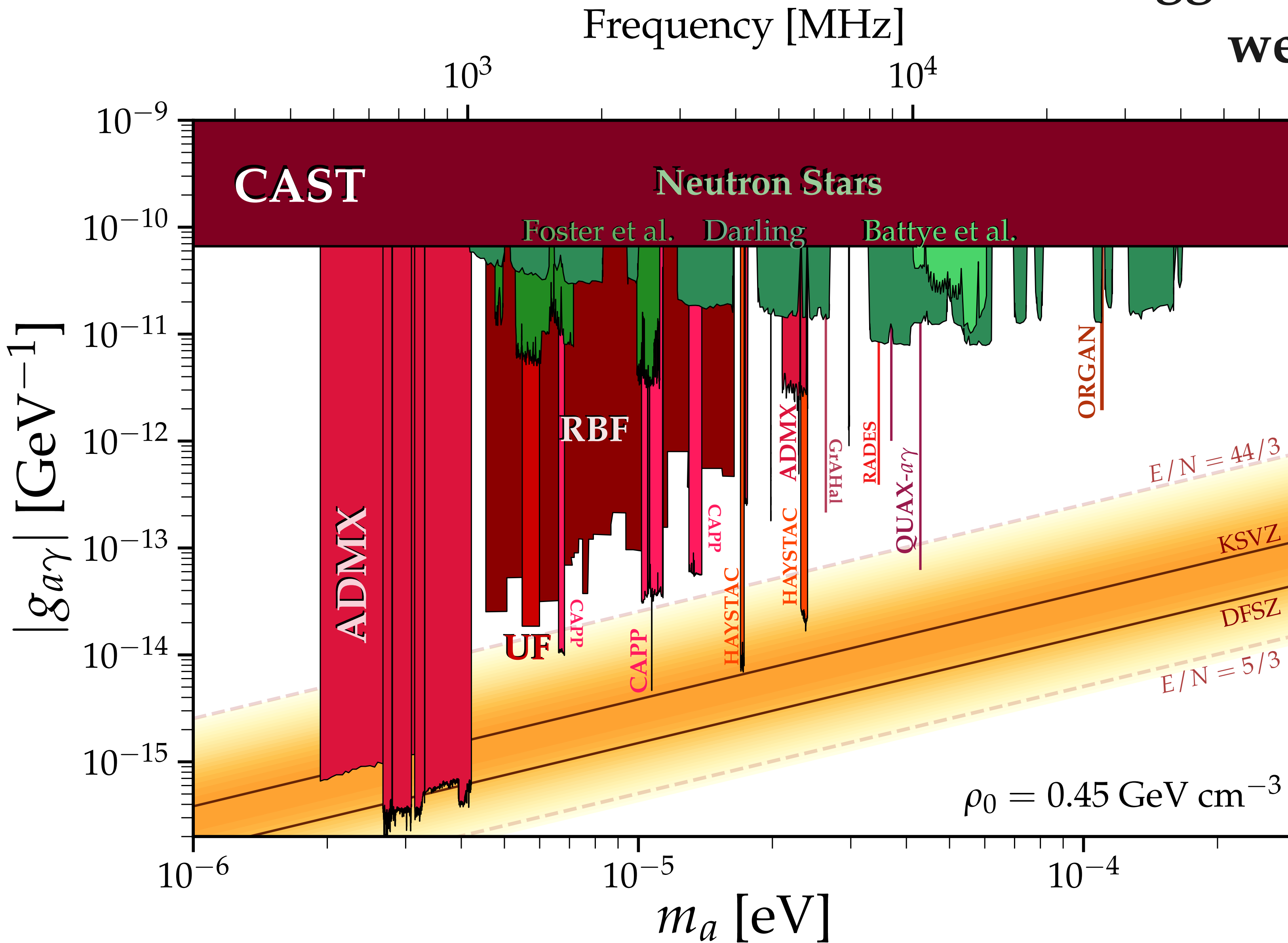


Biggest challenge right now is that we don't know the axion mass

Sensitivity:

$$g_{a\gamma} \propto T^{-1/4}$$

Will take a long time to cover DFSZ from $\mu\text{eV} - 100 \mu\text{eV}$

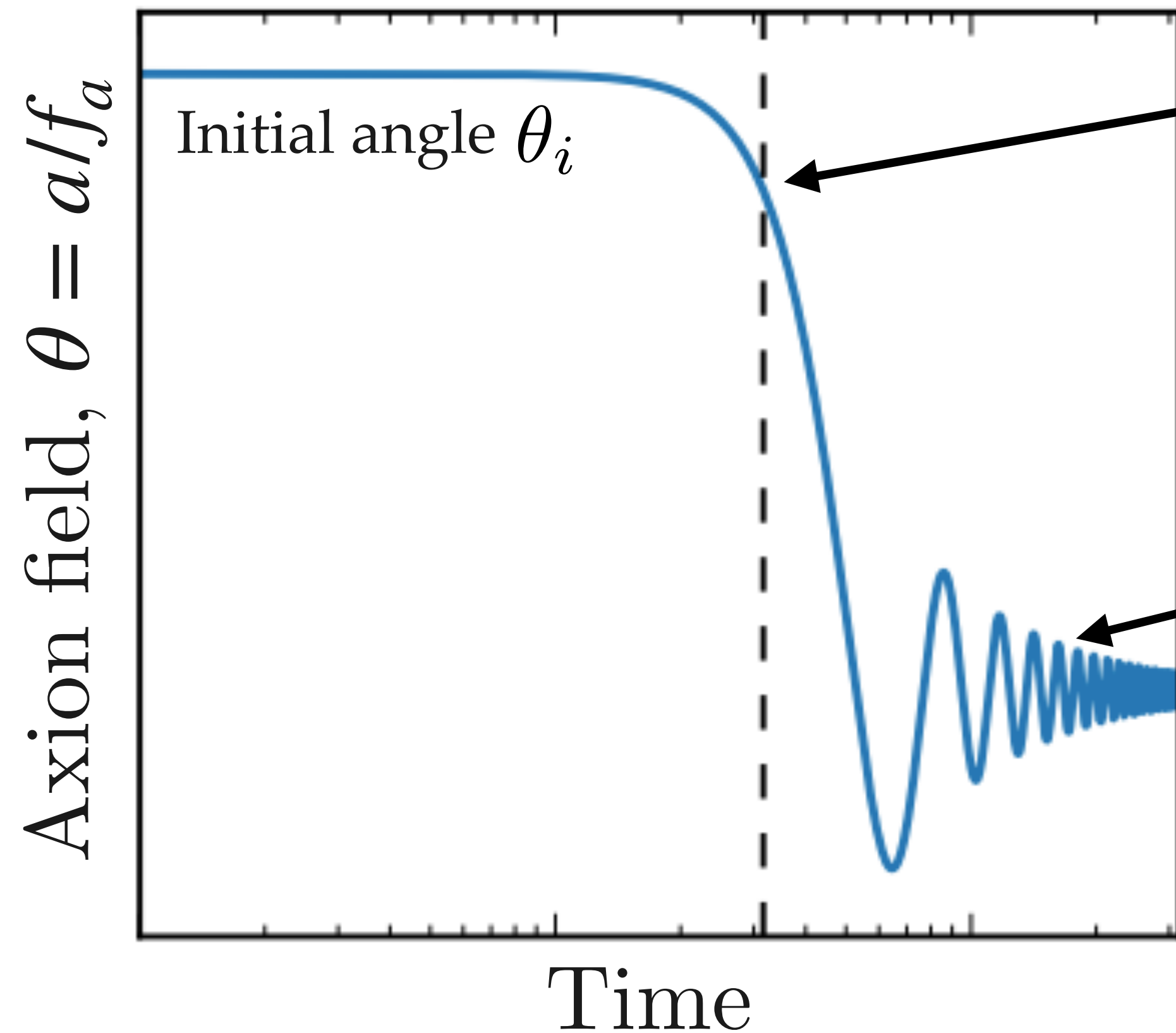


How good are our chances of detecting the axion?

For the sake of argument, let's assume that a canonical QCD axion model to make up 100% of dark matter

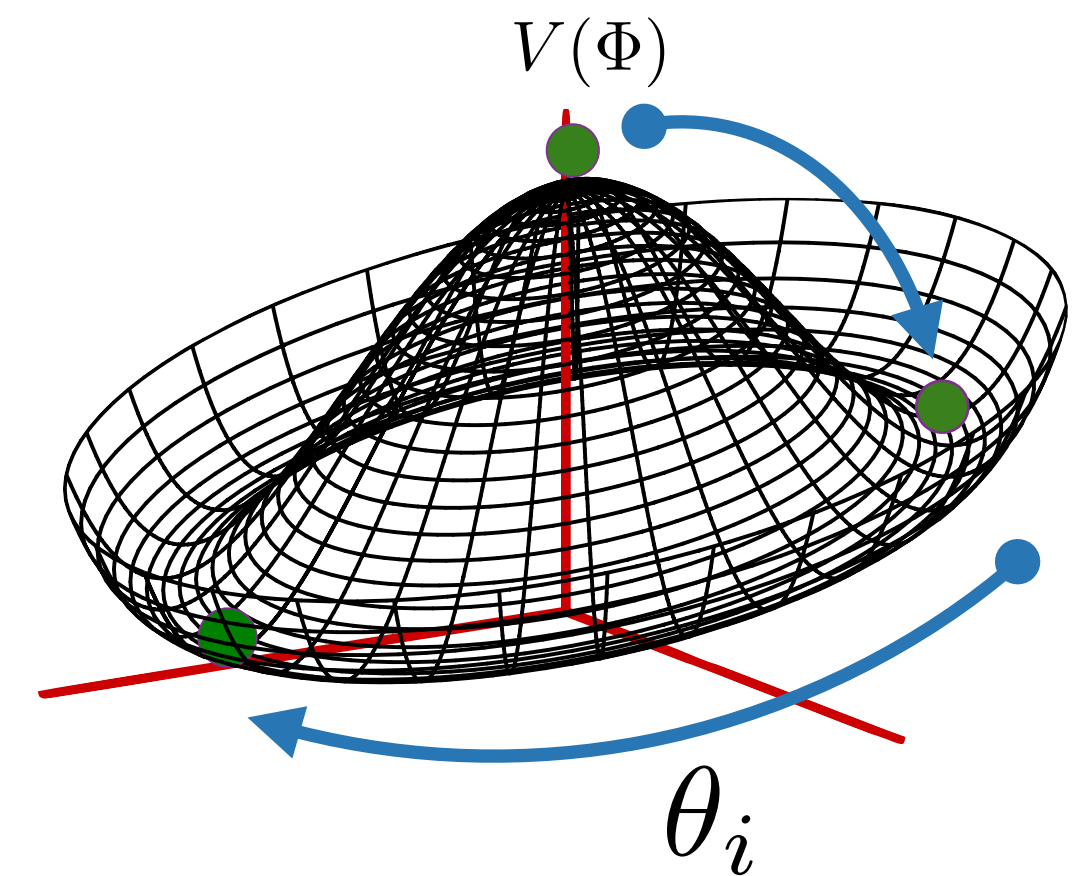
Predicting the mass of the axion with cosmology: Misalignment mechanism

$$\ddot{a} + 3H\dot{a} + \frac{\partial \mathcal{V}(a)}{\partial a} = 0 \quad \text{where,} \quad \mathcal{V}(a) \approx \frac{1}{2} m_a^2 a^2$$



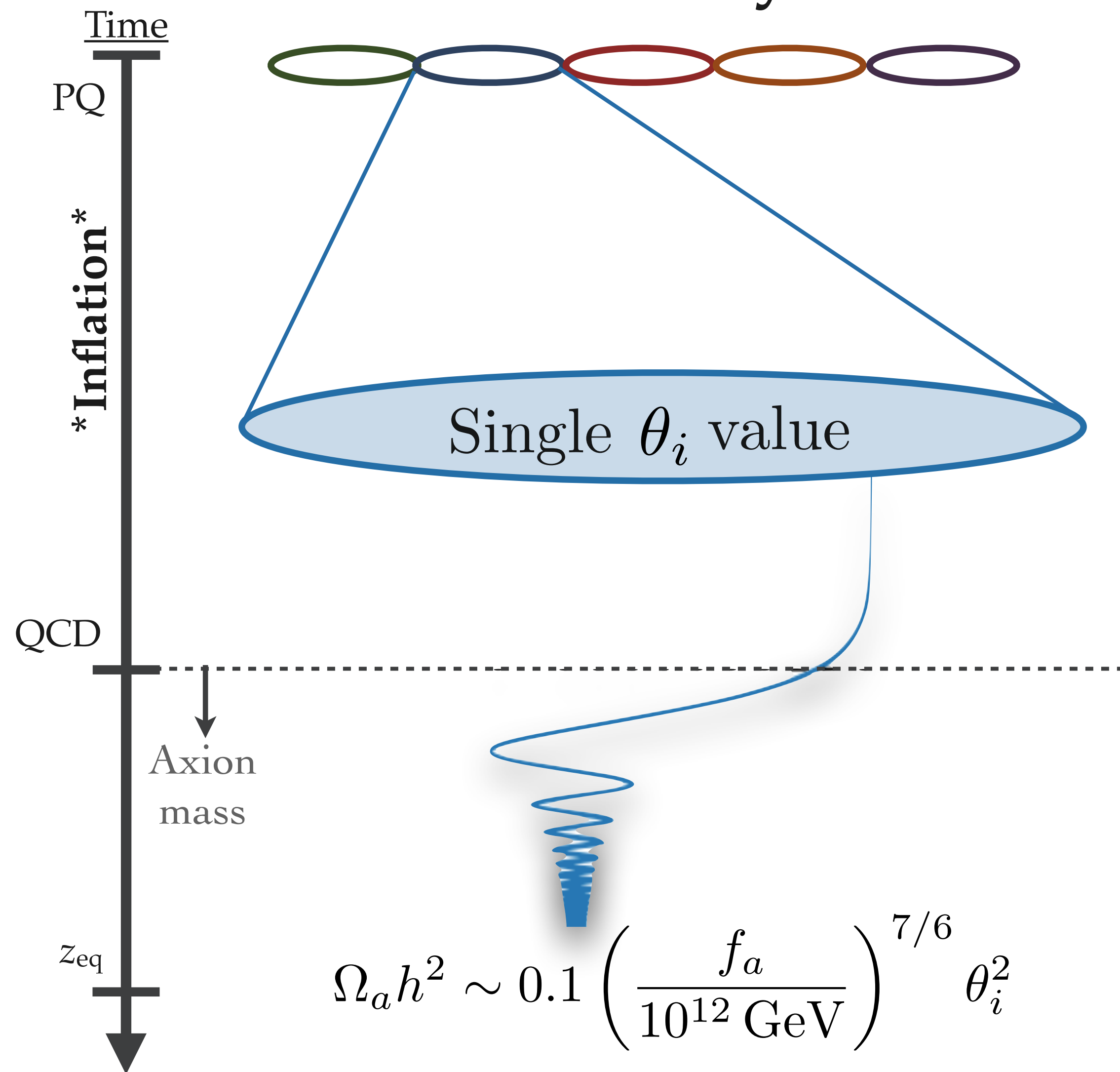
$m_a(t) \approx 3H(t)$
Axion field rolls down
potential

$m_a(t) \gtrsim 3H(t)$
Axion field starts damped
oscillations with frequency $\sim m_a$
 \rightarrow **cold axions dark matter**



Scenario 1:

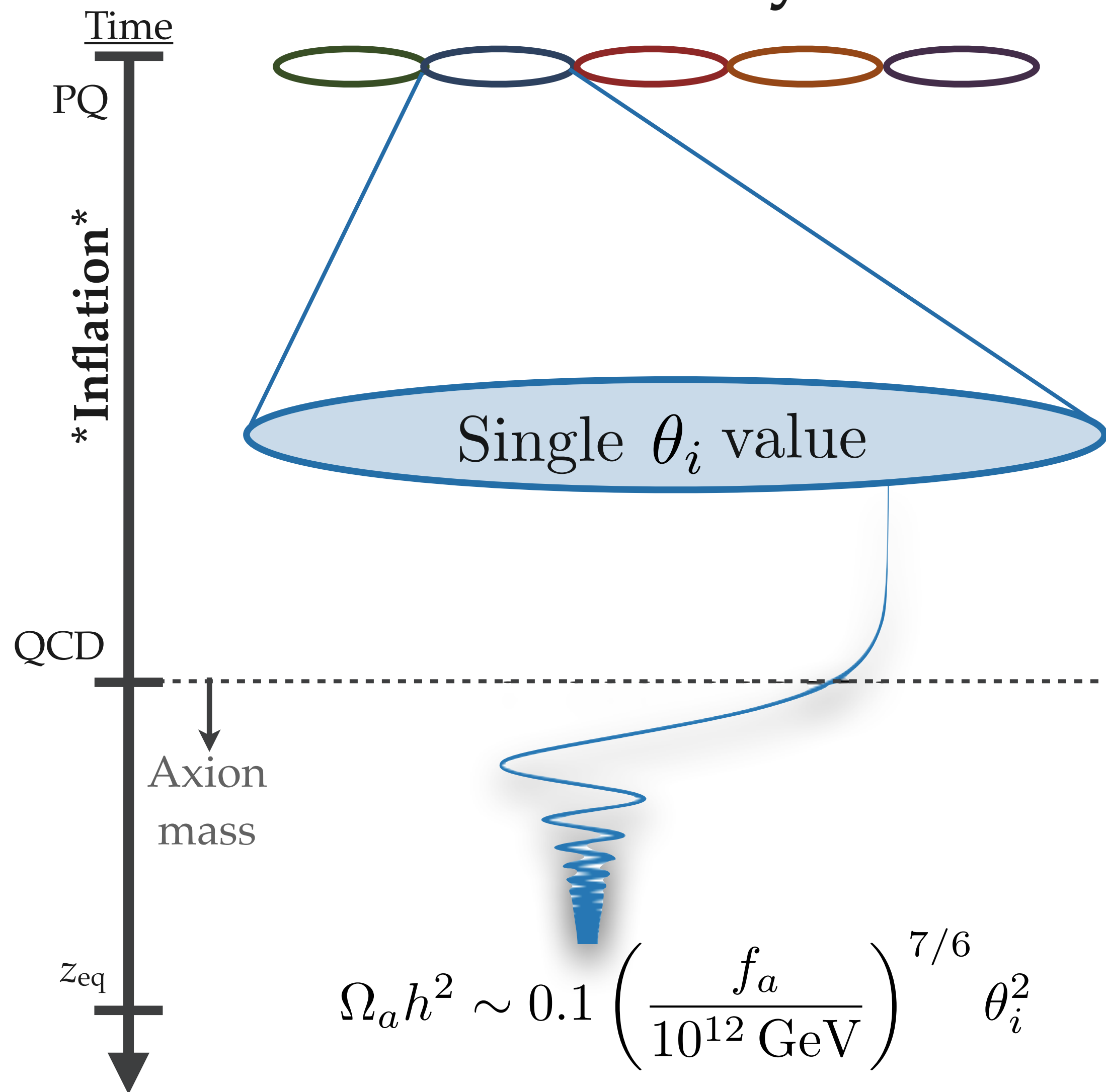
Pre-inflationary axions



**Relic density just depends on single
initial misalignment angle**

Scenario 1:

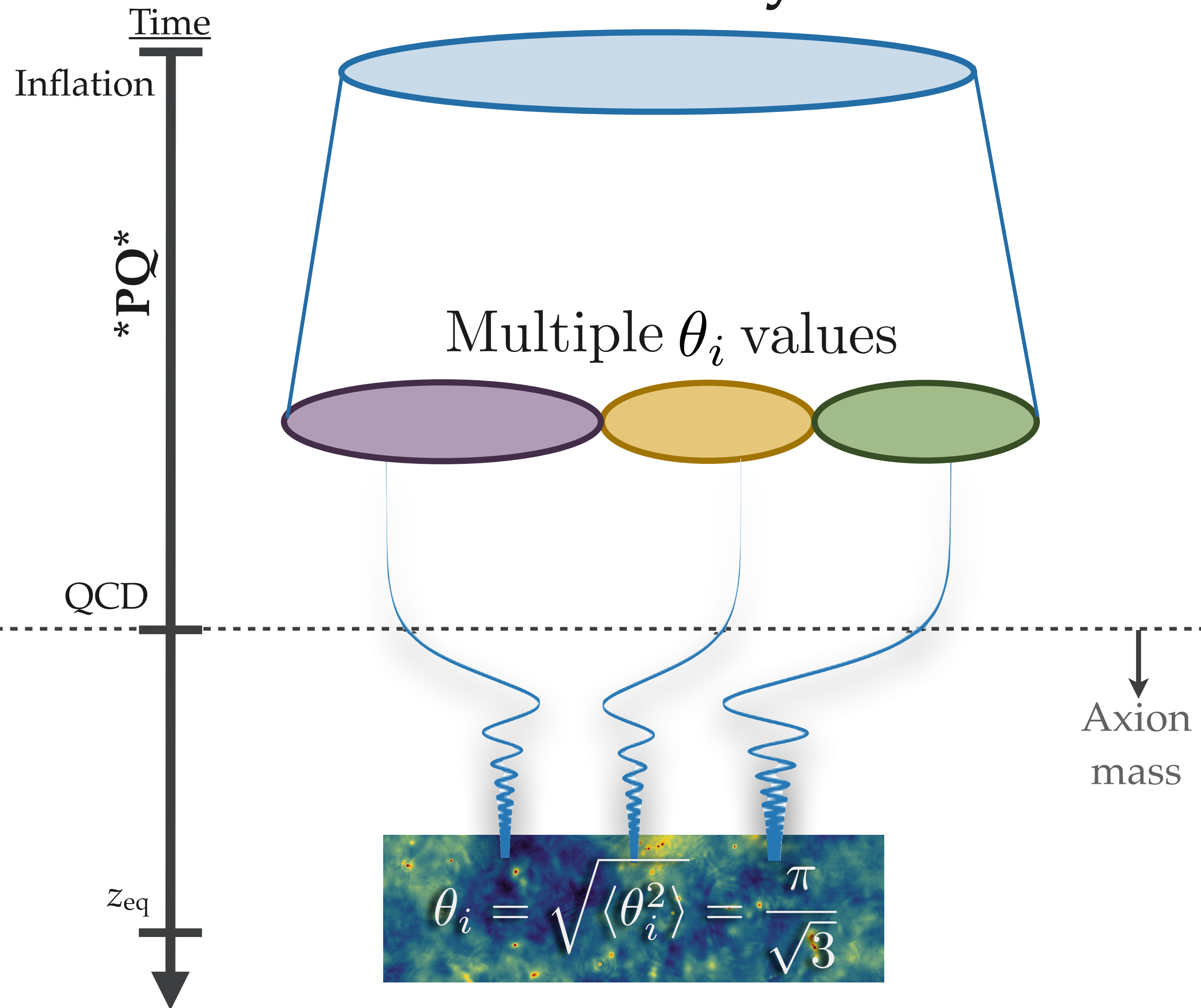
Pre-inflationary axions



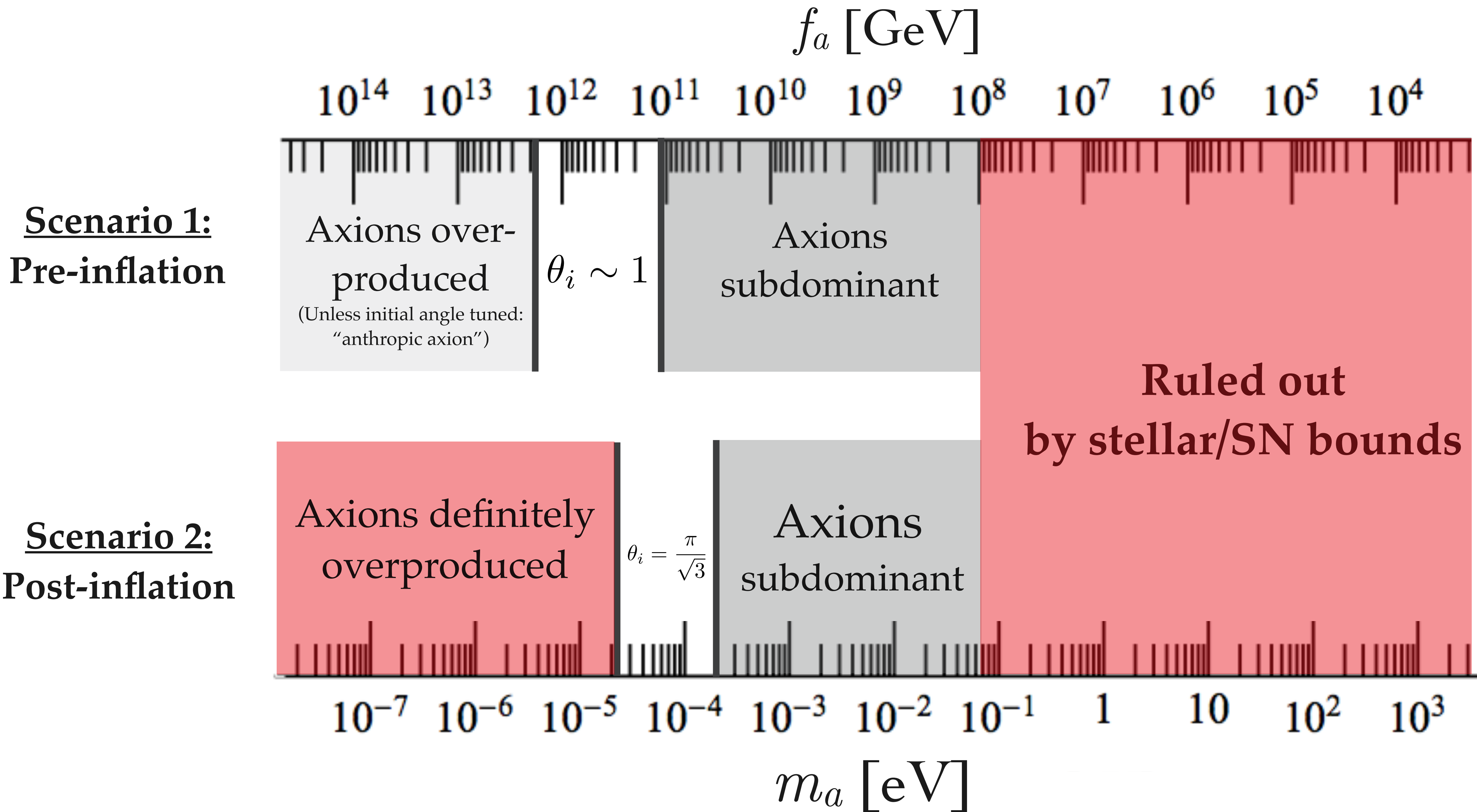
Relic density just depends on single initial misalignment angle

Scenario 2:

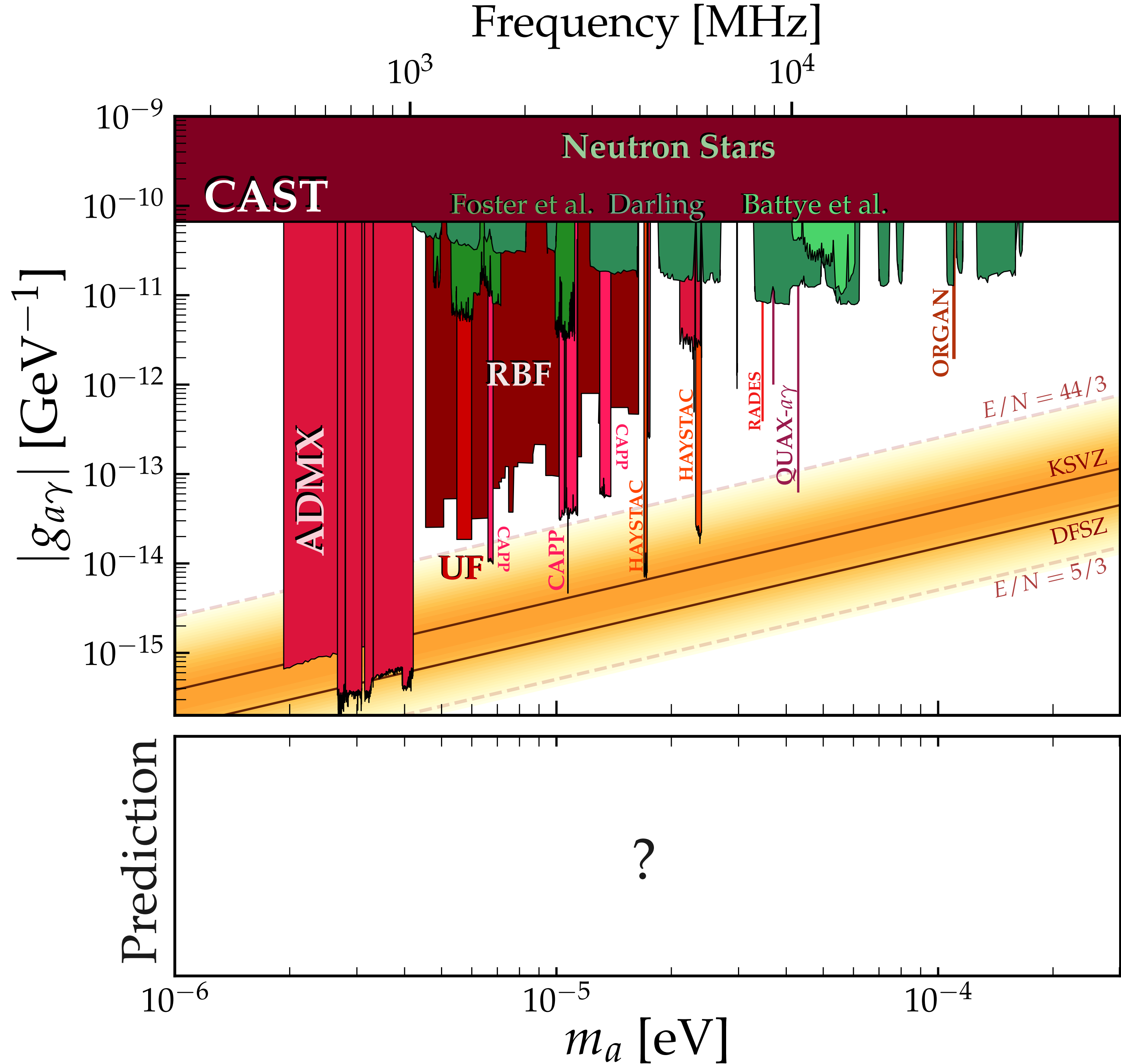
Post-inflationary axions



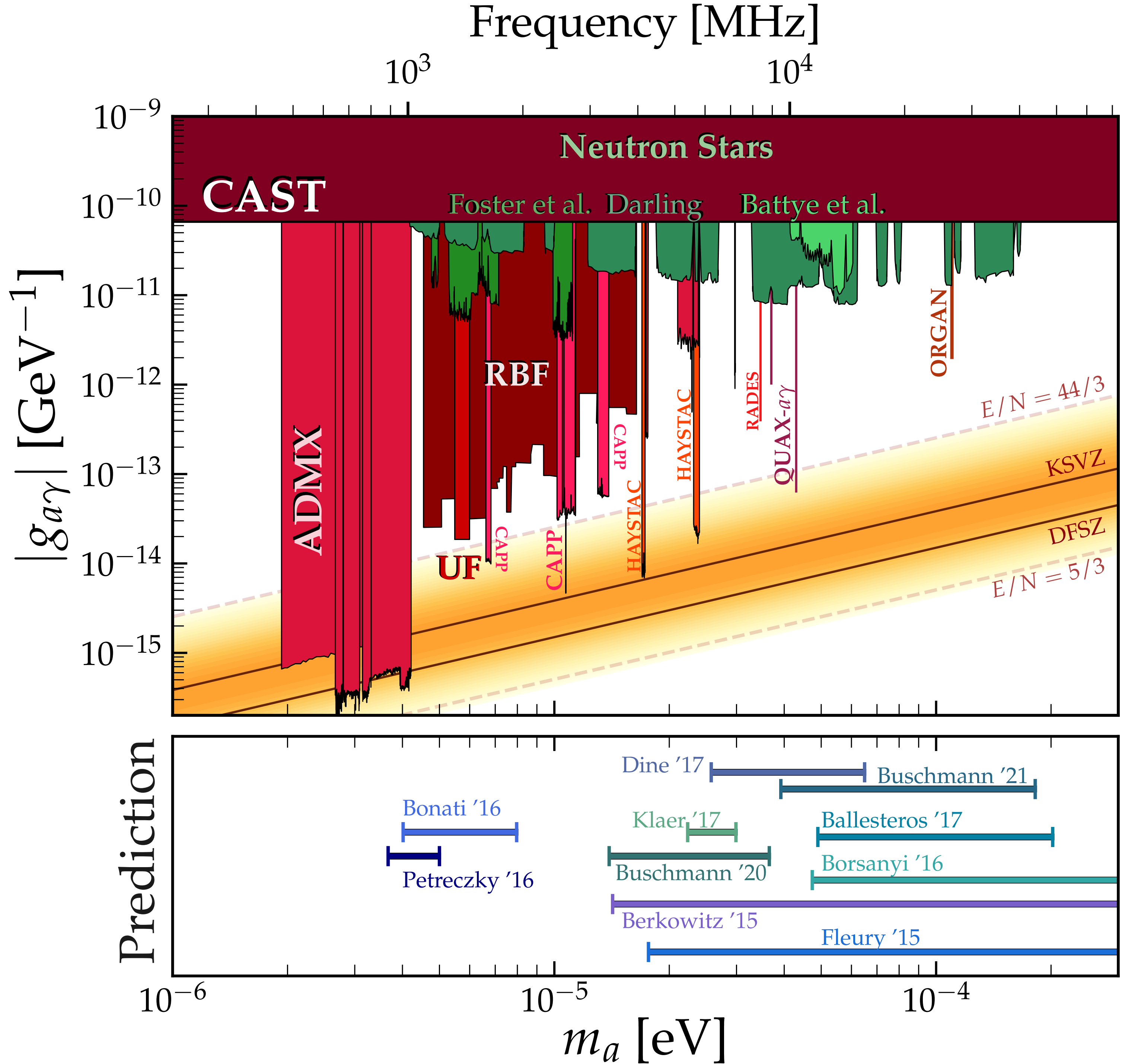
Ensemble of initial misalignment angles
→ Density set by single stochastic average



In principle one can match the abundance of axions to $\Omega h^2 = 0.12$ and find the m_a that matches:

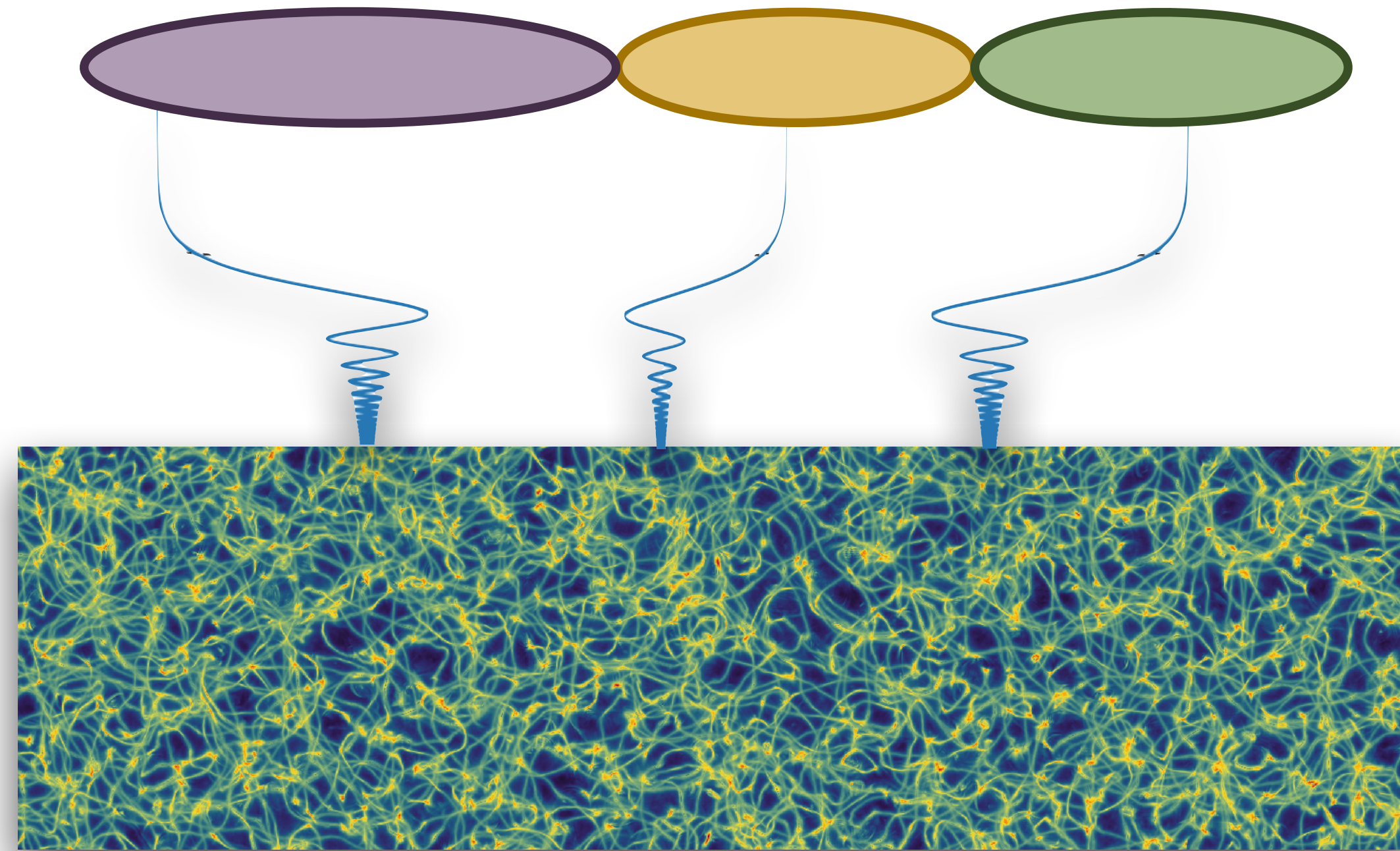


In principle one can match the abundance of axions to $\Omega h^2 = 0.12$ and find the m_a that matches:



Why no agreement?

Complication in the post-inflationary scenario: topological defects



After U(1) spontaneous breaking (at $T < f_a$):

⇒ **Cosmic strings** from axion field winding around 2π

After explicit breaking (at $T \lesssim \Lambda_{\text{QCD}}$)

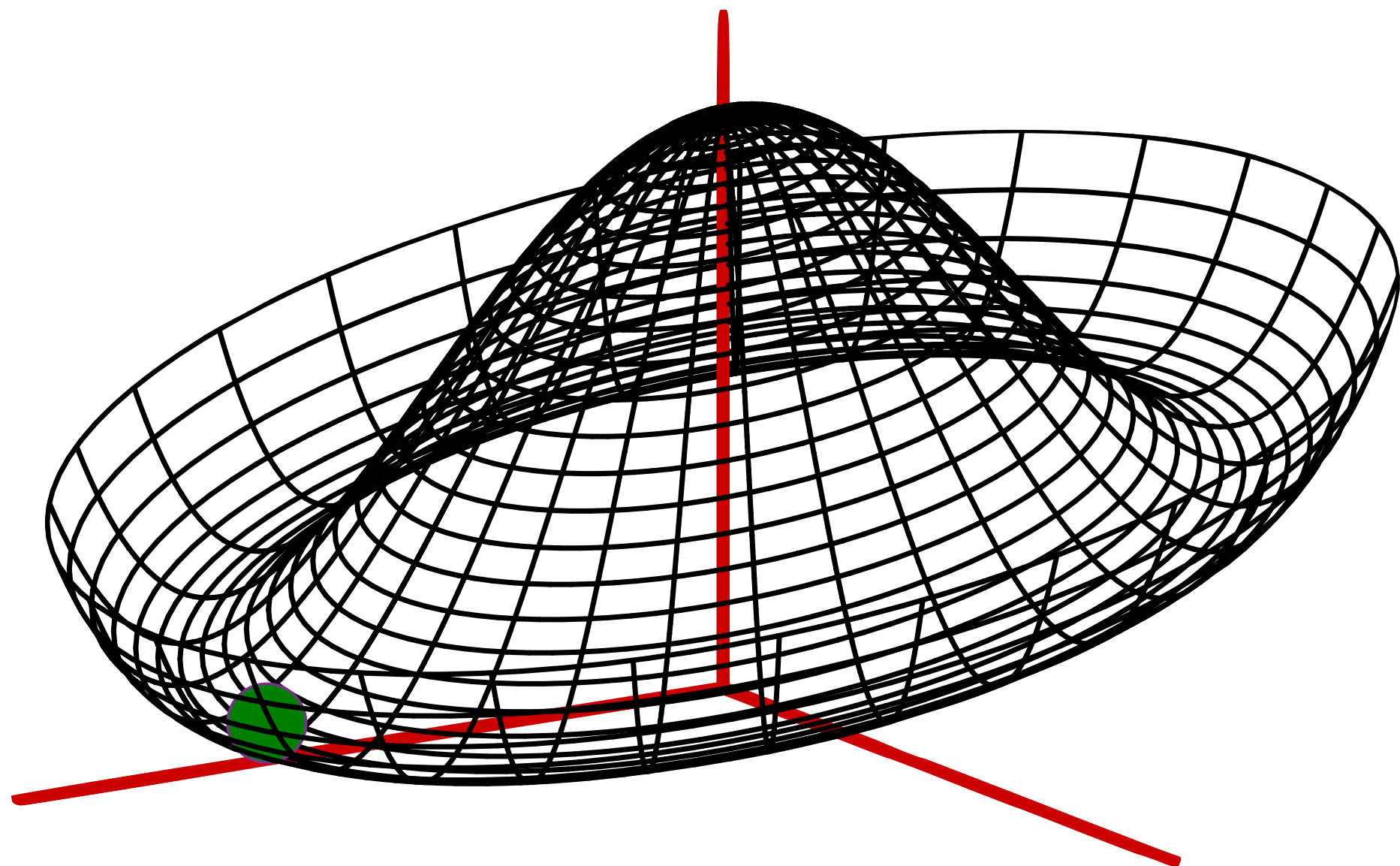
⇒ **Domain walls** between axion field at true/false vacuum (0 and π)

Numerical simulations

Evolve complex PQ scalar in expanding universe under potential:

$$V(\phi) = V_{\text{PQ}}(|\phi|) + V_{\text{QCD}}(\theta) = \frac{\lambda_\phi}{8} (|\phi|^2 - f_a^2)^2 + \chi(T)(1 - \cos \arg \phi)$$

$$\phi(\mathbf{x}) \sim |\phi(\mathbf{x})| e^{i\theta(\mathbf{x})}$$

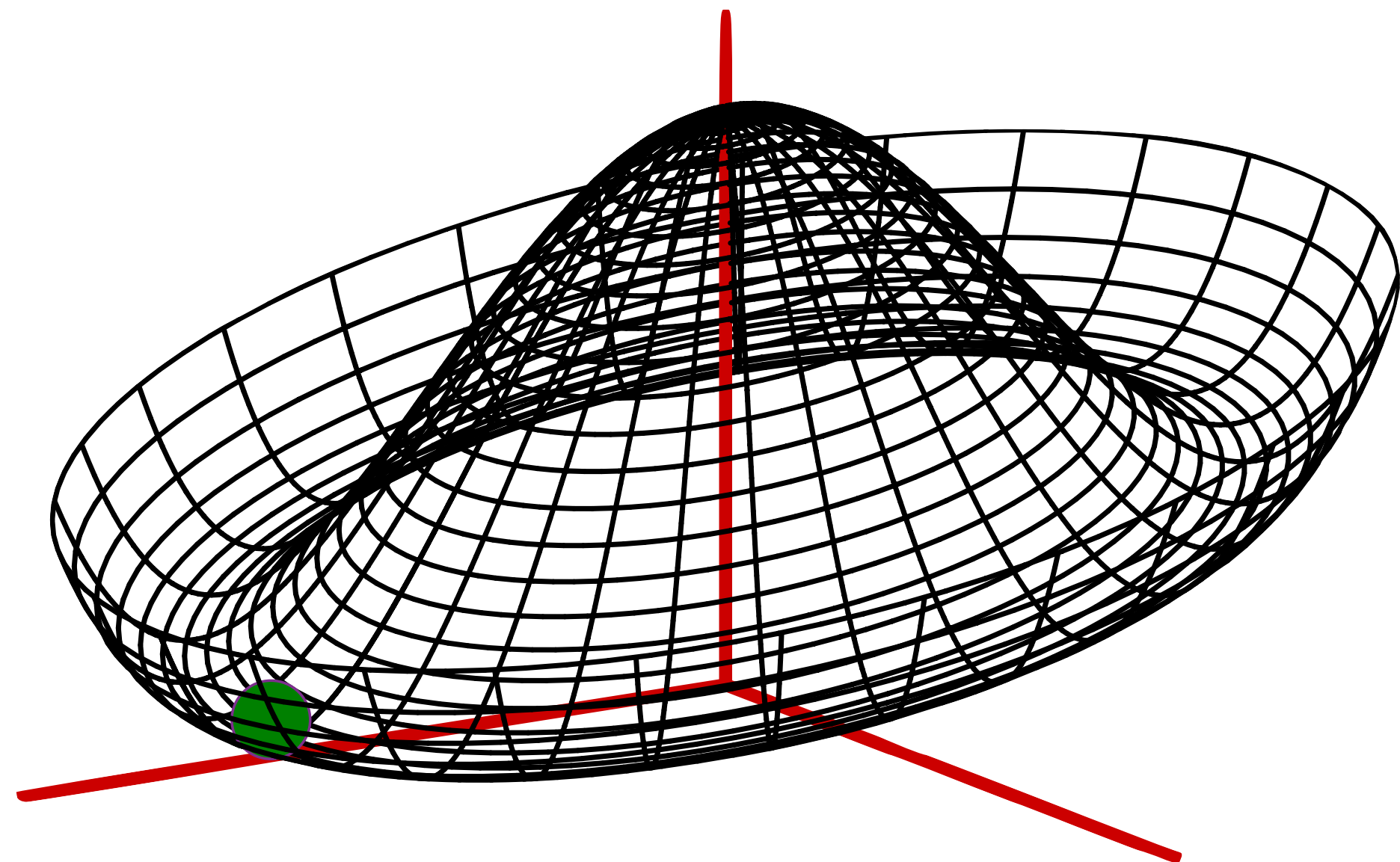


Numerical simulations

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$$|\phi(\mathbf{x})|$$

Radial dof: "saxion"

Sets string width.

Mass =

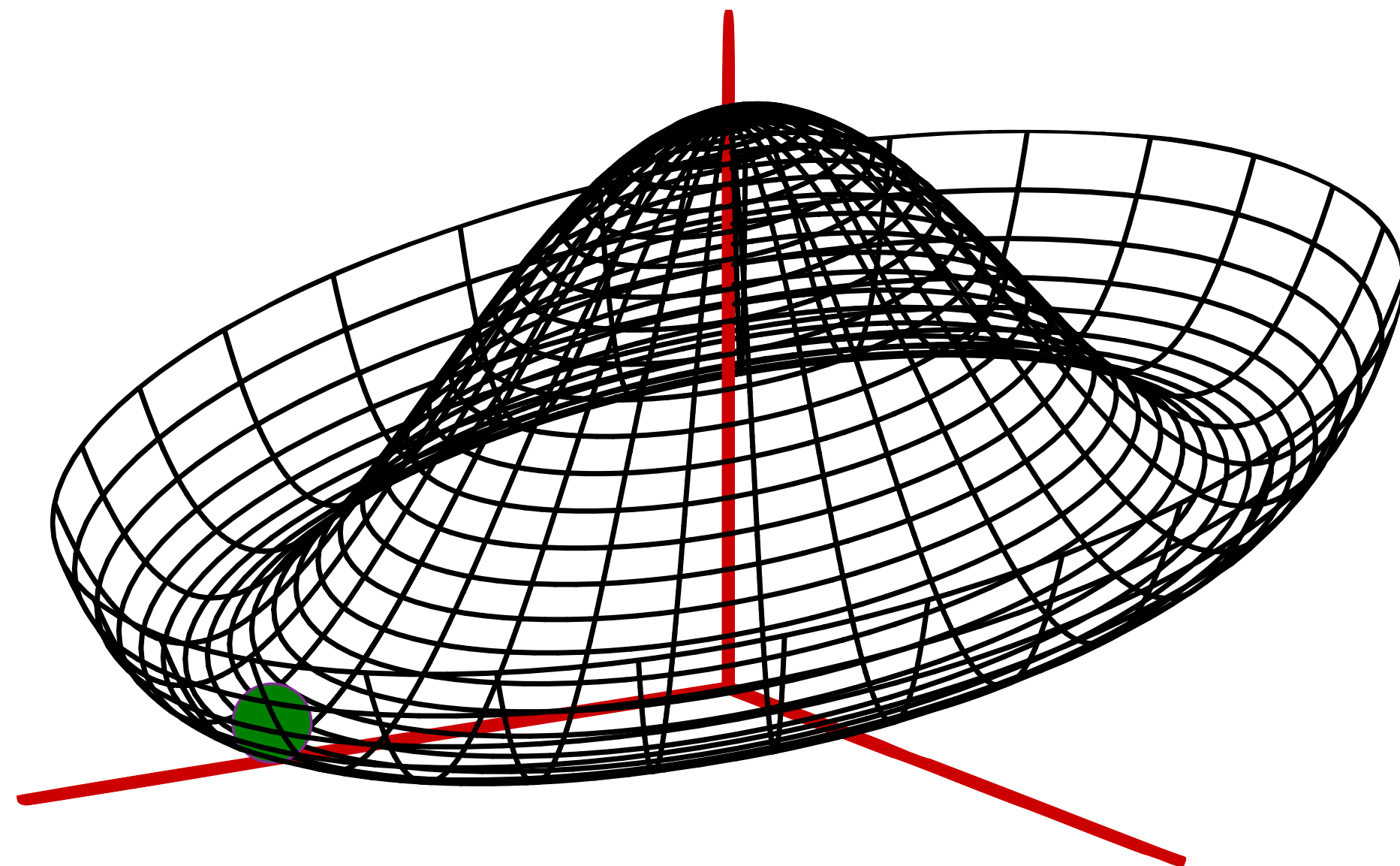
$$m_s = \sqrt{\lambda_\phi} f_a$$

Numerical simulations

Evolve complex PQ scalar in expanding universe under potential:

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$$\phi(\mathbf{x}) \sim |\phi(\mathbf{x})| e^{i\theta(\mathbf{x})}$$



$$|\phi(\mathbf{x})|$$

Radial dof: "saxion"

Sets string width.

Mass =

$$m_s = \sqrt{\lambda_\phi} f_a$$

$$\theta(\mathbf{x}) = a(\mathbf{x})/f_a$$

Angular dof: "axion"

Sets domain walls

Temperature dependent mass:

$$m_a^2(T) = \frac{\chi_0}{f_a} \left(\frac{150 \text{ MeV}}{T} \right)^n$$

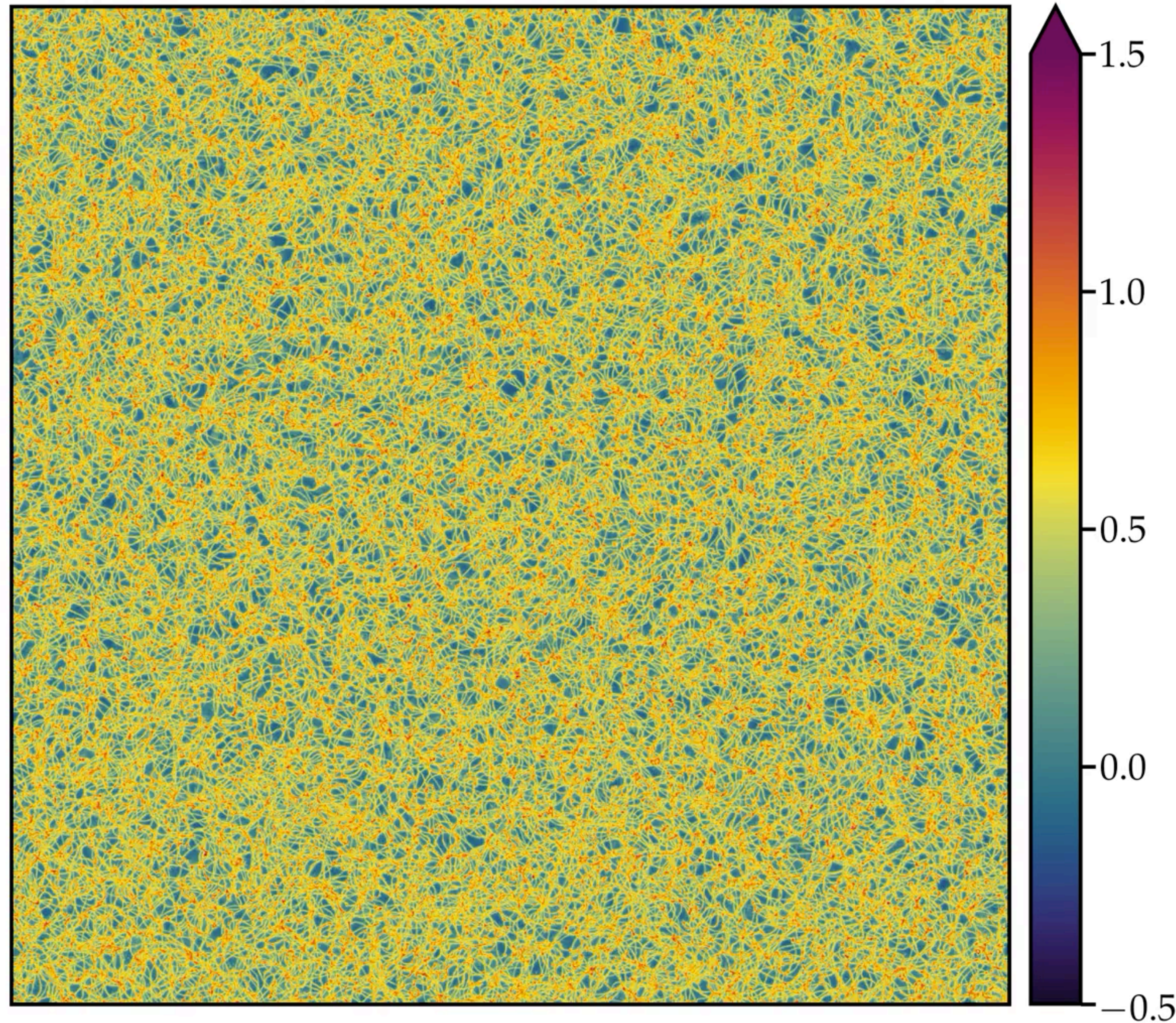
$\chi_0 \approx (76 \text{ MeV})^4$ and $n \sim 6 - 8$
can be calculated via e.g lattice

QCD [1606.07494]

Evolution of the axion field in the post-inflationary scenario

$\tau = 0.5$

$\log_{10}(\rho_a/\bar{\rho}_a)$

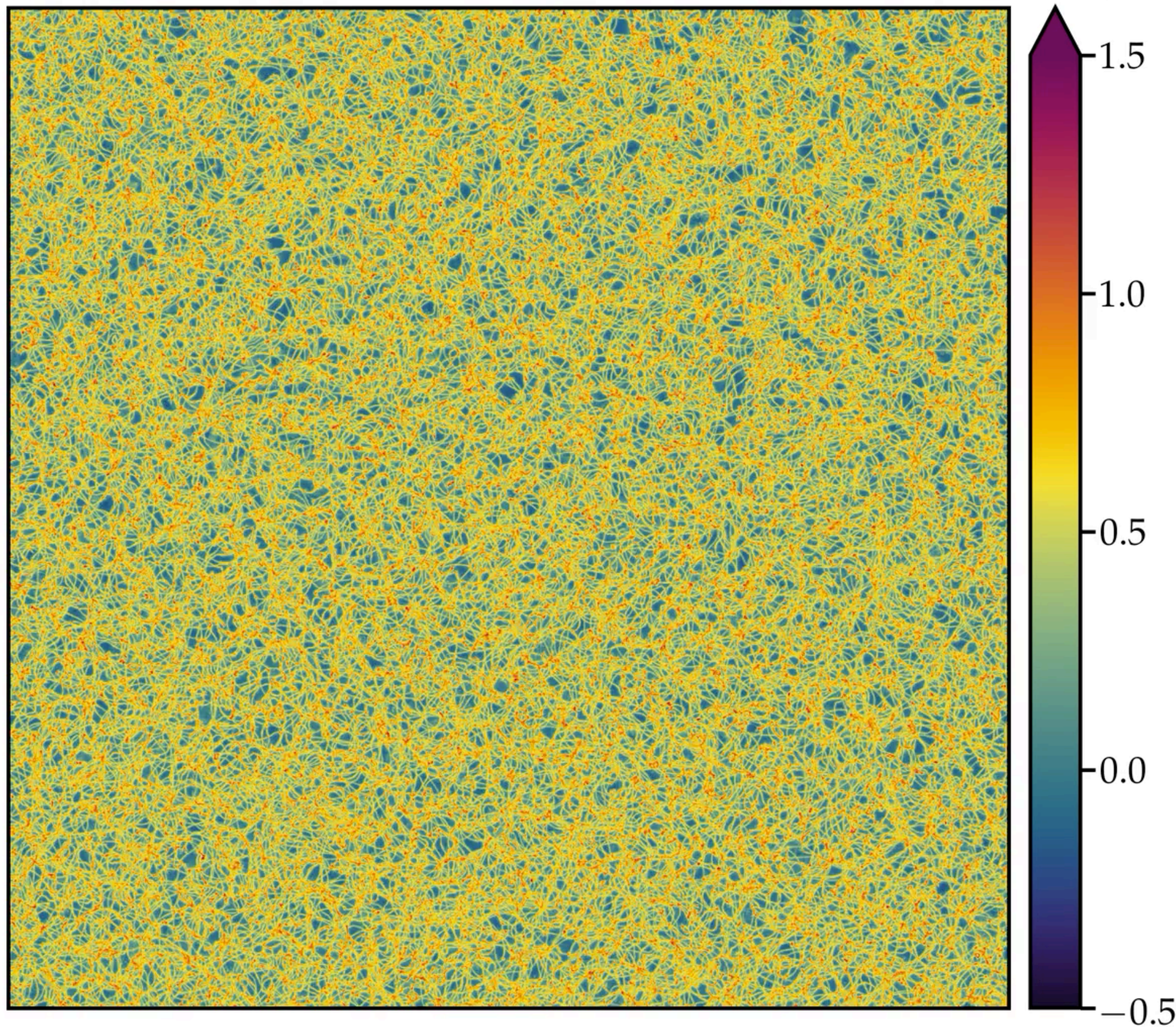


(movie)

Evolution of the axion field in the post-inflationary scenario

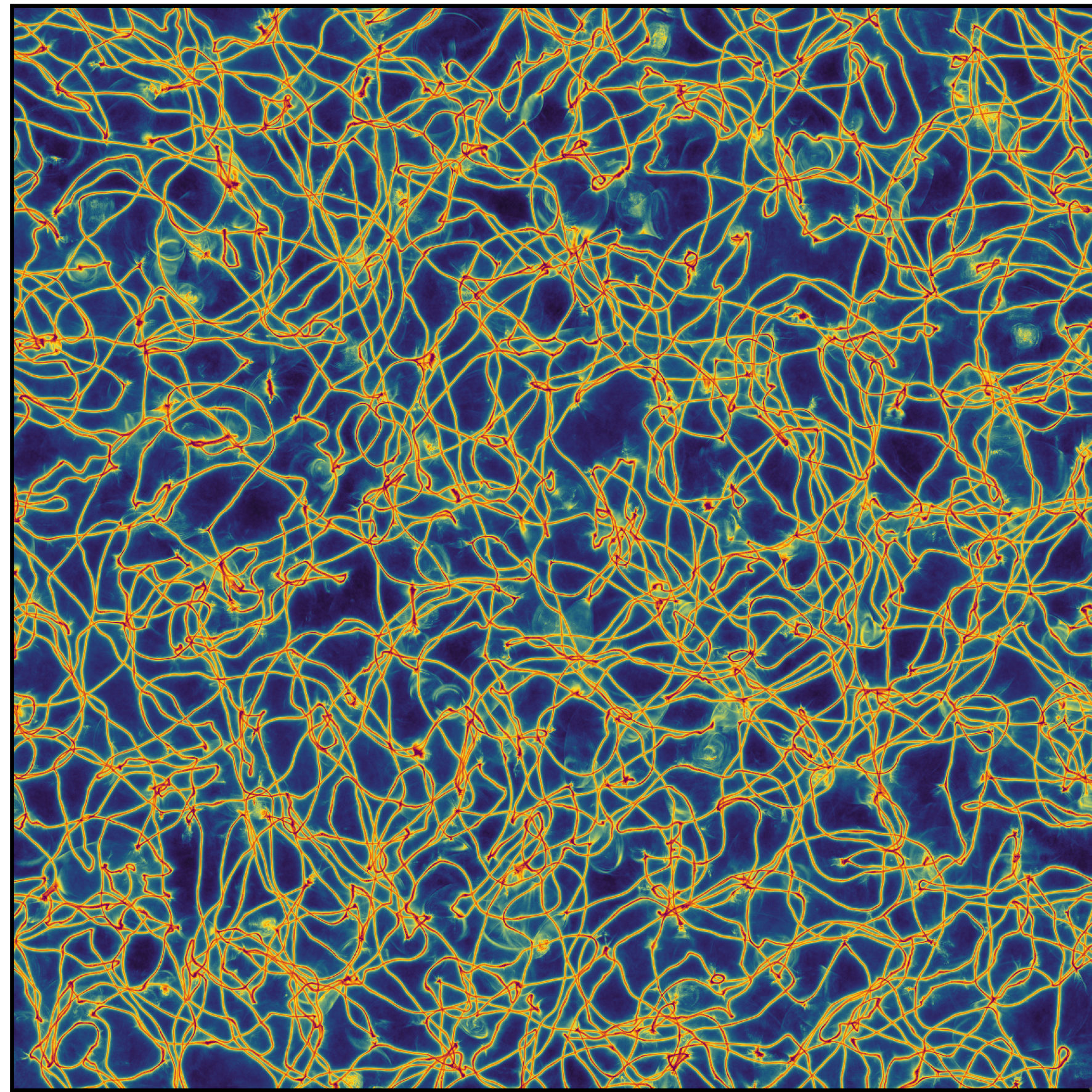
$\tau = 0.5$

$\log_{10}(\rho_a/\bar{\rho}_a)$



(movie)

Evolution of the axion field in the post-inflationary scenario



PQ

String network scaling

QCD

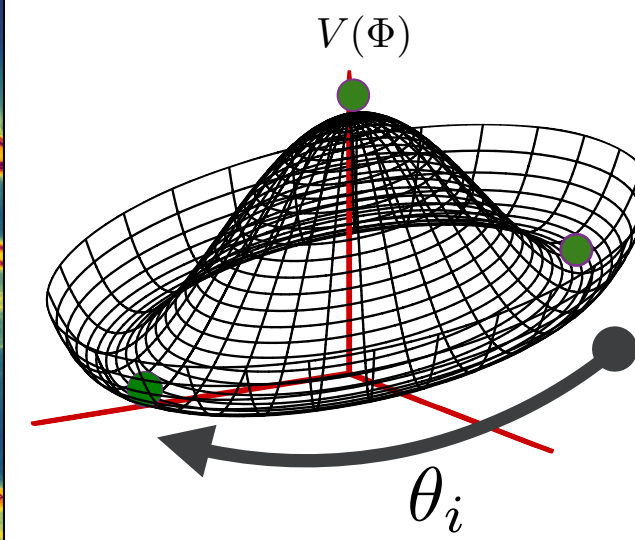
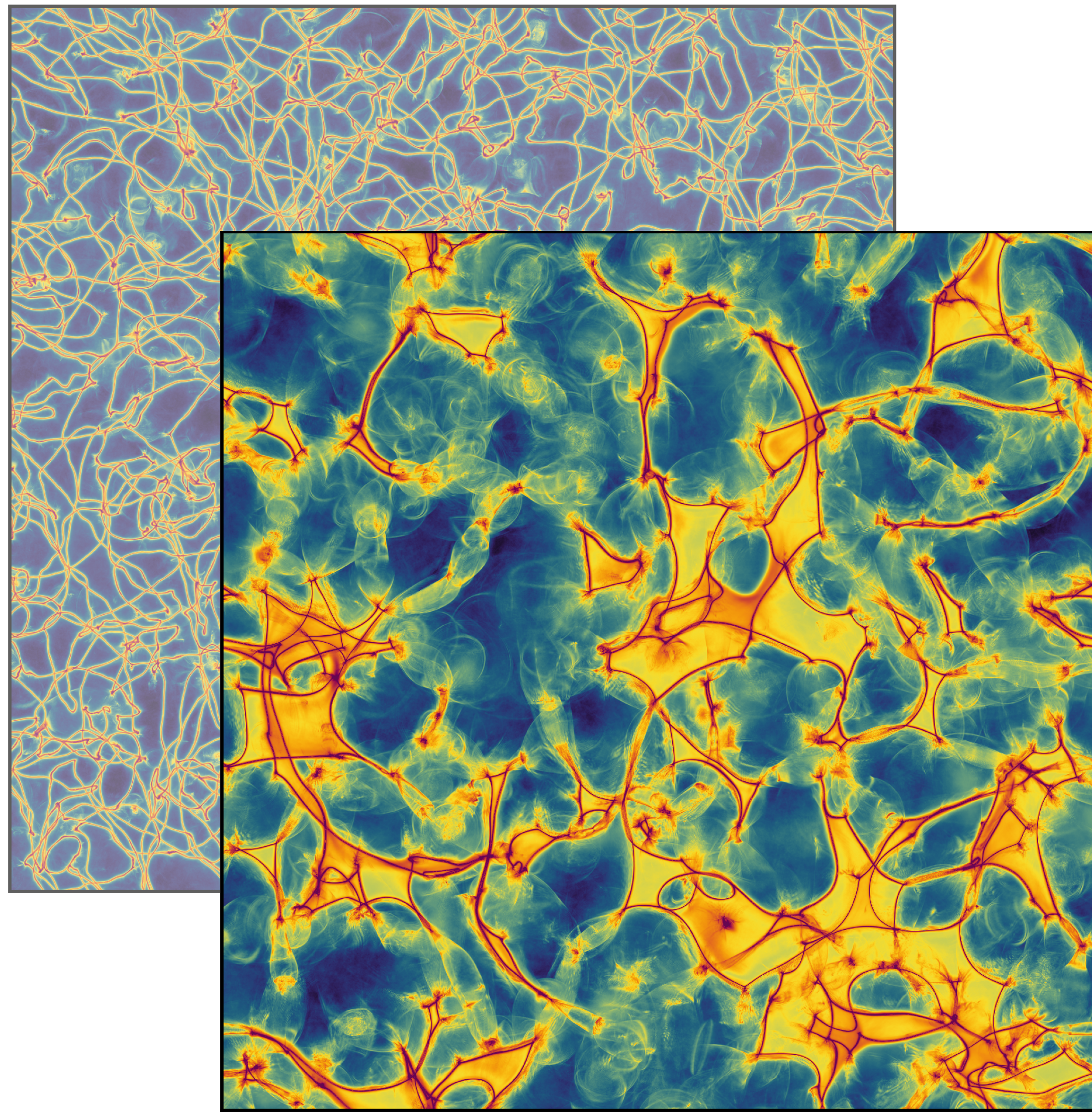
Domain walls attached to strings
→ network collapses

z_{eq}

Inhomogeneous distribution of
axions free streams

Gravitational collapse into
miniclusters and halos

Evolution of the axion field in the post-inflationary scenario



PQ

String network scaling

QCD

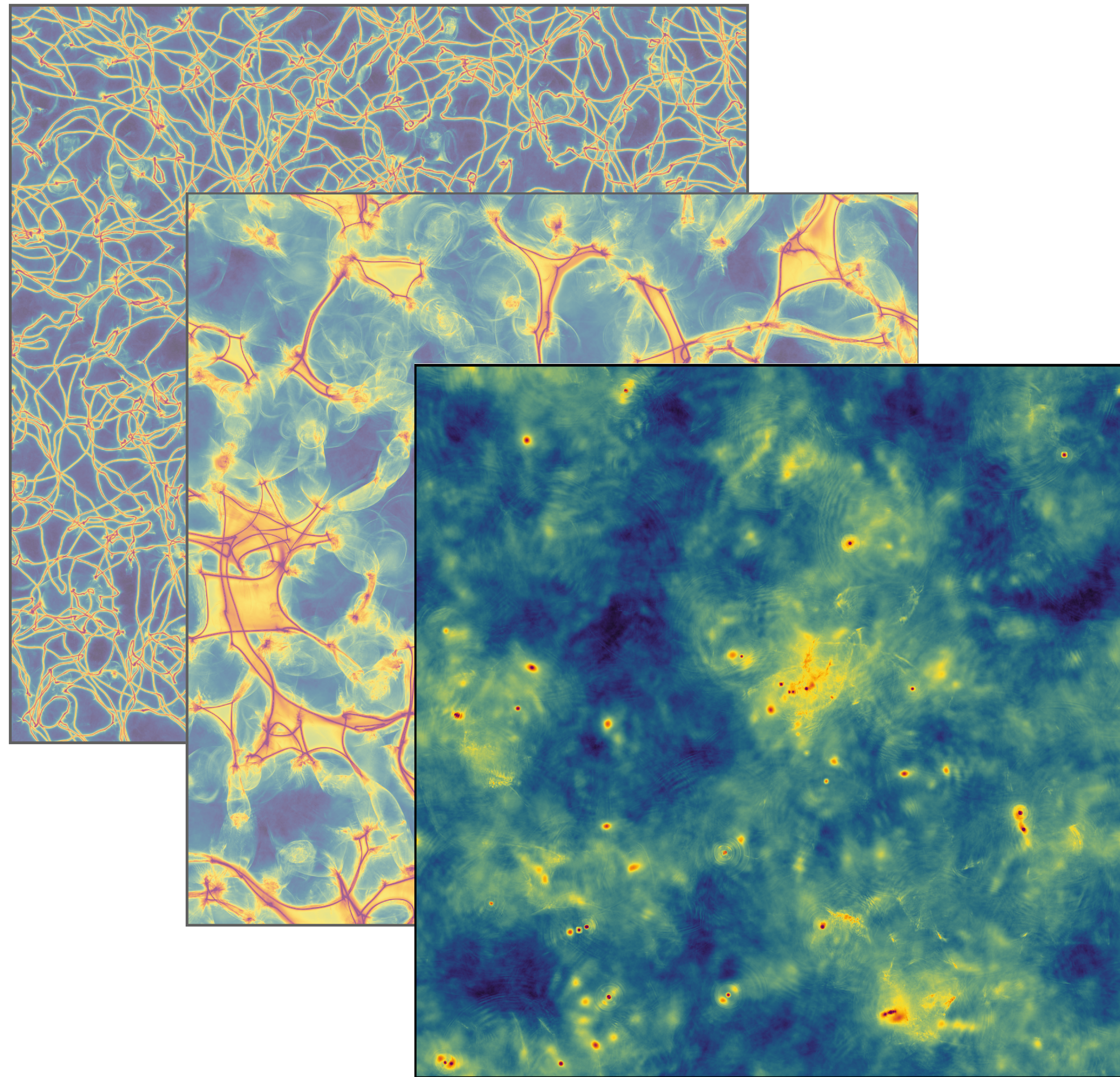
Domain walls attached to strings
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Evolution of the axion field in the post-inflationary scenario



PQ

String network scaling

QCD

Domain walls attached to strings
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z_{eq}

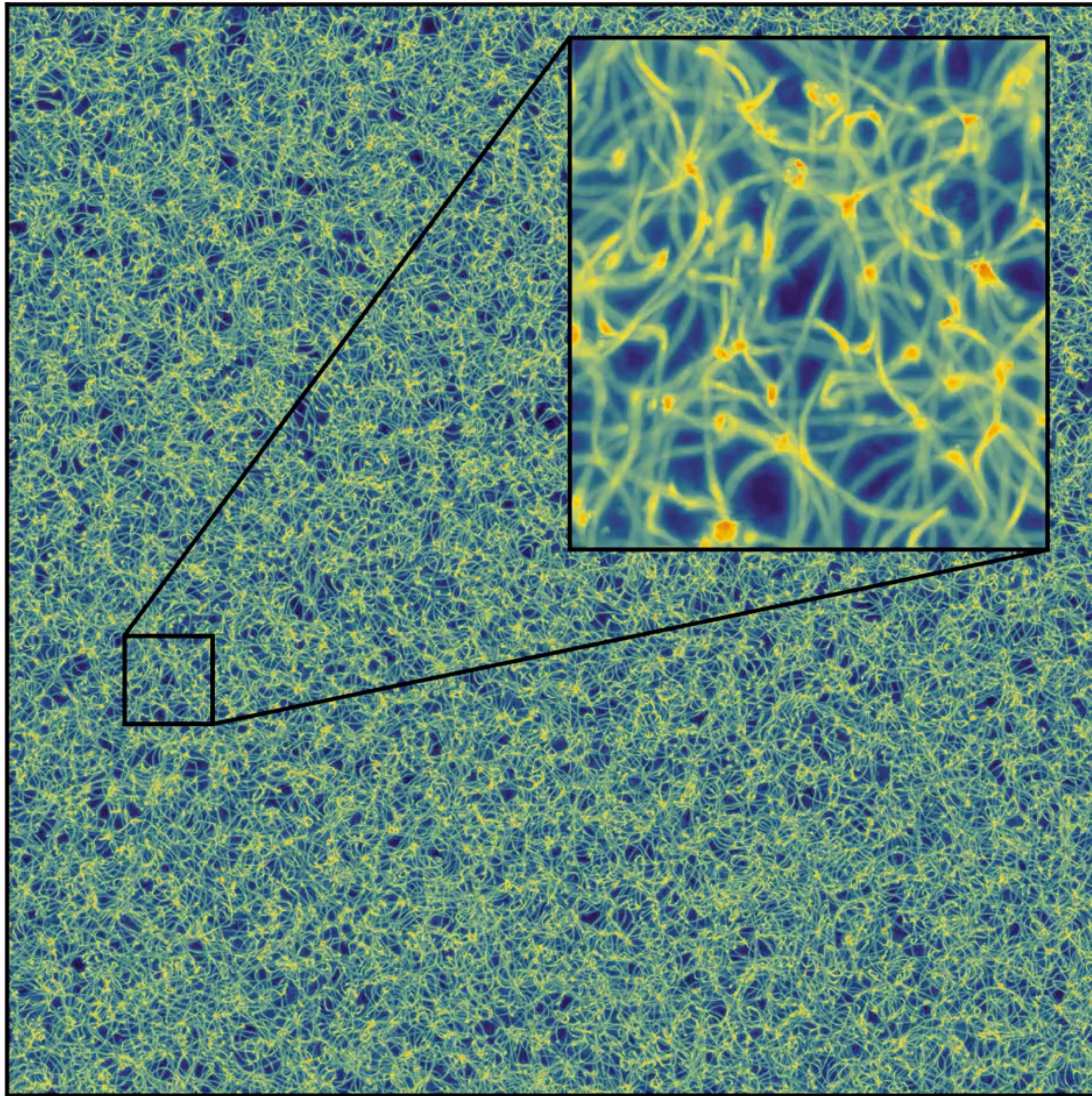
Inhomogeneous distribution of
axions free streams until non-
relativistic

Seeds of structure
gravitationally collapse
into miniclusters and halos

Evolution of the axion field in the post-inflationary scenario

When the axion mass grows quickly with temperature (e.g. $m_a^2 \propto T^{-6.68}$) large numbers of high density oscillating lumps are seeded towards the end of the simulation with sizes $\lambda \sim m_a^{-1}$

→ “Axitons”



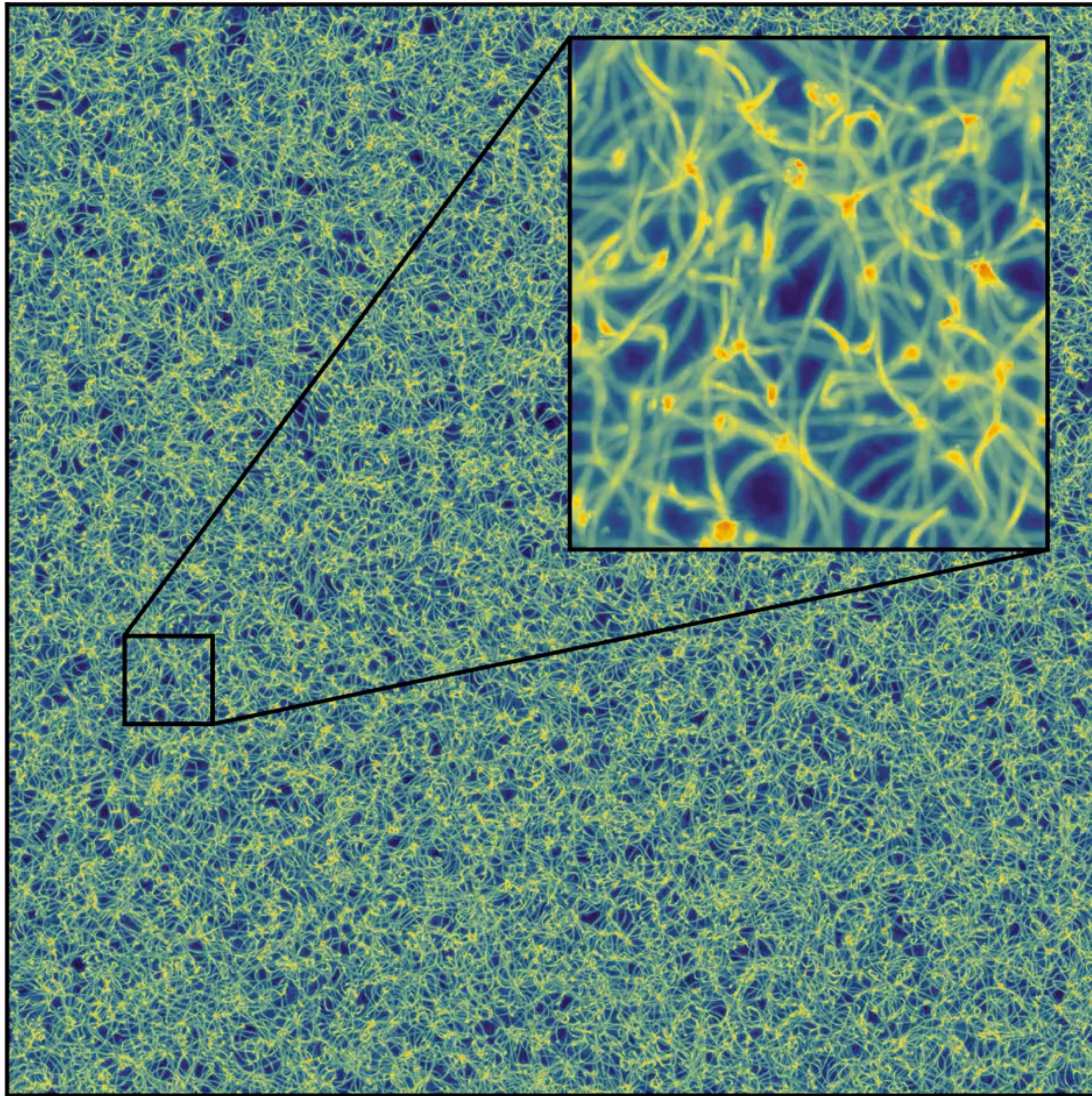
(Movie)

CAJO, Pierobon, Redondo, Wong [in prep.]

Evolution of the axion field in the post-inflationary scenario

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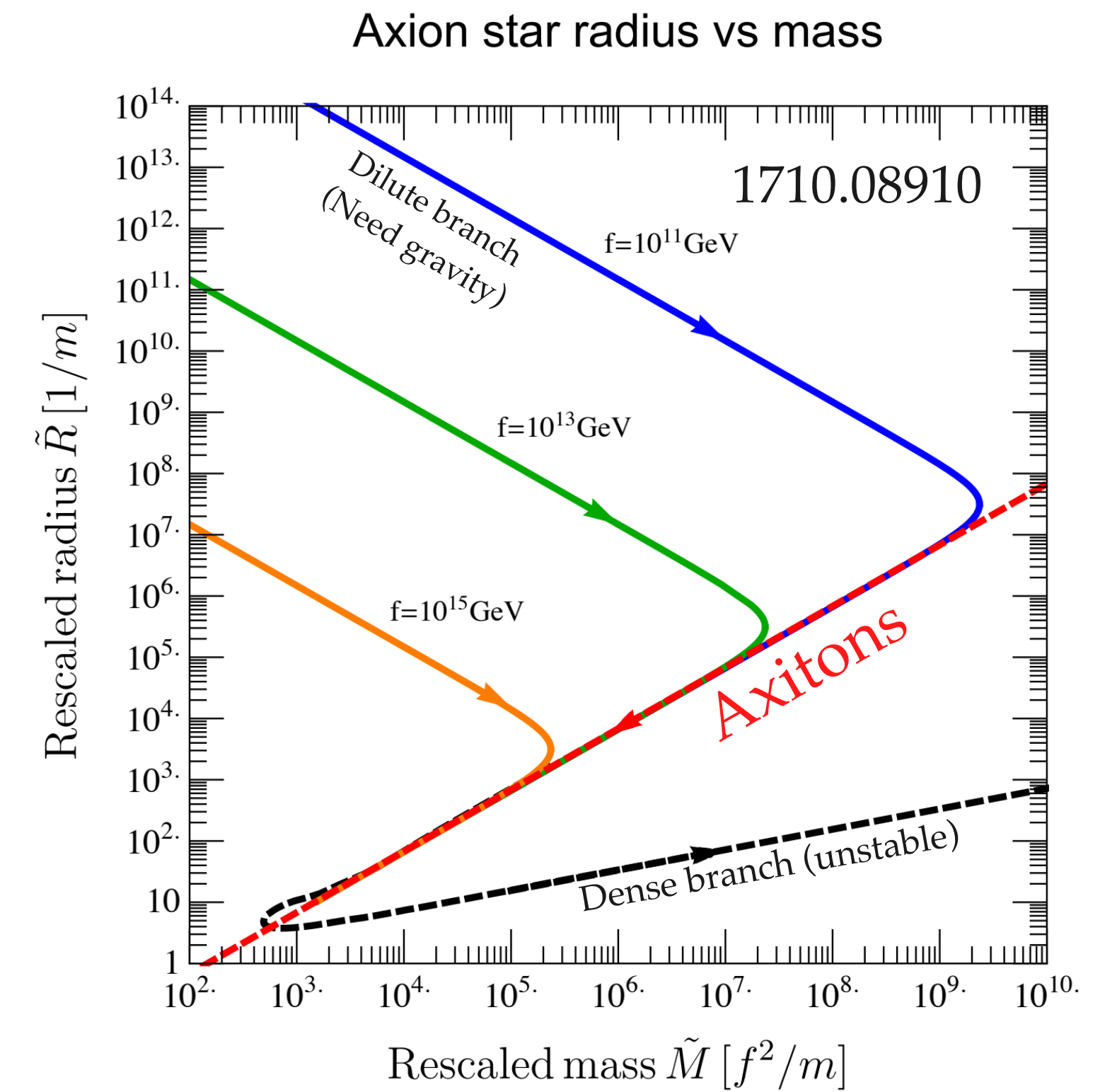


(Movie)

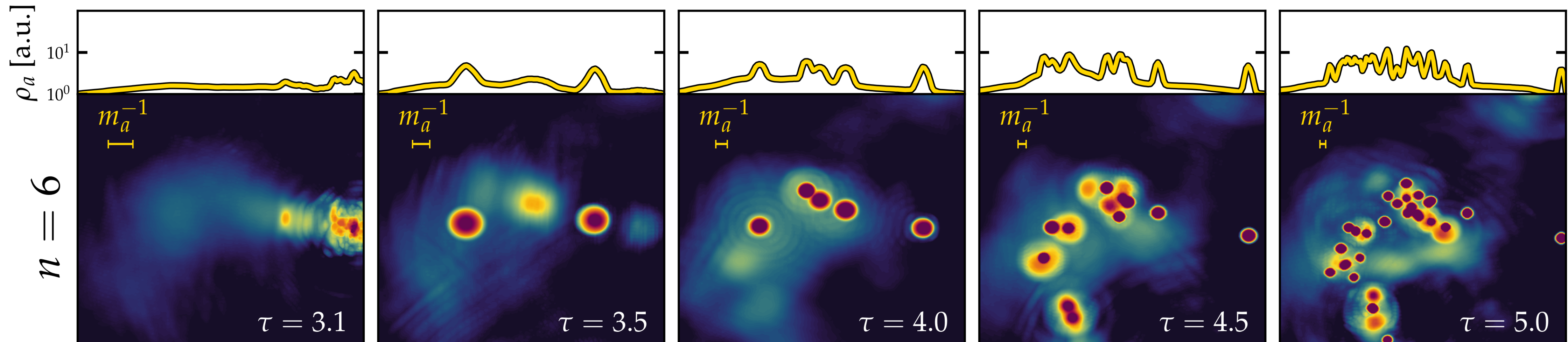
CAJO, Pierobon, Redondo, Wong [in prep.]

Axions (aka oscillons)

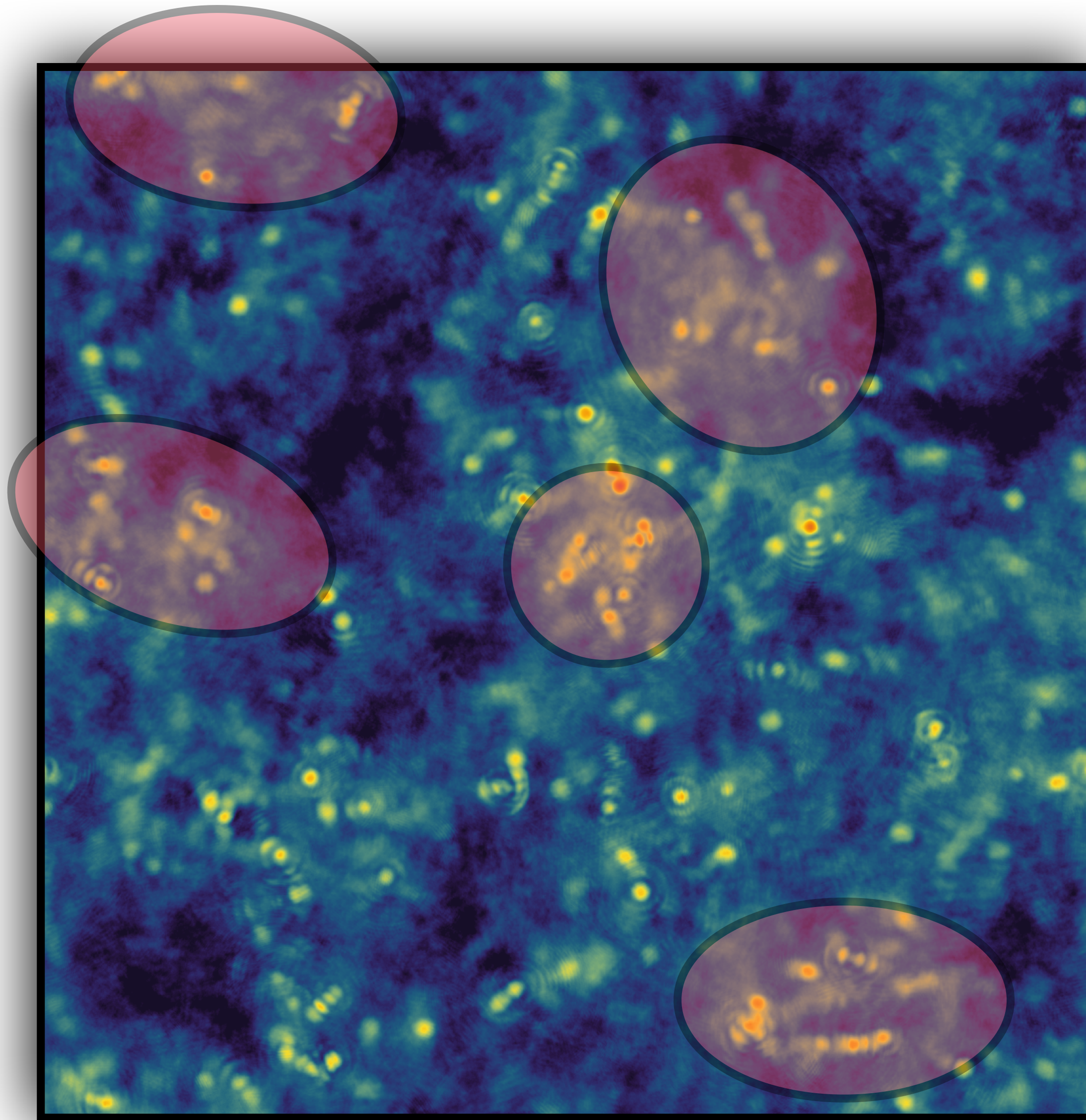
- Pseudo-breathing solutions of the Sine-Gordon equation with a growing mass $m_a^2(T) \propto T^{-n}$
- Can also be thought of as the unstable transition between dilute and dense axion stars
- Radiate away axions but eventually will dissipate once the axion mass reaches its present day value



Mass increasing with time \longrightarrow



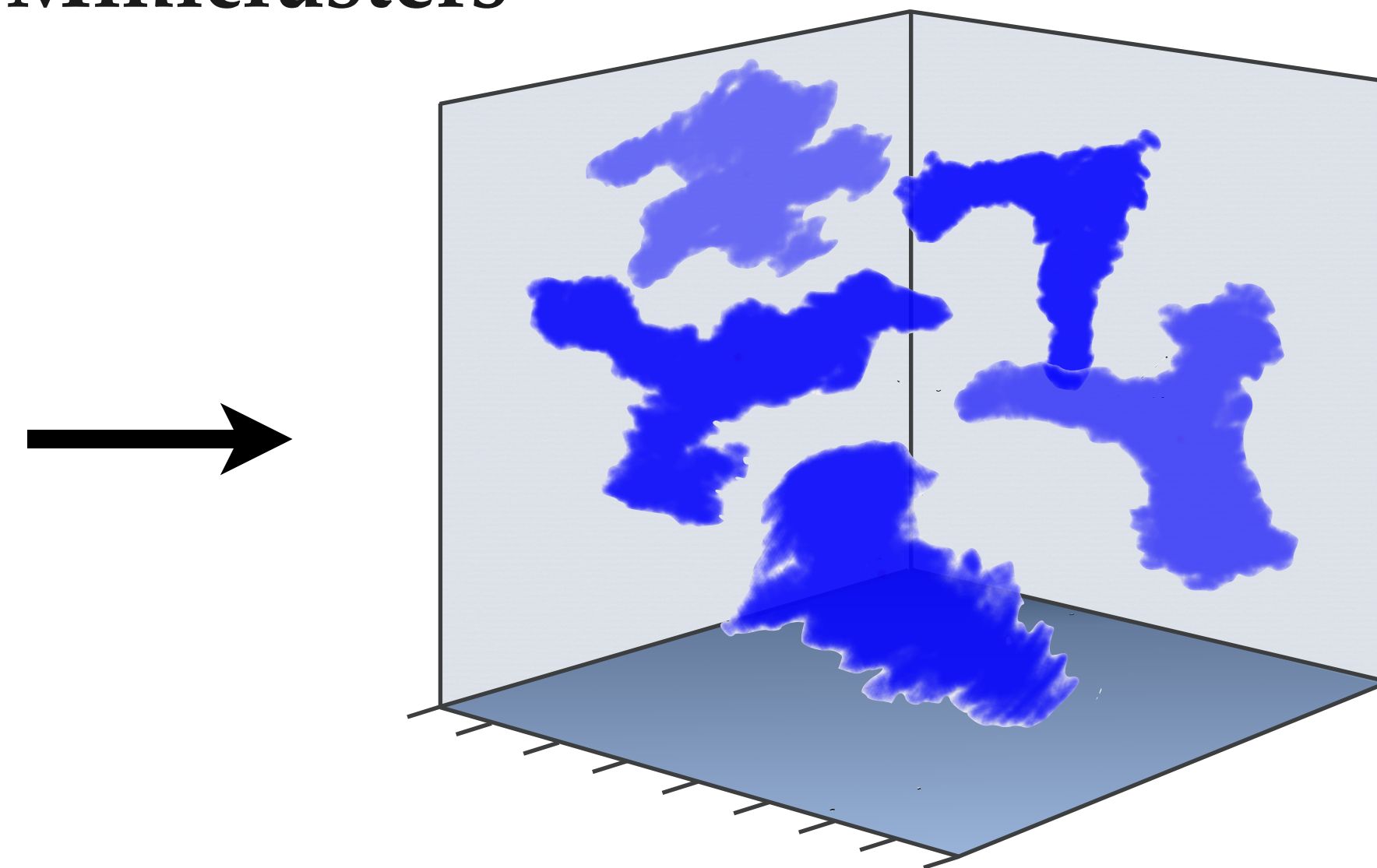
What next? → Gravity



Around $z_{\text{eq}} \sim 4000$, field is inhomogeneities on small scales $L \sim 0.1$ pc

→ Leads to gravitational collapse of structures much earlier conventional thermal CDM

→ **Miniclusters**



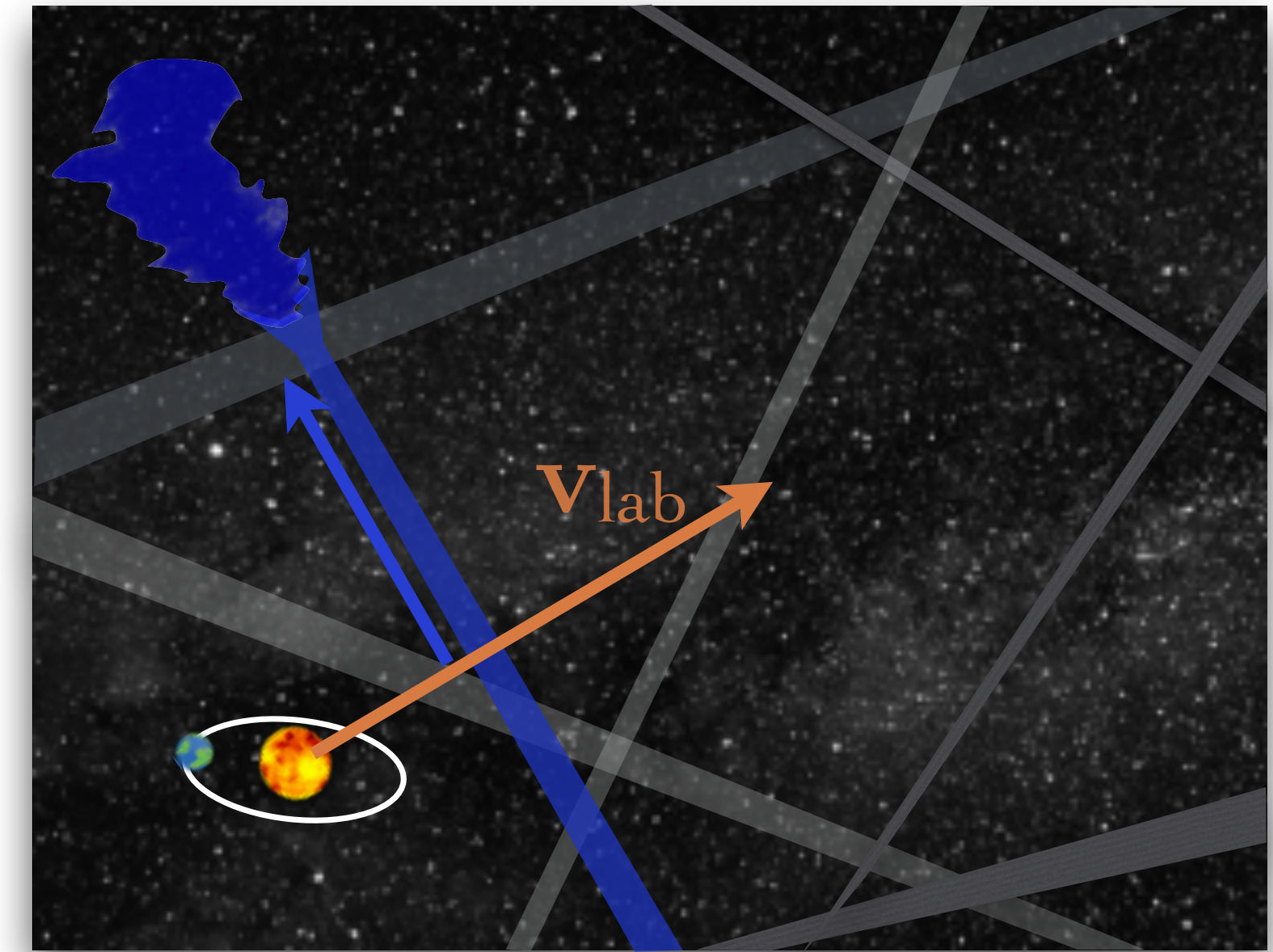
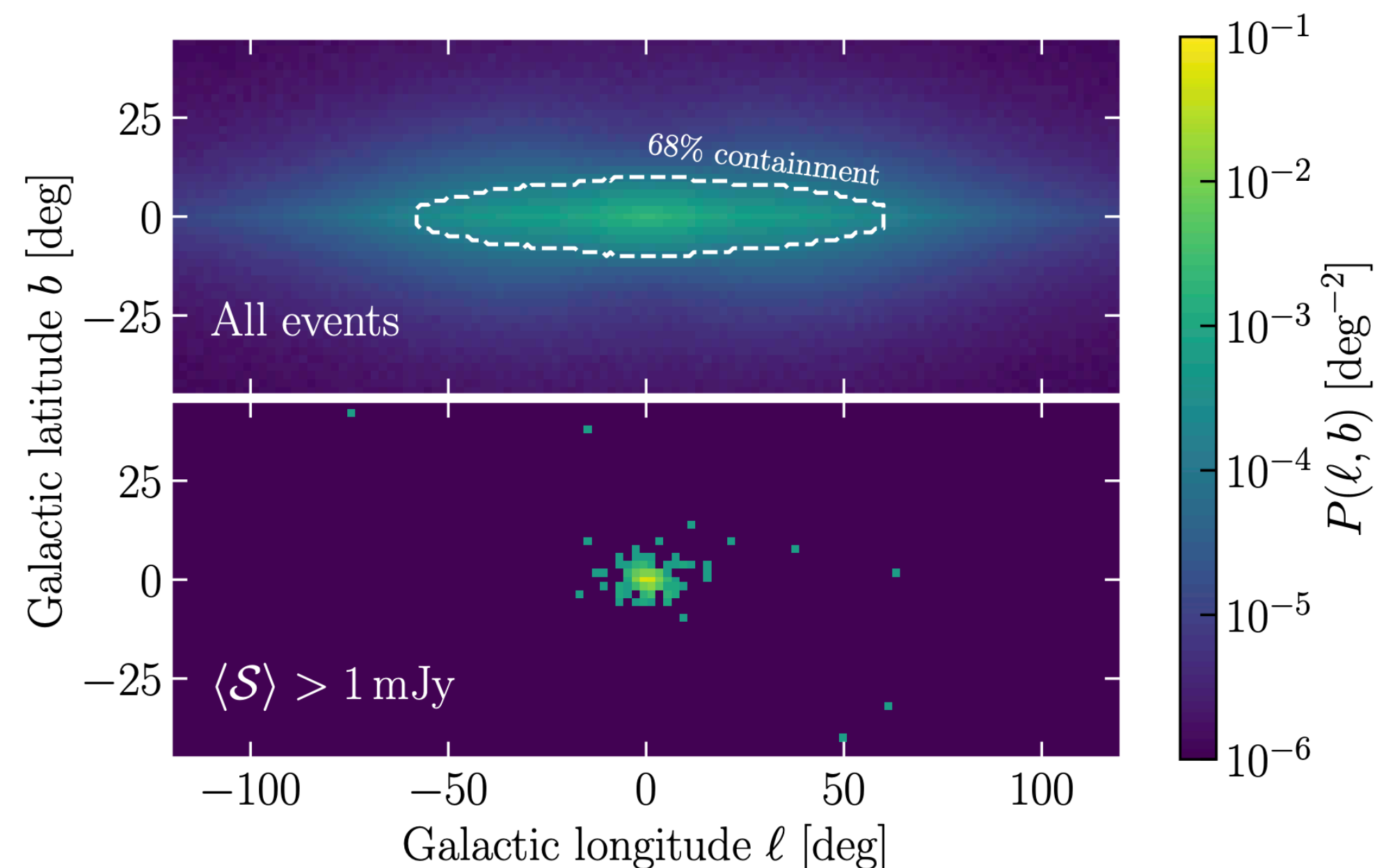
$$M_{\text{mc}} \sim 10^{-12} M_{\odot} \quad \rho_{\text{mc}} \sim 10^4 \text{ GeV cm}^3$$

(For QCD axion, ALP miniclusters will be fluffier)

Outstanding problem 1: the DM distribution

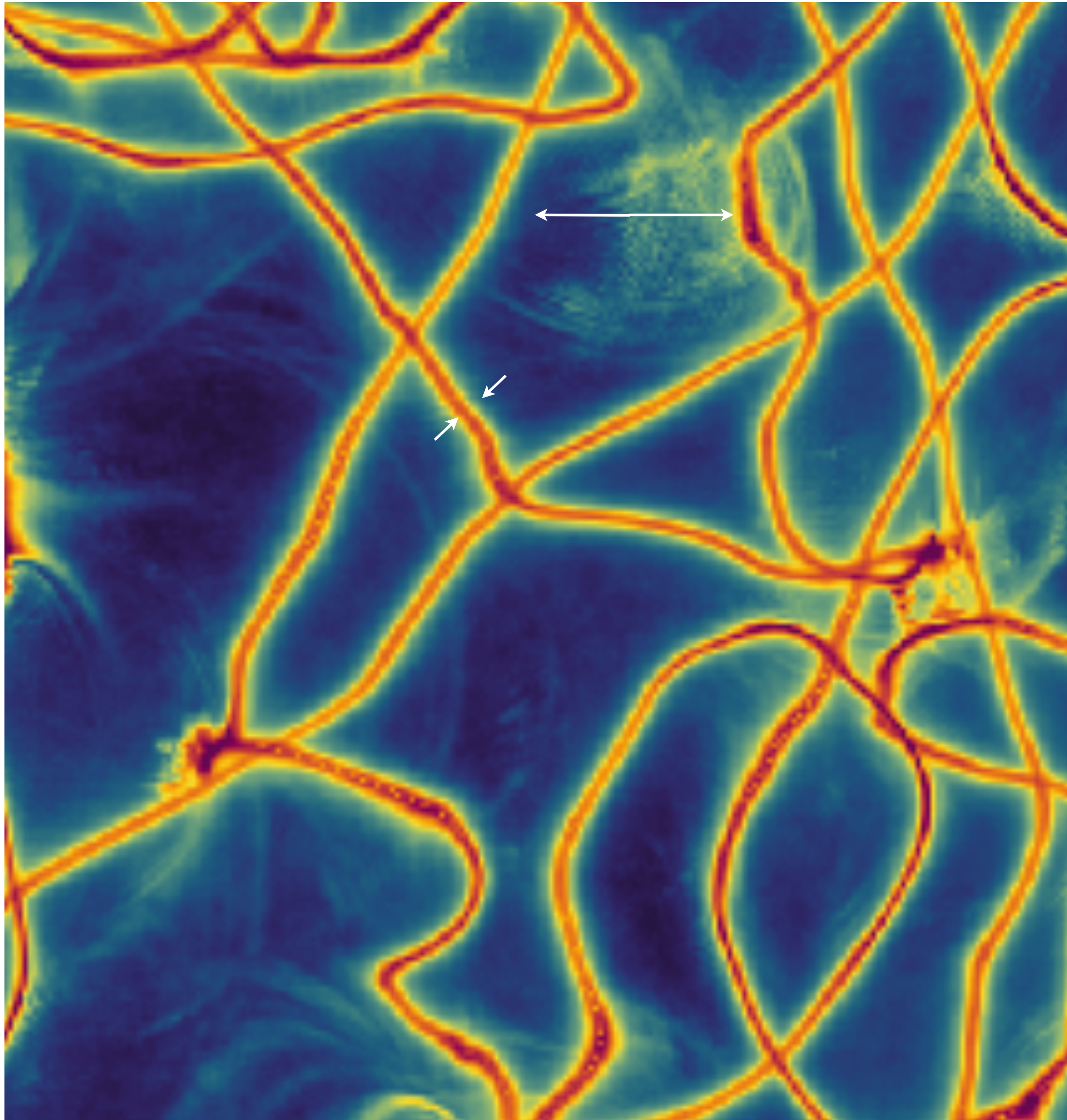
Problems for direct detection

- Encounter rate \sim once every 10^4 — 10^6 years.
- If tidally disrupted by stars we could pass through streams [2011.05377], but this implies a radically different signal model for lab experiments



- ## Opportunities for indirect detection
- Collision of miniclusters with neutron stars, observe in radio [2011.05378]
 - Miniclusters passing line of sight (microlensing) [1908.01773],[1701.04787]

Problem 2: String radiation and the dynamical range



- Want to simulate larger than the causal horizon $L \sim 1/H$
- Whilst also resolving string cores $\Delta x \sim 1/m_s = (\sqrt{\lambda}f_a)^{-1}$
- For a realistic model e.g. $f_a = 10^{11}$ GeV $\rightarrow m_s/H \sim 10^{28}$
- With current resources $\lesssim 8192^3$ grid points, can only simulate $m_s/H \sim 10^{3-4}$
- Might be okay since this parameter enters as $\log m_s/H$ in the string tension but still needs to be checked, e.g. with AMR [2108.05368]

Summary

- The axion is the best candidate for dark matter
- The axion could be found tomorrow, or in 20 years time
- Need high-resolution numerical simulations to predict the axion mass and to study the clumpiness of axions in our Universe. Many open questions and avenues for further study

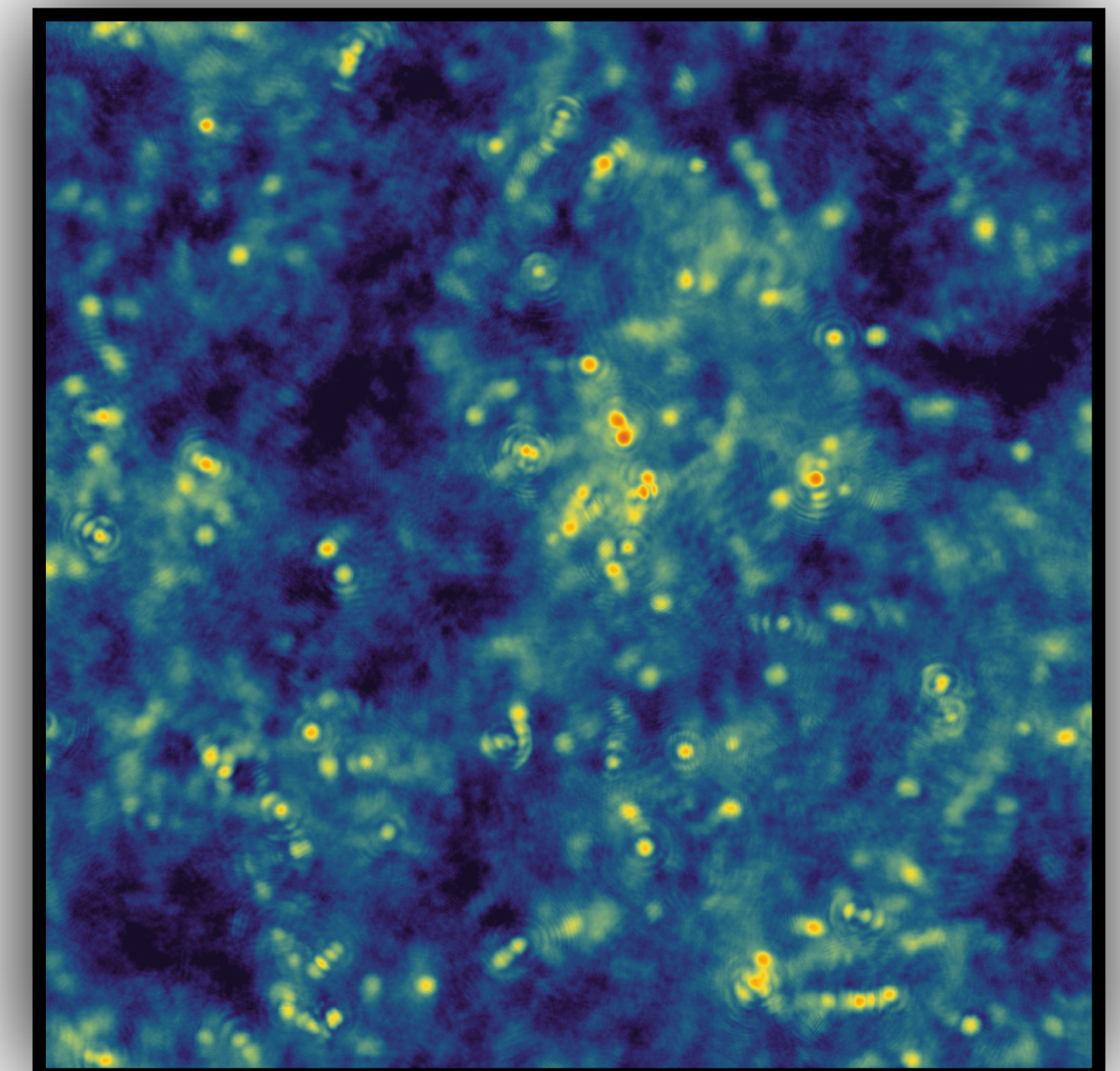
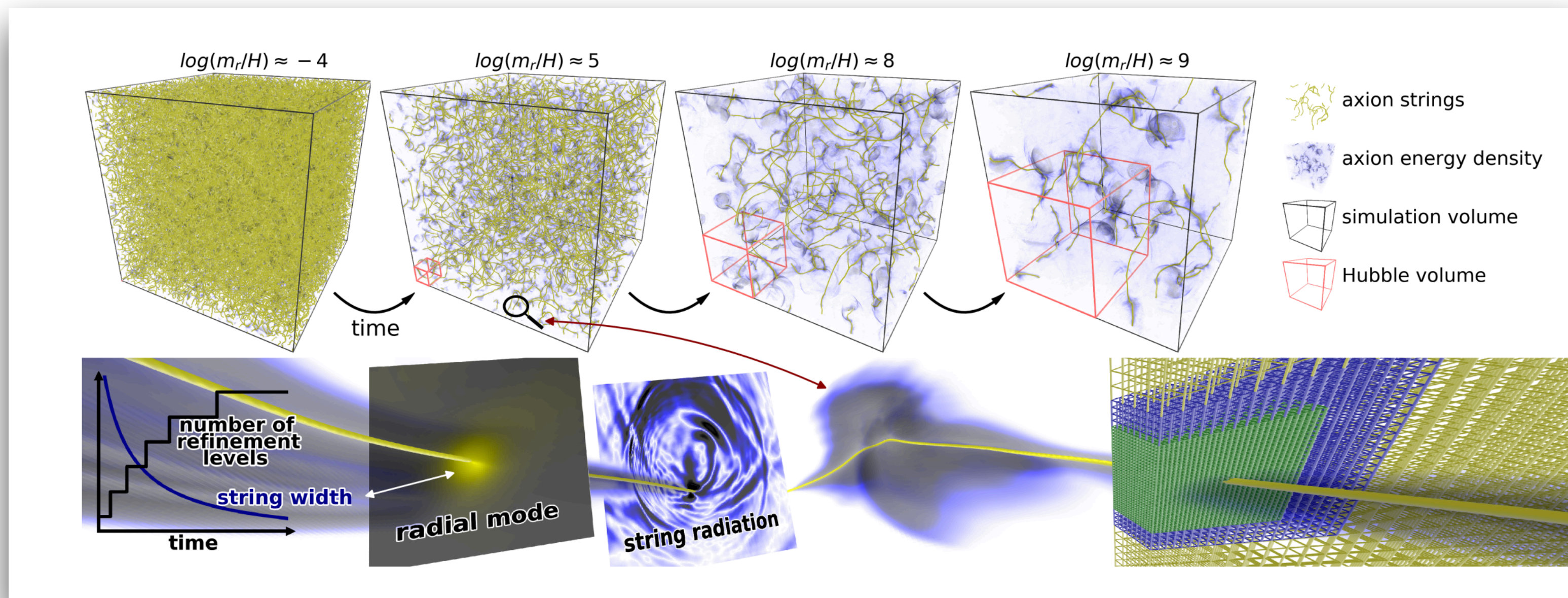
Key issues to be resolved

Axion dark matter abundance/axion mass

- Current simulations cannot study the string scaling regime in full due to high required dynamical range, see e.g. [2007.04990]
- Not clear if the spectrum is dominated by IR modes (meaning large overproduction) or UV modes (. Important for predicting the axion mass, see [2108.05368] for recent work with AMR

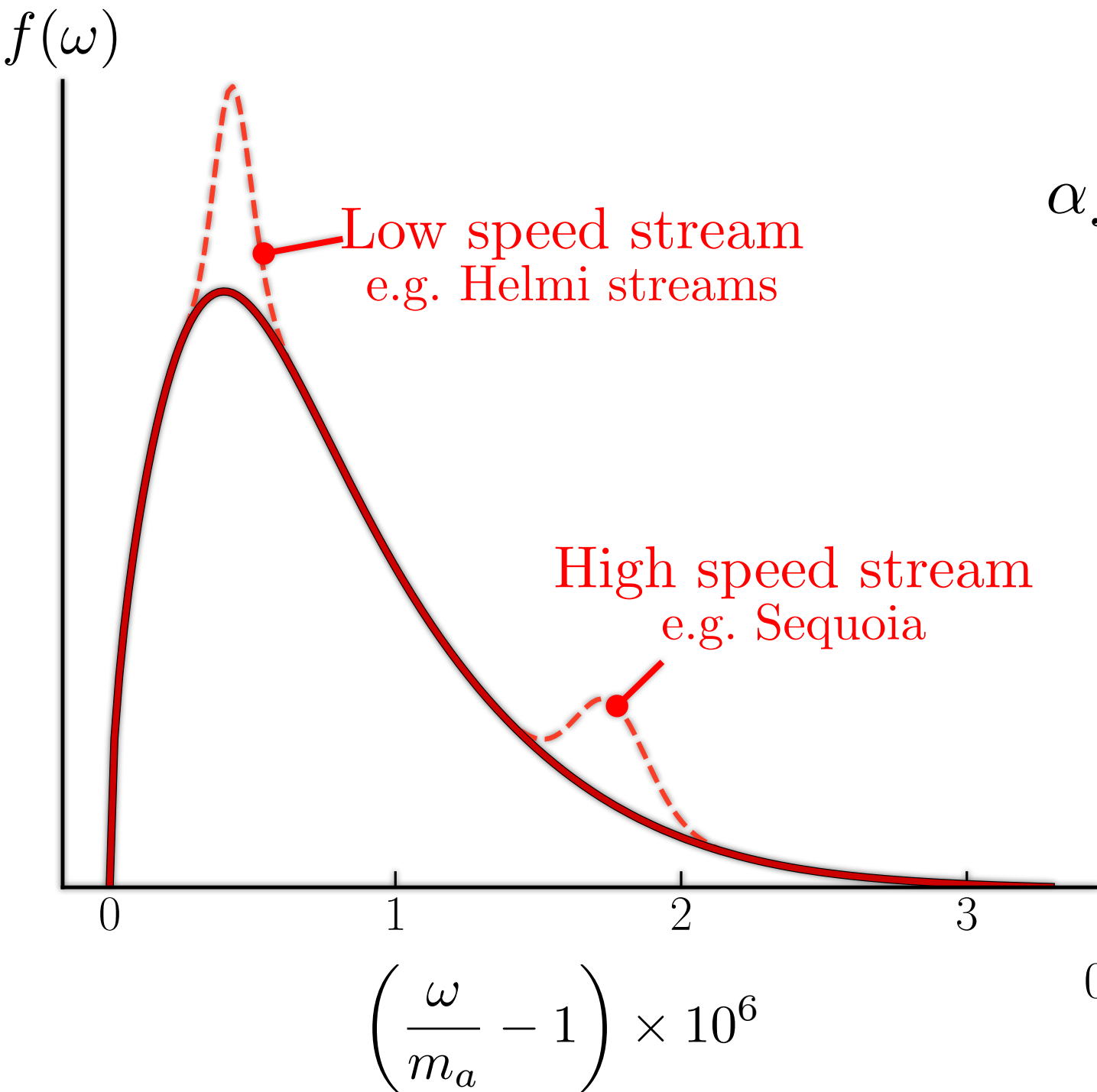
Implications of an inhomogeneous axion distribution

- Formation of gravitationally bound structures “axion miniclusters”
- Do miniclusters survive to present day? Could be important for direct and indirect searches
- Can stable axion stars form? Could there be signals of these e.g. fast radio bursts?

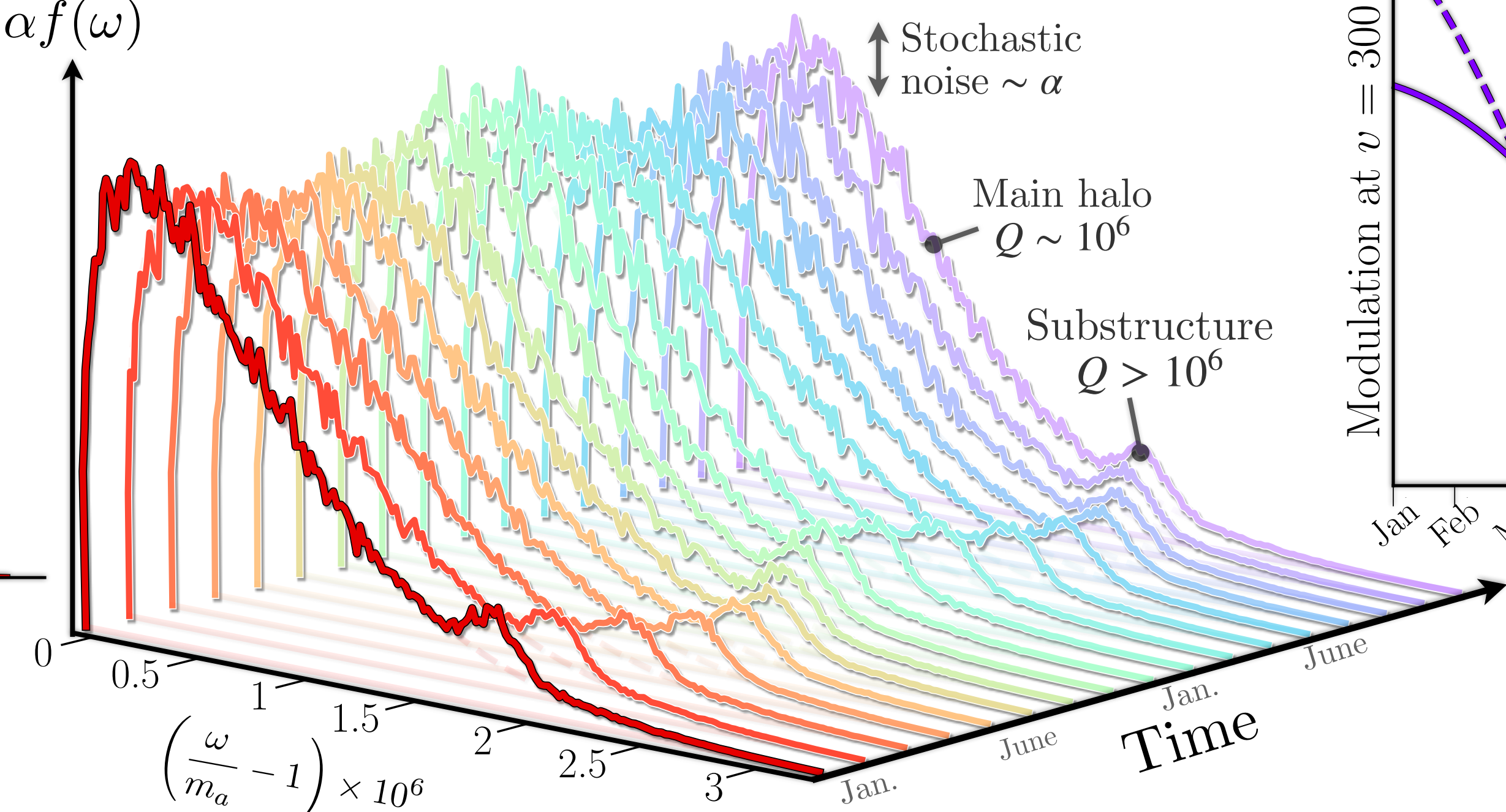
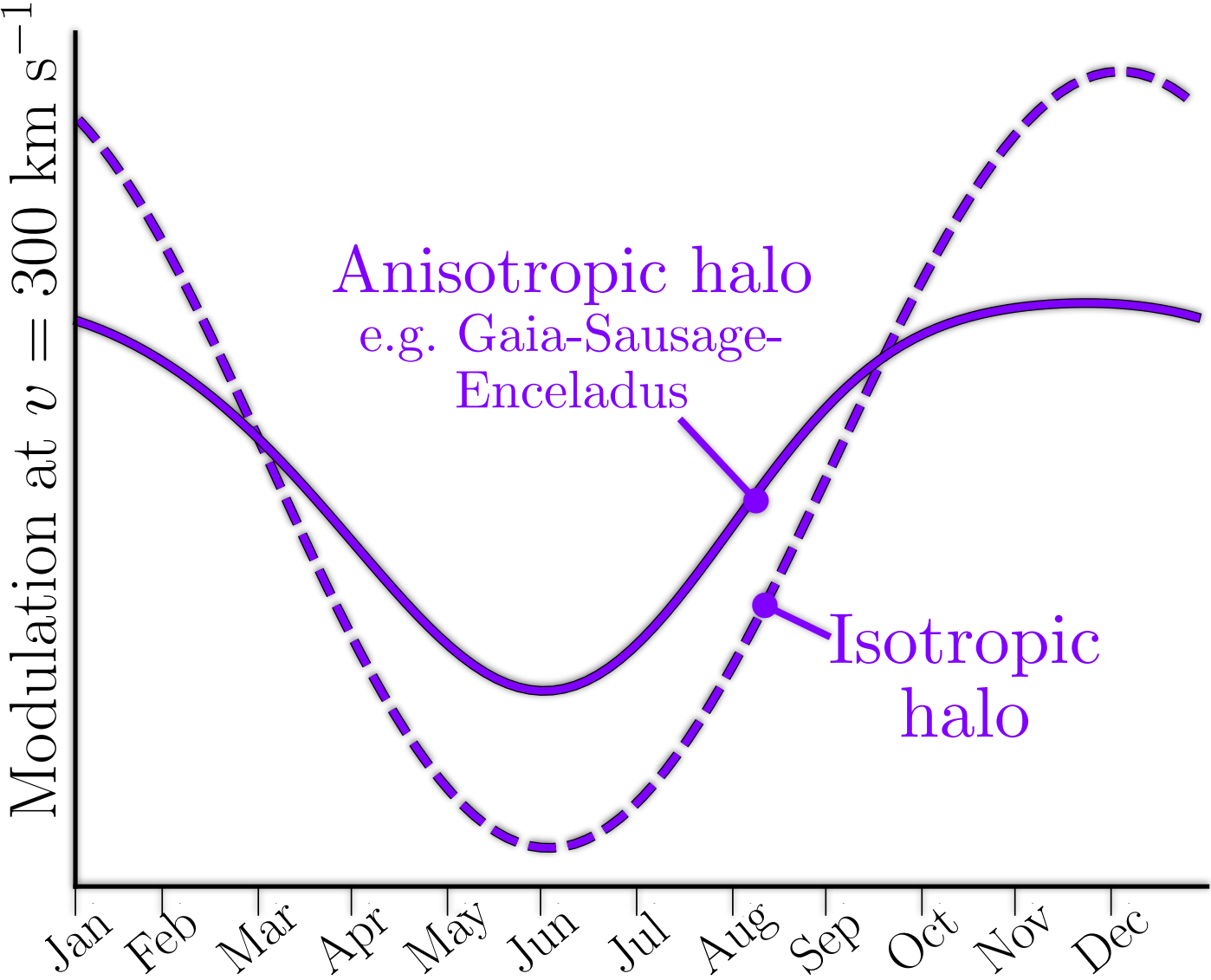


The axion lineshape

Effect of substructure

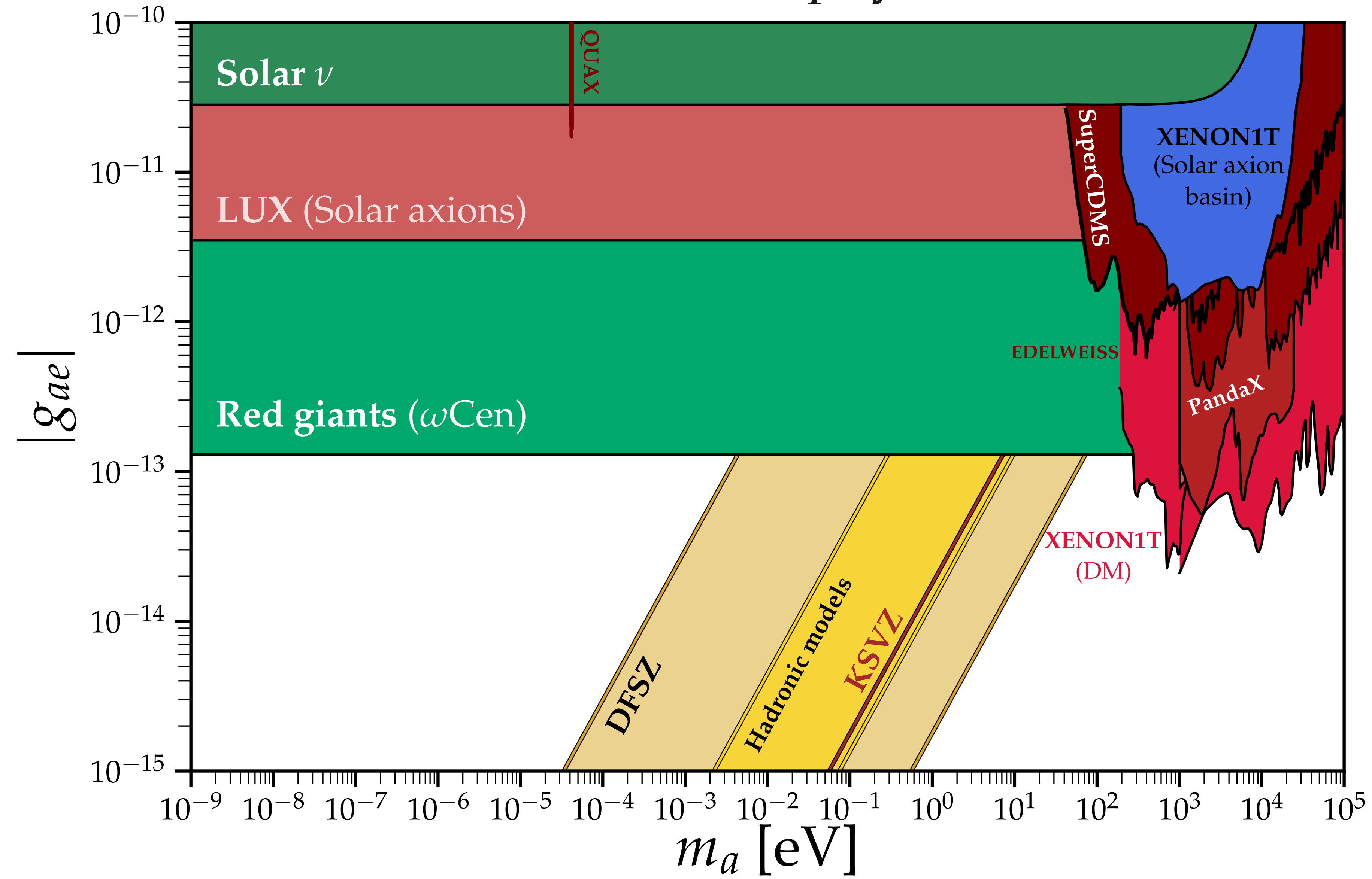


Effect of halo anisotropy



Fermion couplings, e.g. axion-electron.

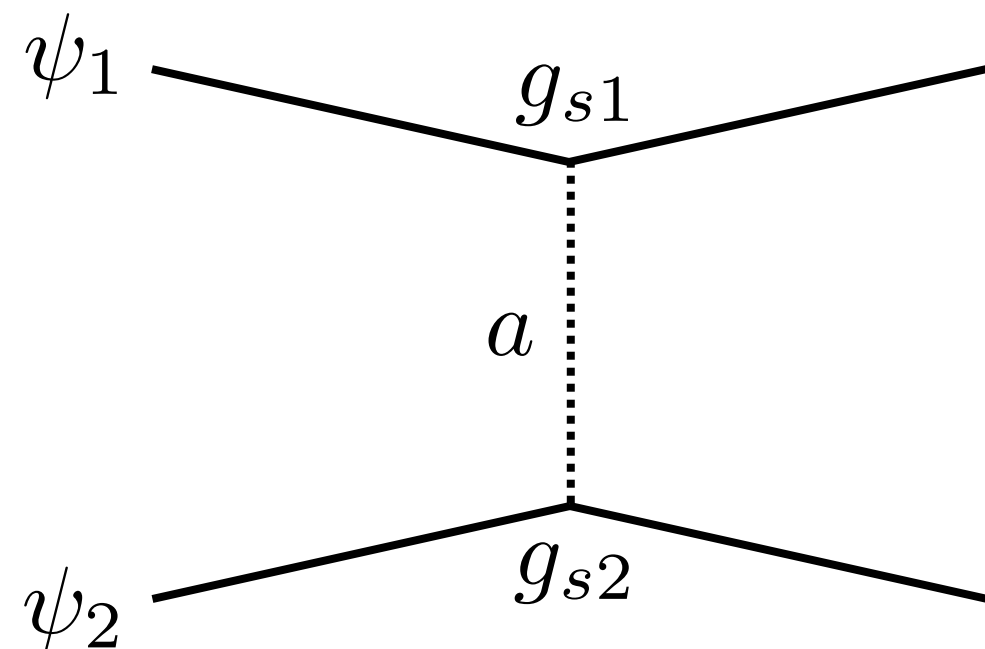
→ Hard to beat astrophysical bounds



Pure laboratory tests of axion-fermion fifth forces

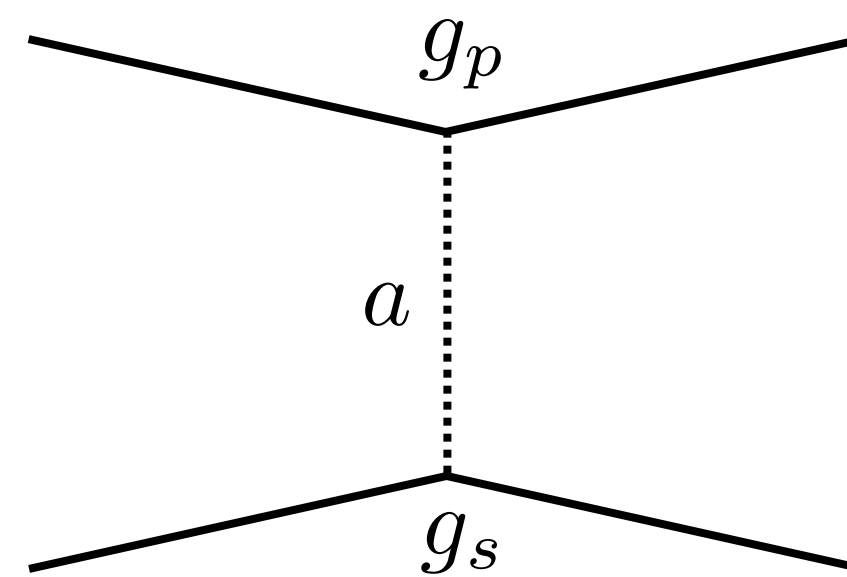
Key point: any SM or BSM CP-violation (could be e.g. size of Jarlskog invariant of CKM matrix) could shift axion vev and generate **CP-violating** axion-fermion couplings in addition to the **CP-conserving** ones

$$\mathcal{L} \supset -a \sum_{\psi} \underline{g_p^{\psi}} (i\bar{\psi}\gamma^5\psi) - a \sum_{\psi} \underline{g_s^{\psi}} (\bar{\psi}\psi)$$



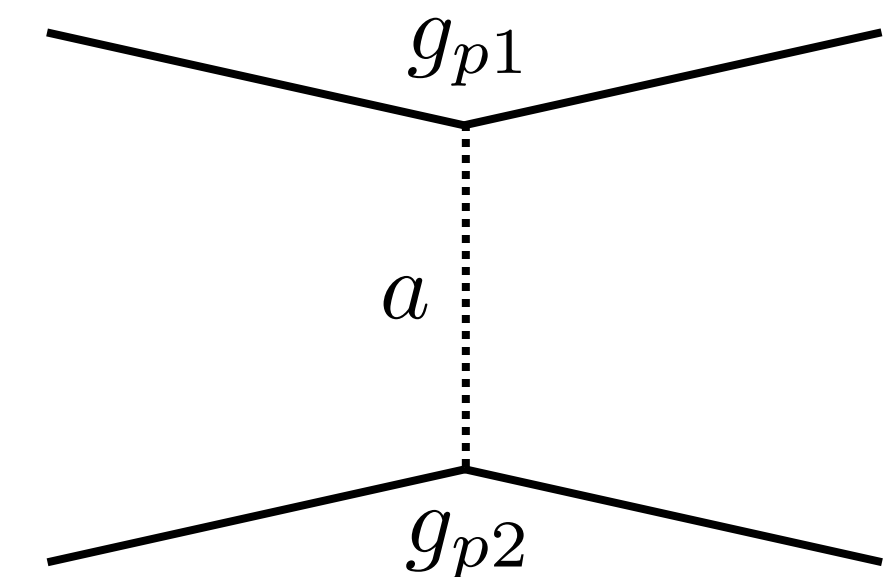
**Monopole-monopole
(Spin independent)**

→ e.g. tests of inverse square law / WEP



**Monopole-dipole
(Spin dependent)**

→ Spin-mass forces e.g. ARIADNE / QUAX



**Dipole-dipole
(Spin dependent)**

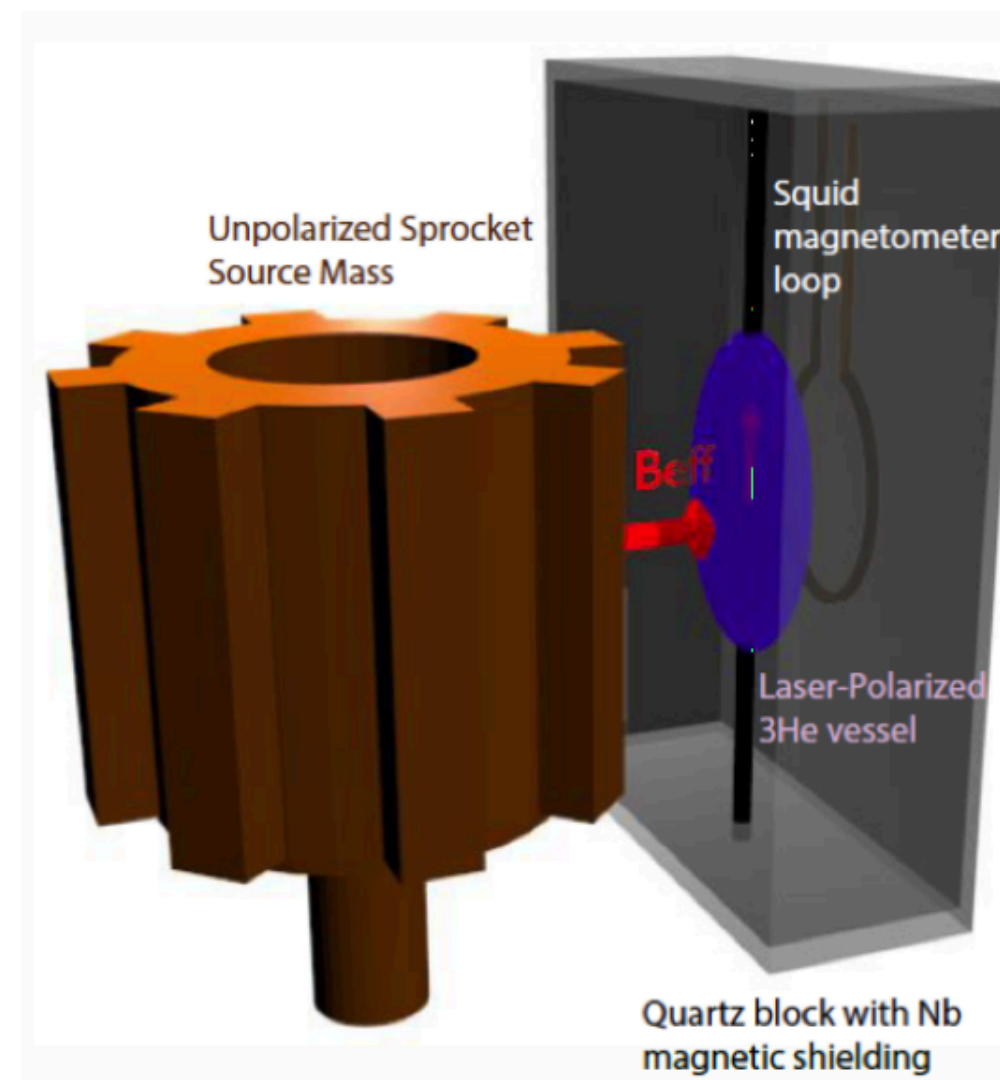
→ Forces between spin-polarised samples

Monopole-dipole searches

Conceptually similar, spin an unpolarised source mass near to a spin-polarised target

ARIADNE

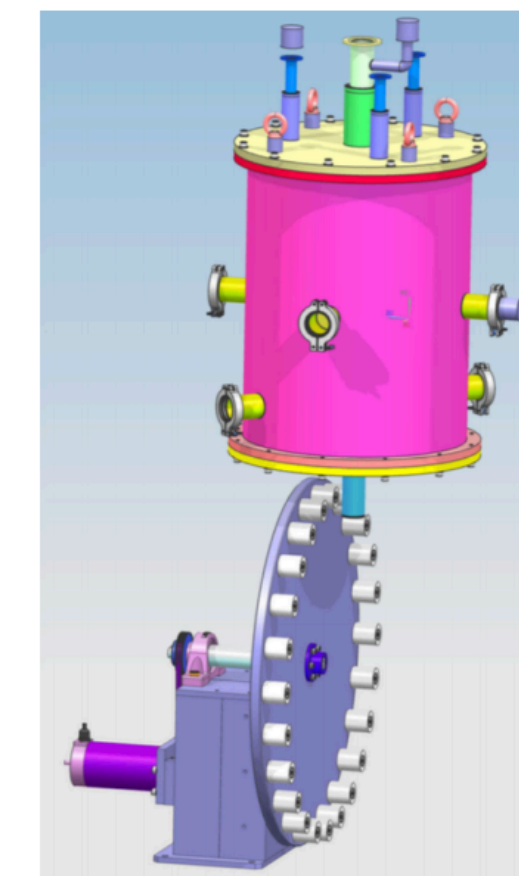
Constrains: g_p g_s (nucleon-nucleon)



QUAX

Constrains: g_p g_s (electron-nucleon)

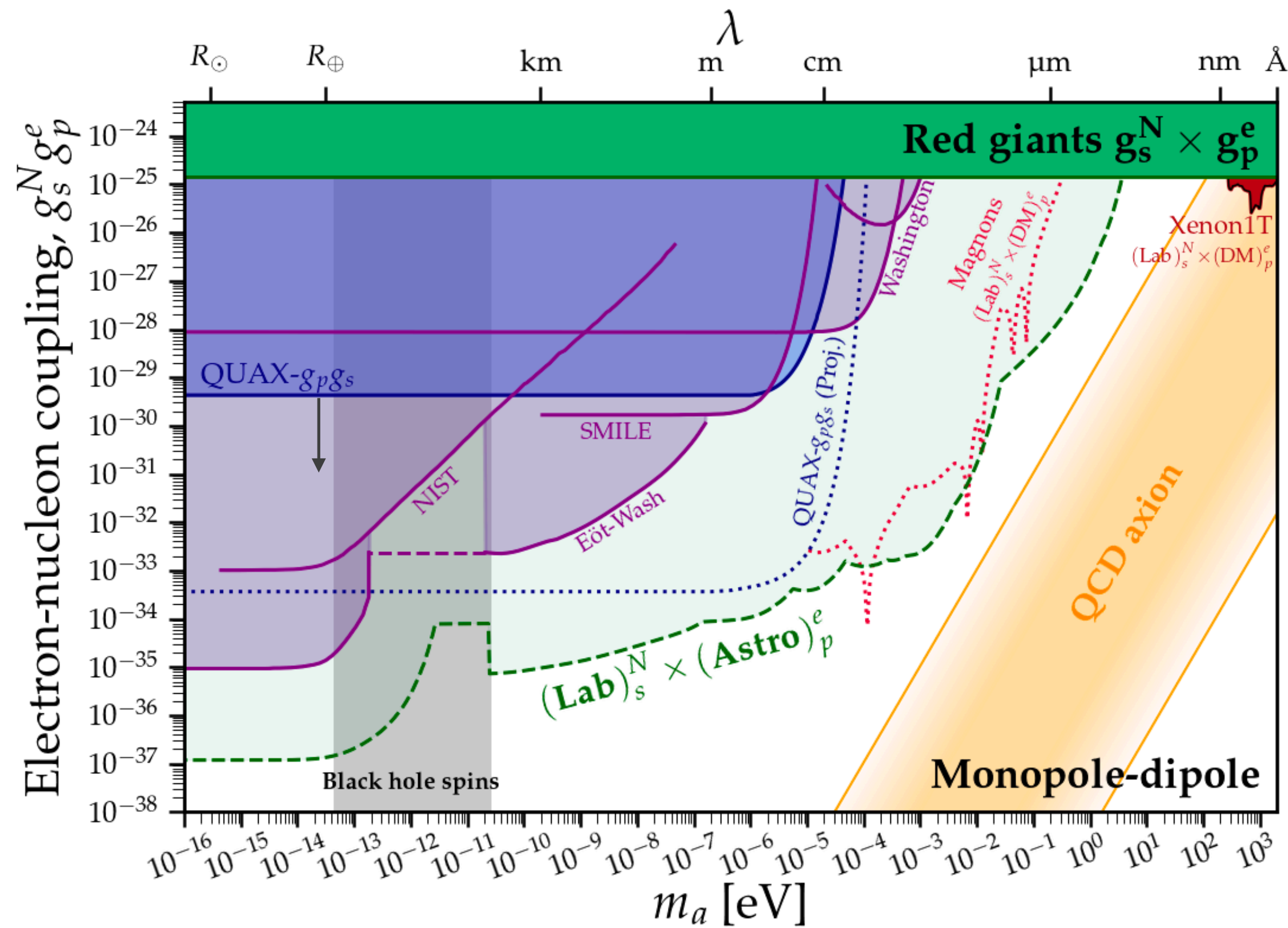
(Latest QUAX result 2011.07100)



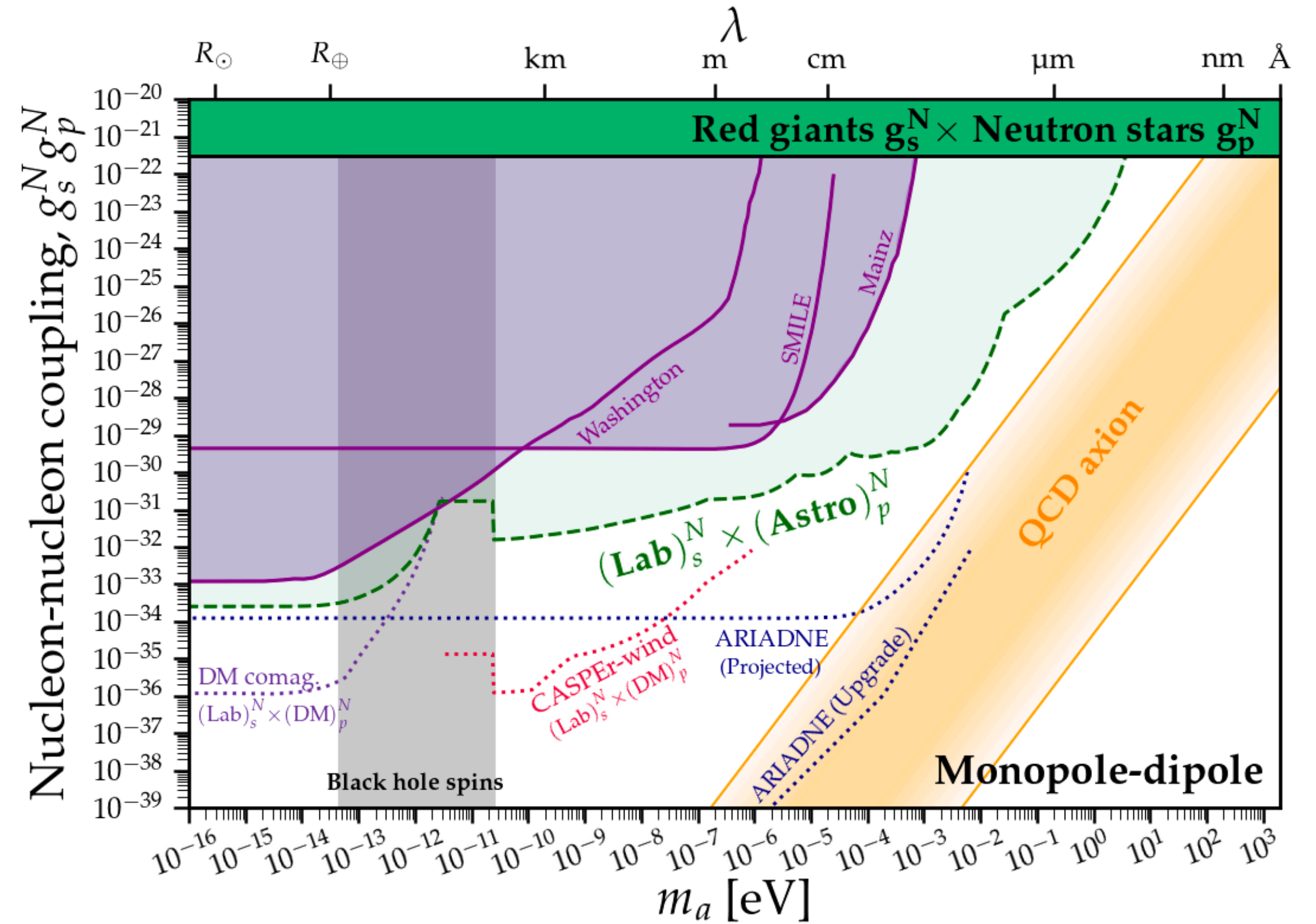
Challenge: stellar bounds tightly constrain g_p , and spin independent fifth force tests easily constrain g_s : so Astro x Lab bound on these coupling combos are very strong

Pure laboratory tests for monopole-dipole axion-mediated forces

Electron-nucleon coupling



Nucleon-nucleon coupling



Hard to beat the **astrophysical bounds**, but ARIADNE projects that it will

$$\Delta_k^2 = \frac{k^3}{2\pi^2} \frac{1}{V} \langle |\tilde{\delta}(\mathbf{k})|^2 \rangle_{|\mathbf{k}|=k}$$

Evolution of dimensionless variance in the density contrast

